The term structure of judgement: interpreting survey disagreement

Federica Brenna and Žymantas Budrys

CEFER - Bank of Lithuania and Vilnius University

Aug 29, 2024 EEA-ESEM 2024 Rotterdam

The views expressed are those of the authors and do not necessarily reflect those of the Bank of Lithuania or the Eurosystem

The forecasting process is a "black box", but there is something we can say about it (ECB, 2019, 2024; Stark, 2013):

- At short horizons, respondents rely heavily on models, especially time series and a combination of models
- At every horizon, the majority of respondents incorporates at least some judgement to their model forecasts

The forecasting process is a "black box", but there is something we can say about it (ECB, 2019, 2024; Stark, 2013):

- At short horizons, respondents rely heavily on models, especially time series and a combination of models
- At every horizon, the majority of respondents incorporates at least some judgement to their model forecasts

Professionals are well informed agents, yet they disagree: Q1: why? Figure

- Because of interpreting information differently?
- Because they have different models?
- Mix of both?

Focus on **interpreting** survey forecasts and disagreement across respondents **structurally**.









Related Literature and Contribution

- Propose a novel way of combining models and forecasts: exploit the information contained in the term structure of individual forecasts to estimate and identify coefficients of a VAR model
 - Bańbura, Brenna, et al., 2021; Bańbura, Leiva León, et al., 2021; Ganics and Odendahl, 2021; Monti, 2010; Robertson et al., 2005
- Offer a deeper look into structural disagreement through time
 - Andrade et al., 2016; Dovern, 2015; Rich and Tracy, 2021 (empirical); Andre et al., 2022; Herbst and Winkler, 2021 (structural)
- Shed further light on professional forecasters' expectation formation process: we do not take a specific stance on the microfoundations behind the process, but model expectations in a flexible, reduced form.
 - Born et al., 2020; Farmer et al., 2021 (sticky information), Casey, 2021 (over-reaction), Dovern and Hartmann, 2017; Giacomini et al., 2020 (heterogeneous forecasters)

Model for the term-structure of forecasts

Each respondent *i* runs a VAR+SV (here simplified):

$$y_t = \beta y_{t-1} + A_0^{-1} e_t$$
 $e_t \sim \mathcal{N}(0, \Lambda_t)$

The optimal **model** forecast done at time *t* would correspond to:

$$y_{t+1|t} = \beta y_t \qquad \qquad y_{t+h|t} = \beta^h y_t$$

If we assumed agents have:

- same available data
- same model
- same priors

we would not see any disagreement, which however we observe in the SPF forecasts.

Each respondent *i* runs a VAR+SV (here simplified):

$$y_t = \beta_i y_{t-1} + A_{0,i}^{-1} e_{t,i} \qquad \qquad e_{t,i} \sim \mathcal{N}(0, \Lambda_{t,i})$$

The optimal **model** forecast done at time *t* would correspond to:

$$y_{t+1|t,i} = \beta_i y_t \qquad \qquad y_{t+h|t,i} = \beta_i^h y_t$$

Instead, we allow for the possibility that forecasters:

use different models

Each respondent *i* runs a VAR+SV (here simplified):

$$y_t = \beta_i y_{t-1} + A_{0,i}^{-1} e_{t,i}$$
 $e_{t,i} \sim \mathcal{N}(0, \Lambda_{t,i})$

The forecast done at time t would correspond to:

$$y_{t+1|t,i} = \beta_i y_t + A_{0,i}^{-1} e_{t+1|t,i} \quad y_{t+h|t,i} = \beta_i^h y_t + A_{0,i}^{-1} e_{t+h|t,i} + \dots + \beta_i^{h-1} A_{0,i}^{-1} e_{t+1|t,i}$$

Instead, we allow for the possibility that forecasters:

- use different models
- incorporate some judgement

$$y_{t+1|t,i} = \beta_i y_t + A_{0,i}^{-1} e_{t+1|t,i} \quad y_{t+h|t,i} = \beta_i^h y_t + A_{0,i}^{-1} e_{t+h|t,i} + \dots + \beta_i^{h-1} A_{0,i}^{-1} e_{t+1|t,i}$$

Formulation of forecasts in this way has its advantages:

- aligns with conditional forecasting methods (Waggoner & Zha, 1999)
- no new parameters \rightarrow more precise estimates

$$y_{t+1|t,i} = \beta_i y_t + A_{0,i}^{-1} e_{t+1|t,i} \quad y_{t+h|t,i} = \beta_i^h y_t + A_{0,i}^{-1} e_{t+h|t,i} + \dots + \beta_i^{h-1} A_{0,i}^{-1} e_{t+1|t,i}$$

Formulation of forecasts in this way has its advantages:

- aligns with conditional forecasting methods (Waggoner & Zha, 1999)
- **no** new parameters \rightarrow more precise estimates

Problem: estimation can be cumbersome due to the non-linearity

 $y_{t+1|t,i} = \beta_i y_t + A_{0,i}^{-1} e_{t+1|t,i} \quad y_{t+h|t,i} = \beta_i^h y_t + A_{0,i}^{-1} e_{t+h|t,i} + \dots + \beta_i^{h-1} A_{0,i}^{-1} e_{t+1|t,i}$

Formulation of forecasts in this way has its advantages:

- aligns with conditional forecasting methods (Waggoner & Zha, 1999)
- **no** new parameters \rightarrow more precise estimates

Problem: estimation can be cumbersome due to the non-linearity **Assumption:** We assume that judgement is distributed independently it buys computational convenience but also adheres to structural interpretation

$$y_{t+h|t,i} = \beta_i y_{t+h-1|t,i} + A_{0,i}^{-1} e_{t+h|t,i}$$

 $y_{t+1|t,i} = \beta_i y_t + A_{0,i}^{-1} e_{t+1|t,i} \quad y_{t+h|t,i} = \beta_i^h y_t + A_{0,i}^{-1} e_{t+h|t,i} + \dots + \beta_i^{h-1} A_{0,i}^{-1} e_{t+1|t,i}$

Formulation of forecasts in this way has its advantages:

- aligns with conditional forecasting methods (Waggoner & Zha, 1999)
- **no** new parameters \rightarrow more precise estimates

Problem: estimation can be cumbersome due to the non-linearity **Assumption:** We assume that judgement is distributed independently it buys computational convenience but also adheres to structural interpretation

$$y_{t+h|t,i} = \beta_i y_{t+h-1|t,i} + A_{0,i}^{-1} e_{t+h|t,i}$$

Price: it does not adhere to intricacies of expectation formation literature

Philadelphia FED SPF and Real Time Dataset for Macroeconomists: Onto

- sample 1984q2-2022q2
- 6 variables: real GDP growth, investment, term spread, AAA-10y spread, CPI inflation, 3-month T-bill
- For every quarter q, observed data and forecasts between quarter q-1 and q+4

- Two main specifications:
 - "Average" respondent
 - Individual models (63 respondents)

Historical decomposition of GDP nowcast and one-year ahead forecast





Historical decomposition of GDP nowcast and one-year ahead forecast



Judgement is **pervasive** in SPF consensus forecasts. But does it help?

CPI Equation HD

Judgement and forecast accuracy

Yes, judgement aids accuracy at short horizons and particularly during crises



Note: The figure shows the percentage gains in terms of root mean squared error (RMSE) for the SPF forecasts compared to model-consistent unconditional forecasts.

Possible explanation: Judgement about nowcast reflects high-frequency and timely info, which is available between the first macro release and the survey submission

Impulse response functions: shocks' labelling

We exploit **heteroskedasticity** for identification, but we still need to provide an economic interpretation.

- $1 \rightarrow$ label shocks by looking at signs of impulse responses
- 2
 ightarrow compare shocks with 150 others in literature, check if valid instruments 📃

Identified shocks:

- I Unanticipated demand (Mertens & Ravn, 2012, 2013; Romer & Romer, 2010)
- 2 Unanticipated supply
- 3 Anticipated demand
- 4 Financial (Bassett et al., 2014; Bloom, 2009; Gilchrist & Zakrajšek, 2012)
- 5 Cost-push (Baumeister, 2023; Känzig, 2021) 🥌
- 6 "Interest rate"



Impulse response functions: individual models



Cross-sectional disagreement

IRFs across individual forecasters present some parameter heterogeneity. But how important is it to explain forecasts dispersion?

We re-arrange terms to isolate the two effects...

$$y_{t+h|t,i} = \underbrace{\left(\sum_{j=0}^{h-1} \beta_{j}^{j}\right) c_{i} + \beta_{i}^{h} y_{t} + \sum_{k=1}^{N} \left(\sum_{j=1}^{h} \psi_{h-j,i,1} \bar{\varepsilon}_{t+j|t,k}\right)}_{\tilde{y}_{h,t,i}(\text{different coefficients})} + \underbrace{\sum_{k=1}^{N} \left(\sum_{j=1}^{h} \bar{\psi}_{h-j,1} \varepsilon_{t+j|t,i,k}\right)}_{\tilde{\varepsilon}_{h,t,i}^{(1,...,N)}(\text{different expected shocks})}$$

 \ldots and calculate the cross-sectional variance as the covariance between each right-hand side term and the left-hand side.

Cross-sectional disagreement of 1-year-ahead GDP forecasts



Cross-sectional disagreement of 1-year-ahead CPI forecasts



- We develop a parsimonious and efficient way to incorporate the full term structure of survey forecasts into a VAR model
 - The added information content allows for sharper parameter estimates and inference
 - Our framework allows to extract judgement shocks from survey forecasts and identify them structurally using heteroskedasticity
- Judgement improves accuracy across the sample, more so in turbulent times and for nowcasts
- Two thirds of disagreement due to different judgements, remaining third due to different coefficients
- Disagreement mainly on size of shocks, not on their nature

Thank you!

Andrade, P., Crump, R. K., Eusepi, S., & Moench, E. (2016). Fundamental disagreement. Journal of Monetary Economics. Andre, P., Pizzinelli, C., Roth, C., & Wohlfart, J. (2022). Subjective models of the macroeconomy: Evidence from experts and representative samples. The Review of Economic Studies. Bańbura, M., Brenna, F., Paredes, J., & Ravazzolo, F. (2021). Combining bayesian VARs with survey density forecasts: Does it pay off? SSRN Electronic Journal. Bańbura, M., Leiva León, D., & Menz, J.-O. (2021). Do inflation expectations improve model-based inflation forecasts? European Central Bank. Bassett, W. F., Chosak, M. B., Driscoll, J. C., & Zakrajšek, E. (2014). Changes in bank lending standards and the macroeconomy. Journal of Monetary Economics. Baumeister, C. (2023, January 1). Measuring market expectations. In R. Bachmann, G. Topa, & W. van der Klaauw (Eds.), Handbook of economic expectations. Academic Press.

Bertsche, D., & Braun, R. (2022). Identification of structural vector autoregressions by stochastic volatility. *Journal of Business & Economic Statistics*.

Bloom, N. (2009). The impact of uncertainty shocks. *Econometrica*.

- Born, B., Dovern, J., & Enders, Z. (2020). Expectation dispersion, uncertainty, and the reaction to news. *SSRN Electronic Journal*.
- Casey, E. (2021). Are professional forecasters overconfident? *International Journal of Forecasting*.
- Chan, J. C. C. (2021). Minnesota-type adaptive hierarchical priors for large bayesian VARs. *International Journal of Forecasting*.
- Chan, J. C. C., Koop, G., & Yu, X. (2024). Large order-invariant bayesian VARs with stochastic volatility. *Journal of Business & Economic Statistics*.
- Dovern, J. (2015). A multivariate analysis of forecast disagreement: Confronting models of disagreement with survey data. *European Economic Review*.

Dovern, J., & Hartmann, M. (2017). Forecast performance, disagreement, and heterogeneous signal-to-noise ratios. *Empirical Economics*.
 ECB. (2019). The ECB survey of professional forecasters forecast processes and methodologies: Results of the 2018 special survey. *The ECB Survey of Professional Forecasters (SPF)*.

ECB. (2024). The ECB survey of professional forecasters. Forecast processes and methodologies: Results of the 2023 special survey. *The ECB Survey of Professional Forecasters (SPF)*.

Farmer, L., Nakamura, E., & Steinsson, J. (2021). *Learning about the long run*. National Bureau of Economic Research.

Ganics, G., & Odendahl, F. (2021). Bayesian VAR forecasts, survey information, and structural change in the euro area. *International Journal of Forecasting*.
Giacomini, R., Skreta, V., & Turen, J. (2020). Heterogeneity, inattention, and bayesian updates. *American Economic Journal: Macroeconomics*.

Gilchrist, S., & Zakrajšek, E. (2012). Credit spreads and business cycle fluctuations. *American Economic Review*.

- Herbst, E., & Winkler, F. (2021, July 1). *The factor structure of disagreement*. Social Science Research Network.
- Jarociński, M. (2010). Responses to monetary policy shocks in the east and the west of europe: A comparison. *Journal of Applied Econometrics*.
- Känzig, D. R. (2021). The macroeconomic effects of oil supply news: Evidence from OPEC announcements. *American Economic Review*.
- Lewis, D. J. (2021). Identifying shocks via time-varying volatility. *The Review of Economic Studies*.
- Litterman, R. B. (1986). Forecasting with bayesian vector autoregressions: Five years of experience. *Journal of Business & Economic Statistics*.

Mertens, K., & Ravn, M. O. (2012). Empirical evidence on the aggregate effects of anticipated and unanticipated US tax policy shocks. *American Economic Journal: Economic Policy*.

- Mertens, K., & Ravn, M. O. (2013). The dynamic effects of personal and corporate income tax changes in the united states. *American Economic Review*.
- Monti, F. (2010). Combining judgment and models. *Journal of Money, Credit and Banking.*
- Rich, R., & Tracy, J. (2021). A closer look at the behavior of uncertainty and disagreement: Micro evidence from the euro area. *Journal of Money, Credit and Banking*.
- Rigobon, R. (2003). Identification through heteroskedasticity. *The Review of Economics and Statistics*.

Robertson, J. C., Tallman, E. W., & Whiteman, C. H. (2005). Forecasting using relative entropy. *Journal of Money, Credit, and Banking.*

Romer, C. D., & Romer, D. H. (2010). The macroeconomic effects of tax changes: Estimates based on a new measure of fiscal shocks. *American Economic Review*.

Schlaak, T., Rieth, M., & Podstawski, M. (2023). Monetary policy, external instruments, and heteroskedasticity. *Quantitative Economics*.
Stark, T. (2013). SPF panelists' forecasting methods: A note on the aggregate results of a november 2009 special survey. *Federal Reserve Bank of Philadelphia*.
Waggoner, D. F., & Zha, T. (1999). Conditional forecasts in dynamic multivariate models. *The Review of Economics and Statistics*.
Zellner, A., & Hong, C. (1992). Forecasting international growth rates using bayesian shrinkage and other procedures. In P. K. Goel & N. S. Iyengar (Eds.), *Bayesian analysis in statistics and econometrics*. Springer.

Background slides

Disagreement over time



Impulse response functions: average model


Impulse response functions: "average" model



Impulse response functions: individual models



Post-estimation procedure to label structural innovations (Bertsche & Braun, 2022; Schlaak et al., 2023) *but extended to a Bayesian setting [accounts for the measurement error]*:

• We assume external shocks w_t are linearly related to our shock estimates, $\hat{\varepsilon}_t$

$$w_t = \psi \hat{\varepsilon}_t + o_t$$
 $o_t \sim \mathcal{N}(0, \sigma_o^2)$ $\hat{\varepsilon}_t \sim p(\varepsilon_t, \Sigma_{\varepsilon, t})$

- Check relevance, s.t. $\psi_k \neq 0$, and exogeneity $\psi_i = 0$ for all $i \neq k$;
- In the analysis, we exploit more than 100 proxies collected from over 40 studies.

External shocks related to unanticipated demand shock

	RR10exo	MR12unc	MR2013TPI	
ψ_1	-0.024***	-0.02***	-0.023***	
ψ_2	0.001	0.001	0.001	
ψ_{3}	-0.019**	-0.013*	-0.016*	
$\psi_{ extsf{4}}$	-0.011	-0.006	-0.004	
ψ_{5}	-0.004	-0.005	-0.005	Ва
ψ_{6}	-0.007	-0.002	-0.002	
Candidate	1	1	1	
$P(M_r y)$	1	1	1	
$\log_{10} BF$	7.964	8.827	8.364	
LRT	0.139	0.488	0.475	

Note: The table presents the coefficients obtained from regressing shocks from the literature on our shock estimates. Asterisks denote levels of high probability density intervals when the zero value is not included (***=99%, **=95%, *=90%). "Candidate" is the shock with the highest absolute coefficient, " $P(M_r|y)$ " is the posterior probability of the restricted model (i.e. the model including only the most relevant shock) to be preferred, "log₁₀(Bayes F.)" is the logarithm of Bayes' factor in favour of the restricted model, and "LRT p-value" is the p-value from the likelihood ratio test.

External shocks related to **financial** shock

	BCDZ14	GZ12	NB09	NB09FMT	NB09MMT
ψ_1	-0.003	-0.005	-0.006	0.002	-0.001
ψ_2	0.001	0	0.001	-0.001	-0.001
ψ_{3}	-0.001	0.006	0.014*	0	0
$\psi_{ extsf{4}}$	0.038**	0.09***	0.064***	0.013**	0.016***
ψ_{5}	0.006	-0.004	-0.001	-0.001	0
ψ_{6}	0.007	0.01	-0.004	0.002	0.002
Candidate	4	4	4	4	4
$P(M_r y)$	1	1	1	1	1
$\log_{10} BF$	9.035	9.013	8.731	11.506	11.473
LRT	0.775	0.39	0.249	0.781	0.665

External shocks related to **cost-push** shock

	DK21s	HAM03b	BH2022E	CCI19inst
ψ_1	-0.003	0.001	0	0.006
ψ_2	-0.002	-0.004*	-0.002	0.001
ψ_{3}	-0.005	0.001	0.004	-0.003
$\psi_{ extsf{4}}$	-0.001	0.014	-0.009	0.009
ψ_{5}	0.013***	0.013***	0.018***	-0.01**
ψ_{6}	0.011	0.001	0.005	0.009
Candidate	5	5	5	5
$P(M_r y)$	1	1	1	1
$\log_{10} BF$	8.553	8.746	9.084	8.766
LRT	0.443	0.509	0.815	0.712

Impulse response functions: robustness



Data Series	Transformation	Available from	Avg Periods	Avg Resp.
Real GDP	log-diff	1968:Q4	61	25 (29)
Investment	log-diff	1981:Q3	57	23 (27)
Term Spread	level	1992:Q1	52	22 (27)
AAA-10y spread	level	1992:Q1	44	18 (23)
CPI Inflation	log	1981:Q3	60	25 (29)
T-bill	diff	1981:Q3	58	24 (28)

Note: The table summarises variables used in the baseline specification, their transformation and the availability of individual responses. "Available from" is the date when forecast information became available in the SPF dataset; "Avg Periods" indicates the average number of quarters in which each respondent reported the forecast for a variable; "Avg Resp." indicates the average number of respondents at each time point in the sample, with the average from 1992q1 in brackets.



Priors

β s are mostly weakly informative but proper

 $\operatorname{vec}(\beta_{\operatorname{avg}}) \sim \mathcal{N}(\beta_0, \Sigma_{\beta}(\kappa)) \qquad \operatorname{vec}(\beta_{\operatorname{indiv}}) \sim \mathcal{N}(\widehat{\beta}_{\operatorname{avg}}, 3 \cdot I)$

For *consensus*: Chan (2021) and Litterman (1986). For *individual*: slight pooling à la Jarociński (2010) and Zellner and Hong (1992) to ensure comparability.

Similarly A₀s for consensus are assumed to follow RW, but slight pooling for individual.

$$\begin{aligned} \forall i = 1, ..., N \quad a_{avg,0,i,i} \sim \mathcal{N}(\widehat{\sigma}_{AR,i}^{-1}, 40) & \forall i \neq j \quad a_{avg,0,i,j} \sim \mathcal{N}(0, 40) \\ \forall i, j \quad a_{indiv,0,i,j} \sim \mathcal{N}(\widehat{a}_{avg,0,i,j}, 4) \end{aligned}$$

For parameters governing SV a hierarchical set-up is assumed to ensure "fatter-tails"

$$egin{aligned} &\sigma_{u,i}^2 \sim \mathcal{IG}(3/2,S_{u,i}) & S_{u,i} \sim \mathcal{G}(1.6/2,1) \ &
ho_i \sim \mathcal{N}(0.9,0.09) \mathbb{1}_{(-1<
ho<1)} \end{aligned}$$



Historical decomposition with conditional forecasts



Historical decomposition of CPI nowcast and one-year ahead forecast



- The model and its estimation capture the whole term-structure of forecasts, but we also want to identify shocks structurally
- To do that, we exploit time variation in the volatility of shocks following Bertsche and Braun (2022), Chan et al. (2024), Lewis (2021), and Rigobon (2003)
- We set the law of motion of stochastic volatility to

$$\lambda_{i,t} = \rho_i \lambda_{i,t-1} + u_{i,t} \qquad \qquad u_{i,t} \sim \mathcal{N}(0, \sigma_{u,i}^2)$$



BACK

Forecast performance gains of SPF versus unconditional forecasts



Note: The figure shows the percentage gains in terms of root mean squared error (RMSE) for the SPF forecasts compared to model-consistent unconditional forecasts: $100(1 - RMSE_{SPF}/RMSE_{UC})$.

IRFs across individual forecasters present some parameter heterogeneity. But how important is it to explain forecasts dispersion?

Historical shock decomposition for each individual *i*:

$$y_{t+h|t,i} = \underbrace{\left(\sum_{j=0}^{h-1} \beta_i^j\right) c_i + \beta_i^h y_t}_{y_{h,t,i}^{(uf)} \text{ (model forecast)}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,1} \varepsilon_{t+j|t,i,1}}_{\varepsilon_{h,t,i}^{(1)} \text{ (shock 1 judgement)}} + \ldots + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j|t,i,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \ldots + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j|t,i,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \ldots + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j|t,i,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \ldots + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j|t,i,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \ldots + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j|t,i,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j,N}}_{\varepsilon_{h,t,i}^{(N)} \text{ (shock N judgement)}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{t+j,N}}_{\varepsilon_{h,i,N}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{h,i,N}}_{\varepsilon_{h,i,N}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{h,i,N}}_{\varepsilon_{h,i,N}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{h,i,N}}_{\varepsilon_{h,i,N}} + \underbrace{\sum_{j=1}^h \psi_{h-j,i,N} \varepsilon_{h,i,N}}_{\varepsilon_{h,i,N}} + \underbrace{\sum_{j=1}^h \psi_{h-j,N} \varepsilon_{h,i,N}}$$

Cross-sectional disagreement

We re-arrange terms to isolate the two effects...

$$y_{t+h|t,i} = \underbrace{\left(\sum_{j=0}^{h-1} \beta_{i}^{j}\right) c_{i} + \beta_{i}^{h} y_{t} + \sum_{k=1}^{N} \left(\sum_{j=1}^{h} \psi_{h-j,i,1} \overline{\varepsilon}_{t+j|t,k}\right)}_{\tilde{y}_{h,t,i}(\text{different coefficients})} + \underbrace{\sum_{k=1}^{N} \left(\sum_{j=1}^{h} \overline{\psi}_{h-j,1} \varepsilon_{t+j|t,i,k}\right)}_{\tilde{\varepsilon}_{h,t,i}^{(1,\dots,N)}(\text{different expected shocks})} + \underbrace{\sum_{k=1}^{N} \left(\sum_{j=1}^{h} (\psi_{h-j,i,1} - \overline{\psi}_{h-j,1}) (\varepsilon_{t+j|t,i,k} - \overline{\varepsilon}_{t+j|t,k})\right)}_{\xi_{h,t,i}(\text{"remainder" term})} - \underbrace{\sum_{k=1}^{N} \left(\sum_{j=1}^{h} \overline{\psi}_{h-j,1} \overline{\varepsilon}_{t+j|t,k}\right)}_{\text{constant in the cross-section}}$$

 \ldots and calculate the cross-sectional variance as the covariance between each right-hand side term and the left-hand side.

Cross-sectional disagreement of 1-year-ahead Investment forecasts



Cross-sectional disagreement of 1-year-ahead Term-Spread forecasts



Cross-sectional disagreement of 1-year-ahead AAA-10y forecasts



Cross-sectional disagreement of 1-year-ahead T-bill forecasts



Estimated stochastic volatility



Forecast error variance decomposition, one-year-ahead



Forecast error variance decomposition, long-run



Historical decomposition of **GDP nowcast**



Historical decomposition of 1-year-ahead GDP forecasts



Historical decomposition of investment nowcast



Historical decomposition of 1-year-ahead investment forecasts



Historical decomposition of term spread nowcast



Historical decomposition of 1-year-ahead term spread forecasts



Historical decomposition of AAA spread nowcast



Historical decomposition of 1-year-ahead AAA spread forecasts



Historical decomposition of CPI nowcast



Historical decomposition of 1-year-ahead CPI forecasts



Historical decomposition of **T-bill nowcast**



Historical decomposition of 1-year-ahead T-bill forecasts



Historical decomposition of CPI and oil events


Posterior densities of A_0^{-1} and multimodality



— Density — Mode — Mean

