

# Strategic Informed Trading and the Value of Private Information

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joint work with  
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# Motivation

**Fact:** In many financial markets, there are investors who possess market power and asymmetric information.

- It is well-documented that large financial institutions possess the power to affect markets (Kojien and Yogo [2019], Rostek and Yoon [2023]).
- These large investors are also known to invest capital to acquire information (Kacperczyk and Pagnotta [2019]).

Price impact and private information make them “*insiders*”.

- The rest of the market knows → *Insiders' signal is partially revealed to uniformed traders through the equilibrium prices.*
- *In this paper: An insider strategically chooses the signal she reveals to the market, a fact that is recognized by the uniformed traders.*

Our goal: Study how the insider's awareness of price impact affects:

- equilibrium prices
- information transmission
- traders' welfare

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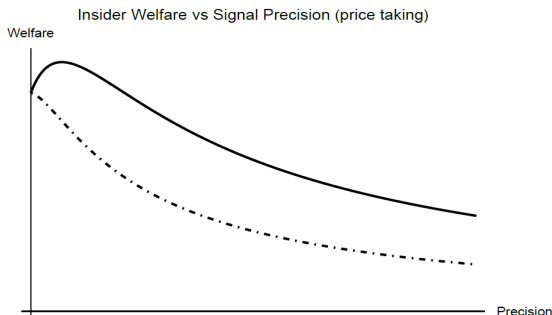
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# Welfare and Signal Precision

*Is it always true that the private information (even costless) is beneficial?*

- ▶ Paradoxically, not. On the contrary, in several models insider welfare may decrease with the signal precision!
- ▶ For example, in price-taking equilibrium of Grossman and Stiglitz [1980], we may have:

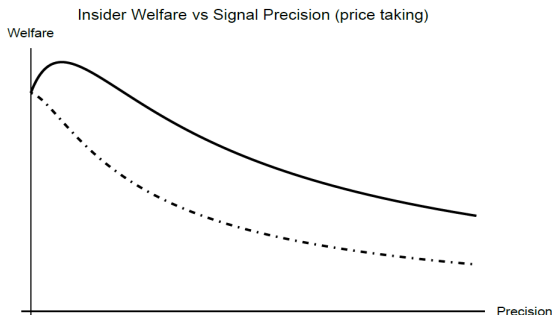


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# Contributions

We adjust the single period CARA-normal setting

- by allowing an insider to **internalize her price impact** while maintaining
- the presence of **price-taking uniformed traders** and **liquidity providers**
- and consider a **linear impact equilibrium**.

## Main results

- We establish existence of the price impact (PI) equilibrium (by getting the unique positive root of a certain cubic equation).
- On information transmission: Market signal becomes fuzzier (as in Kacperczyk et al. [2023]) and equilibrium price less reactive to the public information (as in Lou and Rahi [2023]).
- On insider's welfare: Under insider's price impact, better information always increases her welfare. While, absent a private signal, internalizing price impact always improves her welfare too.
- On the effect of private signal: Price impact may reduce the insider's welfare!
- On uniformed traders' welfare: If being at the same side of trade with the insider, their welfare increases due to price impact with and without private information.

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# A Short List of Related Literature

- ▶ **Price-impact equilibria:** Vayanos [2001] and Rostek and Weretka [2015], Malamud and Rostek [2017] and Anthropolos and Kardaras [2024] Bergemann et al. [2021]
- ▶ **Information acquisition:** Vives [2011], Rostek and Weretka [2012] and Vives [2014], Nezafat and Schroder [2023], Kacperczyk et al. [2023], Lou and Rahi [2023].
- ▶ **Information sharing:** Goldstein et al. [2023] and Indjejikian et al. [2014]).

# The Model

There is **one period** and

- a **risky asset** with terminal payoff  $X \sim N(0, 1)$  and supply  $\Pi > 0$ .
- **An insider**  $I$  who obtains a **private signal**  $G$  taking the form

$$G = X + Z_I; \quad Z_I = \frac{1}{\sqrt{p_I}} \mathcal{E}_I,$$

where  $\mathcal{E}_I \sim N(0, 1)$  is independent of  $X$  and  $p_I > 0$  is the signal precision.

- There is also a mass of price-takers **uniformed traders** whose representative agent is called  $U$ .
- Both  $I$  and  $U$  have **exponential preferences with risk tolerances**  $\alpha_I$  and  $\alpha_U$ .
- Lastly, there are **liquidity providers** (noise traders), denoted by  $N$ , with exogenous demand

$$Z_N = \frac{1}{\sqrt{p_N}} \mathcal{E}_N,$$

where  $\mathcal{E}_N \sim N(0, 1)$  is independent of both  $X$  and  $\mathcal{E}_I$ .

## The Model, *cont'd*

- $I$  and  $U$  are endowed with share **initial positions**  $\{\pi_{i,0}\}$ , which are assumed Pareto optimal absent private information

$$\pi_{i,0} = \alpha_i \widehat{\Pi} \quad i \in \{I, U\}, \quad \widehat{\Pi} := \frac{\Pi}{\alpha_I + \alpha_U}.$$

- Writing the to-be-determined equilibrium price as  $p$ , the **terminal wealth** is

$$\mathcal{W}^{\pi_i} := \pi_{i,0} p + \pi_i (X - p); \quad i \in \{I, U\}.$$

- The **equilibrium clearing condition** is

$$\Pi = \alpha_I \widehat{\psi}_I + \alpha_U \widehat{\psi}_U + Z_N,$$

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# Equilibrium Construction

We seek a **linear impact equilibrium**: The insider perceives that if she changes her position from  $\pi_{I,0} = \alpha_I \psi_{I,0}$  to  $\pi_I = \alpha_I \psi_I$ , then the price will be an affine function of her trade combined with the noise trader demand,

$$p_L(\psi_I, Z_N) = V + M \left( \psi_I - \psi_{I,0} + \frac{Z_N}{\alpha_I} \right),$$

for constants  $V, M$  that are determined in equilibrium. The insider's optimal demand for any fixed  $M$  and  $V$ :

$$\inf_{\psi \in \mathcal{A}_I} \mathbb{E} \left[ e^{-\psi_{I,0} p_L(\psi, Z_N) - \psi(X - p_L(\psi, Z_N))} \mid \sigma(G, Z_N) \right].$$

The uniformed trader's demand

$$\inf_{\psi \in \sigma(H_L)} \mathbb{E} \left[ e^{-\psi(X - p_L(H_L))} \mid \sigma(H_L) \right],$$

where the public signal is

$$H_L := G + \Lambda_L Z_N = X + Z_I + \Lambda_L Z_N.$$

Note that it has the same form as insider's signal  $G$  (except with lower precision)

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# Equilibrium Existence

## Theorem

The equilibrium price is of the form  $p_\iota(H_\iota)$ , for the price function

$$p_\iota(h_\iota) = p_0 + \frac{p_I \hat{y}}{(1 + p_I)(1 + 2\hat{y})} (h_\iota - p_0),$$

where  $p_0$  is the equilibrium price without private signal and price impact and  $\hat{y}$  is the unique positive solution of a certain cubic. The insider has optimal policy  $\hat{\pi}_{I,\iota} = \hat{\psi}_{I,\iota}(G, Z_N)/\alpha_I$  where

$$\hat{\psi}_{I,\iota}(g, z) = \frac{1}{1 + \hat{y}} (p_I g - (1 + p_I)p_\iota(h_\iota(g, z)) - \hat{y}p_0).$$

The uninformed agent has optimal policy  $\hat{\pi}_{U,\iota} = \hat{\psi}_{U,\iota}(H_\iota)/\alpha_U$  where

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# Comparison Analysis

Our comparison analysis works in two directions: **with and without price impact** and **with and without asymmetric information**. For this, we also consider

- the price-taking equilibrium (where insider doesn't exploit her price impact) and
- the no-signal equilibrium ( $p_I \rightarrow 0$ ) with and without price impact.

## Signals and price sensitivity

- ✓ Price impact decreases the precision of the public signal:  $p_{U,i} \leq p_U$ .
- ✓ The equilibrium price is less sensitive to the market signal in the price-impact equilibria: The slope of  $p_i$  wrt  $h_i$  is lower than the slope of  $p$  wrt to  $h$ .

Hence,

*by assuming the insider is a price taker, one overestimates the quality of the public signal and the reactivity of equilibrium prices.*

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# Comparison Analysis on Welfare

Following the standard literature, we calculate and compare the certainty equivalents (CEs) of traders at all equilibria:

For  $k \in \{I, U\}$  the **interim CEs** are

$$\begin{aligned} \text{CE}_{0,k}^I &= -\alpha_I \log \left( \mathbb{E} \left[ e^{-(1/\alpha_I)\widehat{\mathcal{W}}_{I,k}} \mid \sigma(G, H_k) \right] \right), \\ \text{CE}_{0,k}^U &= -\alpha_U \log \left( \mathbb{E} \left[ e^{-(1/\alpha_U)\widehat{\mathcal{W}}_{U,k}} \mid \sigma(H_k) \right] \right), \end{aligned}$$

while the **ex-ante CEs** are

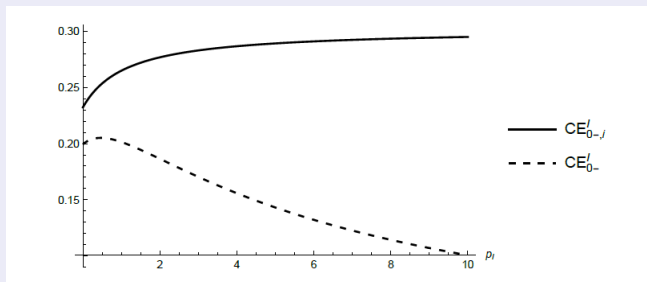
$$\text{CE}_{0-,k}^j = -\alpha_j \log \left( \mathbb{E} \left[ e^{-(1/\alpha_j)\widehat{\mathcal{W}}_{j,k}} \right] \right); \quad j \in \{I, U\},$$

where  $\widehat{\mathcal{W}}_{j,k}$  denotes the terminal wealth at each equilibrium.

# Comparison Analysis on Welfare, *cont'd*

## Signal and insider's welfare

- ✓  $CE_{0-,l}^I$  is strictly increasing in the precision  $\rho_I$  (this is not the case for  $CE_{0-}^I$ ).
  - Here is a simple example



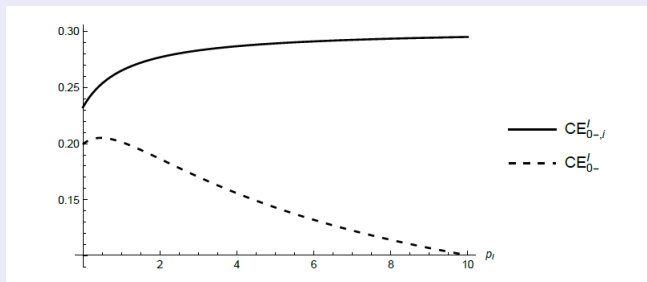
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- ✓ Price impact benefits uniformed trader:  $CE_{0-,l}^U \geq CE_{0-}^U$ .
- ✓ Both  $CE_{0-,l}^I > CE_{0-}^I$  and  $CE_{0-,l}^I < CE_{0-}^I$  are possible.

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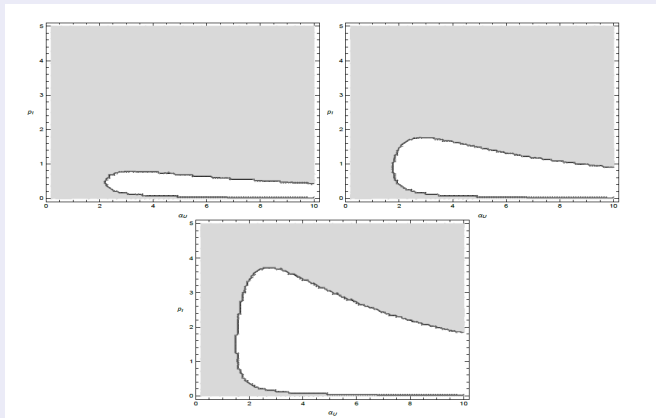


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# Comparison Analysis on Welfare, *cont'd*

Price impact may reduce insider's welfare!



The white region is where  $CE'_{0-,i} < CE'_{0-}$ .

✓ When uninformed is close to risk neutrality and signal has modest quality, then the welfare may decrease.

This holds when insider is sufficiently risk averse and  $\alpha_U^2 p_N > (1/p_I) + 1$ .



# Comparison Analysis on Welfare, *cont'd*

## Welfare in the absence of private information

$$\begin{aligned}\lim_{p_I \rightarrow 0} CE_0^I(G, Z_N) &< \lim_{p_I \rightarrow 0} CE_{0,t}^I(G, Z_N). \\ \lim_{p_I \rightarrow 0} CE_0^U(H) &< \lim_{p_I \rightarrow 0} CE_{0,t}^U(H_t)\end{aligned}$$

✓ Both traders' interim welfare a.s. increases due to price impact.

## Homogeneous case

In fact, assuming no private signal and  $\alpha_U = \alpha_I$ , we have the following a.s. order of interim CEs

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# Qualitative Comments on Equilibrium Structure

Analysis on the prices and allocations on different equilibria indicates the following messages:

- For both the PT and PI equilibria, **private signal** is expected to **increase the insider's demand and price** (albeit with a lower change in the PI equilibrium) and decrease the uniformed trader's demand.
- **Price impact** with no signal results in a **lower** (resp. higher) equilibrium position for the **insider** (resp. uniformed trader) at a **better price**.
- Due to **price impact**, a sufficiently low (resp. high) **risk tolerant insider** is expected to **buy less** (resp. more) units at a better price, while uniformed trader buys more (resp. less).

## Closing Remarks – Summary

In this paper, we study a market of risky financial assets with three types of traders: informed, uninformed and noisy traders.

- ▶ The informed trader together with her asymmetric information possesses market power due to her size.
- ▶ We model insider's price impact as her **revealing a strategically chosen signal** to the market.
- ▶ We show the **existence** of equilibrium when the uninformed traders act as price-takers (but they do take into account the insider's strategy).
- ▶ At this model, **better signal means better welfare for the insider**, while **price impact is not always a beneficial structure for her**.
- ▶ When informed and uninformed traders are at the same side of trading, **price impact increases their total welfare from trading**.
- ✓ Note that although the main analysis considers one asset and Pareto-allocated initial endowments, the paper develops the model with more assets and general traders' initial positions.

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Thank you for your attention!  
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The latest version of the paper is available at [ssrn](https://ssrn.com).