

VAGUE BY DESIGN: PERFORMANCE EVALUATION AND LEARNING FROM WAGES

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Performance evaluation is a key aspect of labor contracts and organization design

- Many ways to evaluate: Shop floor control, consumer scores, product testing, sales,...
- Digitization and AI provide a growing number of possibilities

Performance evaluations are an important source of information in the workplace

- **Inform the firm** about the worker's performance
 - Necessary basis of incentivizing effort via performance pay
 - Classic results show more information is better Holmström '79, Grossman&Hart '83
- **Inform the worker** about his performance
 - Learn about ability/match with the job
 - Confidence in his capability to succeed and sense of agency

Dual role of performance evaluation: basis of *incentives* and *agent learning*

- How do these two aspects interact?
- How to optimally design performance evaluation when it shapes worker confidence?

This Talk: Binary Case

RELATED LITERATURE

- Design of information
Kolotilin '18, Kolotilin et al. '22, Doval&Skreta '23, ...
and performance pay:
Georgiadis&Szentes '20, Hoffmann et al. '21, Li&Yang '20
- Implicit incentives and information design:
Ely&Szydlowski '20, Hörner&Lambert '21, Smolin '20
- More information can increase the cost of incentives:
Fang&Moscarini '05, Jehiel '14, Meyer&Vickers '97, Nafziger '09

The Model

THE MODEL

- Two time periods $t \in \{1, 2\}$, common discount factor δ .
- Agent
 - risk averse with utility index u and reservation utility U ($u(x)/x \rightarrow 0$ as $x \rightarrow \infty$)
 - observable but nonverifiable effort $e_t \in \{0, 1\}$ at cost $c \cdot e$
 - time-invariant ability $\theta \in \Theta = \{\theta_L, \theta_H\}$ (this talk), with prior μ_0
- Principal
 - risk neutral
 - implements high effort

TECHNOLOGY: BINARY CASE

- Output is high or low, $y_t \in \{y_L, y_H\}$ (this talk), high with probability

type \ effort	$e_t = 0$	$e_t = 1$
$\theta = \theta_L$	a	$a + b$
$\theta = \theta_H$	$a + \Delta a$	$a + b + \Delta a + \Delta b$

- Effort is productive: $b \geq 0$
- Ability is productive: $\Delta a \geq 0$
- Complementarities: Δb
 - Log-Supermodular: $\frac{\Delta b}{b} > \frac{\Delta a}{a}$
 - Log-Submodular: $\frac{\Delta b}{b} + \frac{\Delta a}{1-a} < 0$

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INFORMATION, CONTRACTS AND COMMITMENT

- At the beginning of each period, the principal commits to a contract (S, p, w) consisting of
 - a signal structure $S, p(s|y_t)$, and
 - wages w as a function the signal.

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- At the beginning of each period, the principal commits to a contract (S, p, w) consisting of
 - a signal structure $S, p(s|y_t)$, and
 - wages w as a function the signal.
- Agent observes the contract and makes participation and effort decision
- Output is not observed
- Principal and agent observe the signal realization, wages, and effort
- Update beliefs to $\mu(s)$

THE CONTRACTING PROBLEM

First Period

$$\Pi_1 = \max_{S,p,w} \iint (y - w(s) + \delta \Pi_2(\mu(s))) dp(s|y) dF(y|1, \mu) \quad (1)$$

$$\text{s.t.} \quad \iint u(w(s)) dp(s|y) dF(y|1, \mu) - c \geq U \quad (P_1)$$

$$\iint u(w(s)) dp(s|y) dF(y|1, \mu) - c \geq \iint u(w(s)) dp(s|y) dF(y|0, \mu) \quad (IC_1)$$

Second Period

$$\Pi_2(\mu) = \max_{S,p,w} \iint (y - w(s)) dp(s|y) dF(y|1, \mu) \quad (2)$$

$$\text{s.t.} \quad \iint u(w(s)) dp(s|y) dF(y|1, \mu) - c \geq U \quad (P_2)$$

$$\iint u(w(s)) dp(s|y) dF(y|1, \mu) - c \geq \iint u(w(s)) dp(s|y) dF(y|0, \mu) \quad (IC_2)$$

2nd Period and Continuation Value

THE 2ND PERIOD

- Pure incentive problem, no motive to shape learning
- Classic result:

Proposition

The optimal evaluation in the final period is fully informative.

$$\int \Pi_2(\mu) dm(\mu)$$

- What is the impact of more information about the agent's type?

$$\int \Pi_2(\mu) dm(\mu)$$

- What is the impact of more information about the agent's type?
 1. Principal can tailor the contract to the agent's ability
 - Filter out the impact of ability: contract less risky
 - Increases continuation profit
 2. Agent has more information when choosing effort
 - More expensive to satisfy incentive compatibility
 - Decreases continuation profit

THE CONTINUATION VALUE: THE IMPACT OF INFORMATION

$$\int \Pi_2(\mu) dm(\mu)$$

- What is the impact of more information about the agent's type?

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} scales with Δa :
impact of ability

2. Agent has more information when choosing effort

- More expensive to satisfy incentive compatibility
- Decreases continuation profit

} scales with Δb :
interaction of
effort and ability

THE BINARY CASE: LEARNING IS COSTLY

- Second-period IC:

$$u(w_H) - u(w_L) = \frac{c}{b + \mu\Delta b}$$

THE BINARY CASE: LEARNING IS COSTLY

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$$u(w_H) - u(w_L) = \frac{c}{b + \mu\Delta b}$$

- Required bonus inversely proportional to a linear function of beliefs
 - Agent with high impact ($b + \mu\Delta b$) cheaper to motivate
 - Uncertain agent is cheaper to motivate
 - Given change in belief: larger effect at low impact

Proposition (under a bound on $u^{-1'''}$)

If the technology is log-supermodular, Π_2 is strictly concave and $\Pi_2''' > 0$.

If the technology is log-submodular, Π_2 is strictly concave and $\Pi_2''' < 0$.

1st Period: Posterior Space and Optimal Evaluation

- General problem is unwieldy: Rewrite as a choice of $m \in \Delta\Delta\Theta$
 - \bar{m} : distribution of posterior with fully informative evaluation

$$\Pi_1 = \max_{w, m \in \Delta[0,1]} \mathbb{E}_m [y - w(\mu) + \delta\Pi_2(\mu)] \quad (3)$$

$$\text{s.t. } \mathbb{E}_m [u(w(\mu))] - c \geq U \quad (P_1)$$

$$\mathbb{E}_m \left[\frac{1}{\mu_0(1 - \mu_0)} \frac{b + \Delta b \mu_0}{\Delta a + \Delta b} (\mu - \mu_0) u(w(\mu)) \right] \geq c \quad (IC_1)$$

$$m \leq_{MPS} \bar{m} \quad (BP)$$

Proposition (Posterior Space)

An evaluation contract (S, p, w) solves the principal's problem if and only if it induces a (w, m) that solves the belief-space problem.

SOLVING THE FULL PROBLEM

- First period: Incentives and learning
 - Incentives: More informative evaluation *decreases* agency cost *this period*
 - Learning: More informative evaluation *may increase* agency cost *next period*

SOLVING THE FULL PROBLEM

- First period: Incentives and learning
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 - Learning: More informative evaluation *may increase* agency cost *next period*
- Information design problem, with:
 - Endogenous payoffs (wages are designed)
 - Additional constraints (participation and incentive compatibility)
- Binary state does not guarantee binary evaluation (Le Treust&Tomala, 2019)

Theorem

The optimal contract in the first period is (essentially) unique. Let $v = u^{-1}$.

- If $\Pi_2''' > 0$ and v'' is decreasing, it features lower censorship.
- If $\Pi_2''' < 0$ and v'' is increasing, it features upper censorship.

THE OPTIMAL CONTRACT

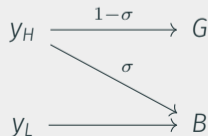
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Corollary

In the binary case with log-complements, the optimal evaluation is binary ($S = \{G, B\}$) and tough. The optimal contract consists of



- a good evaluation and associated high wage, only if output was good,
- a bad evaluation and associated low wage: always after output was bad, with prob. σ after output was good.

PROOF OF THEOREM 1: OUTLINE

$$\mathcal{L}(w, m; \underbrace{(\lambda_P, \lambda_{IC})}_{\lambda})$$

Lagrangian of the contracting problem including (P) and (IC)

Information design on the partially maximized Lagrangian (Georgiadis&Szentes '20)

PROOF OF THEOREM 1: OUTLINE

$$\mathcal{L}(w, m; \lambda)$$

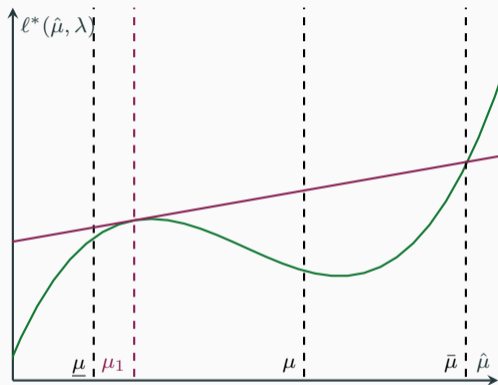
Optimal Wages given m, λ : Standard moral hazard problem $\mapsto w^*(\hat{\mu}; \lambda)$

objective is an expectation given λ : $\mathcal{L}(w^*(\hat{\mu}; \lambda), m; \lambda) = \int \ell^*(\hat{\mu}; \lambda) m(\hat{\mu}) d\hat{\mu}$

Information Design given λ : Shape of $\ell^* \mapsto m^*(\hat{\mu}; \lambda)$

$$\frac{\partial^3}{\partial \hat{\mu}^3} \ell^*(\hat{\mu}; \lambda) = \lambda_{IC}^3[\cdot] \rho''(\lambda_P + \lambda_{IC}[\cdot](\hat{\mu} - \mu)) + \delta \Pi_2'''(\hat{\mu})$$

Duality: \mapsto Solution exists and features of m^* hold in the optimal contract



- Unconstrained information design
- Payoff $\ell^*(\mu; \lambda)$
- Suppose $\frac{\partial^3}{\partial \hat{\mu}^3} \ell^*(\hat{\mu}; \lambda) > 0$
 - Convex $\Rightarrow m$ fully informative
 - Concave-convex: For low μ , agent-learning effect dominates \Rightarrow partial pooling at the bottom
- This for given λ , but $\lambda(m)$!

OPTIMAL EVALUATION: DISCUSSION

- Noisy evaluation can be optimal
 - Preserve agent's uncertainty
- Complements:
 - Selective tailored bonuses (rich Y)/tough evaluation: Avoid unwarranted praise, embrace unwarranted reprimand
 - “Drill-sergeant mentality” is part of optimal organization design
- Substitutes:
 - Capped performance pay (rich Y)/lenient evaluation
- Prevent very low posteriors
 - Costly to motivate, change in posterior has a large effect
- Result of joint design of evaluation and wages

Extensions

- Principal can acquire private information
 - Principal-preferred outcome: equivalent to optimal contract
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- Long-run commitment
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- Many periods
 - Not analytically tractable: lack of control over shape of continuation value
 - Numerically: Same structure within period; noisier evaluation early in the relationship

CONCLUSION

- Outcome of performance evaluation is a crucial source of information
 - about effort: Incentives
 - about the agent's ability: Confidence

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 - As much information as possible about effort
 - Often as little information as possible about ability
 - *In the paper*: Formalized in a more general setting

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 - *In the paper*: Formalized in a more general setting
- Optimal Performance Evaluation
 - Noisy, even though wages could condition on true y
 - Avoid very low posterior belief about the impact of effort
 - *In the paper*: Optimal evaluation upper/lower censorship policies

OUTLOOK

- Preference across given information sources: conduct, not results!
 - Salary differences between workers: mostly driven by types, so should be concealed
- Affects task design: Harder/easier to keep agents motivated
- Career Concerns: informationally opposite forces
 - information about effort and ability inseparably intertwined
 - here: source of friction; CC: source of incentives

Thank You!

UTILITY FUNCTION

- Sufficient condition on utility function
- $w = u^{-1}$, “cost of utility”

Assumption 1

1. (No incentives at probability zero) $\frac{w(x)}{x} \rightarrow \infty$ as $x \rightarrow \infty$.
2. (Decreasing curvature) $w''' \leq 0$.
3. (Bounded changes in curvature) $\frac{w'''(u_H)}{w''(u_H)} \geq -A$.

Condition

- Satisfied for CRRA $u(x) = \frac{x^{1-\gamma}}{1-\gamma}$
 - if $\gamma \leq 1/2$ and U sufficiently large.
 - Always satisfied for $\gamma = \frac{1}{2}$

STEP 1: OPTIMAL WAGES

- Let $\mathcal{L}(m, w; (\lambda_P, \lambda_{IC}))$ denote the Lagrangian associated to the problem.
- Solving for the optimal wage given λ yields

$$w^*(\hat{\mu}, \lambda) = u'^{-1} \left(\left(\lambda_P + \lambda_{IC} \frac{b + \Delta b \mu}{(\Delta a + \Delta b) \mu (1 - \mu)} (\hat{\mu} - \mu) \right)^{-1} \right)$$

- Partially maximized Lagrangian, $\sup_w \mathcal{L}(m, w; (\lambda_P, \lambda_{IC}))$, is posterior separable

$$\begin{aligned} \mathcal{L}(m, w^*(\hat{\mu}, \lambda); (\lambda_P, \lambda_{IC})) &= \int \left\{ P_\mu^1 Y + \delta \Pi_2(\hat{\mu}) - w^*(\hat{\mu}, \lambda) \right. \\ &\quad + \lambda_P (u(w^*(\hat{\mu}, \lambda)) - c - U) \\ &\quad \left. + \lambda_{IC} \left(\frac{b + \Delta b \mu}{(\Delta a + \Delta b) \mu (1 - \mu)} (\hat{\mu} - \mu) u(w(\hat{\mu}, \lambda)) - c \right) \right\} m(\hat{\mu}) d\hat{\mu} \end{aligned}$$

STEP 2: INFORMATION DESIGN

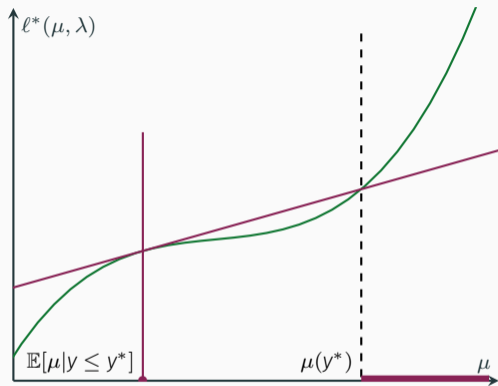
- Unconstrained information design problem with payoff $\ell^*(\hat{\mu}; \lambda)$
- The objective is either convex or concave-convex since

$$\frac{\partial^3}{\partial \hat{\mu}^3} \ell^*(\hat{\mu}; \lambda) = \lambda_{IC} \left(\frac{b + \Delta b \mu}{(\Delta a + \Delta b) \mu (1 - \mu)} \right) \frac{\partial^2}{\partial \hat{\mu}^2} u(w(\hat{\mu}; \lambda)) + \delta \Pi_2'''(\hat{\mu}) > 0$$

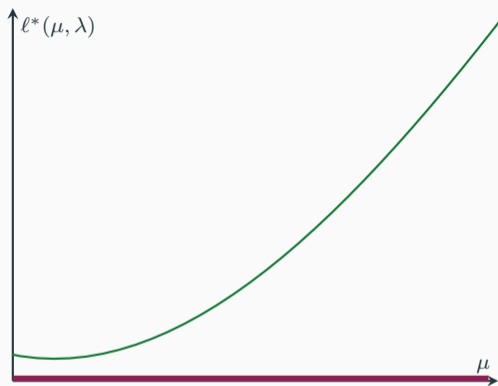
Lemma

For any λ_{IC} , there exists a unique solution to the information design problem. It induces at most two posteriors: the highest feasible posterior $\bar{\mu}$ with probability $m(\bar{\mu}) \in [0, \frac{\mu - \underline{\mu}}{\bar{\mu} - \underline{\mu}}]$ and a low posterior, $\mu^* \in [\underline{\mu}, \mu]$ with $m(\mu^*) \in [\frac{\bar{\mu} - \mu}{\bar{\mu} - \underline{\mu}}, 1]$.

STEP 2: INFORMATION DESIGN



(a) Interior solution.



(b) Corner solution.

STEP 3: STRONG DUALITY

- We need to show strong duality in the general problem, i.e.

$$\inf_{\lambda \geq 0} \sup_{w, m \text{ s.t. (BP)}} \mathcal{L}(m, w; \lambda) = \sup_{w, m \text{ s.t. (BP)}} \inf_{\lambda \geq 0} \mathcal{L}(m, w; \lambda)$$

- Two steps: [1] Wages

Lemma

The wage setting problem satisfies strong duality, i.e.

$$\sup_w \inf_{\lambda \geq 0} \mathcal{L}(m, w; \lambda) = \inf_{\lambda \geq 0} \sup_w \mathcal{L}(m, w; \lambda).$$

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- Two steps: [2] Information Design

Lemma

The information design problem satisfies strong duality, i.e.

$$\sup_{m \text{ s.t. (BP)}} \inf_{\lambda \geq 0} \int \ell^*(\hat{\mu}; \lambda) m(\hat{\mu}) d\hat{\mu} = \inf_{\lambda \geq 0} \sup_{m \text{ s.t. (BP)}} \int \ell^*(\hat{\mu}; \lambda) m(\hat{\mu}) d\hat{\mu}.$$

A SIMPLIFIED PROBLEM

- Define a simplified problem, using binary and tough evaluation

$$\max_{m_1, m_2, \mu_1, w_1, w_2} \mathbb{E}[y_1 | e = 1, \mu] + m_1(\Pi_2(\mu_1) - w_1) + m_2(\Pi_2(\bar{\mu}) - w_2) \quad (4)$$

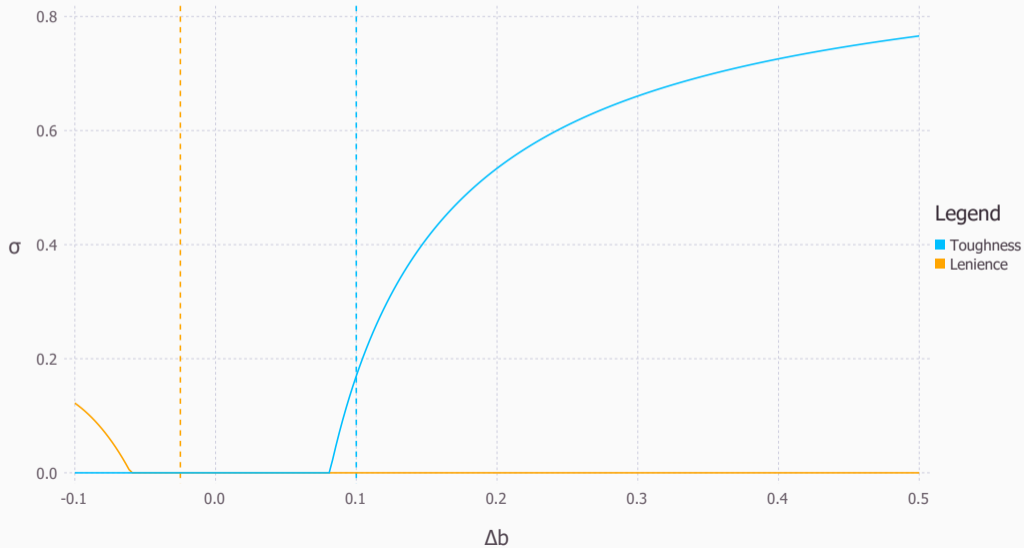
$$\text{s.t. } m_1 u(w_1) + m_2 u(w_2) - c \geq U \quad (\text{P})$$

$$\frac{b + \Delta b \mu}{(\Delta a + \Delta b) \mu (1 - \mu)} \sum_i m_i (\mu_i - \mu) u(w_i) \geq c \quad (\text{IC})$$

$$m_1 \mu_1 + m_2 \bar{\mu} = \mu; \quad m_1 + m_2 = 1; \quad \mu_1 \geq \underline{\mu} \quad (\text{BP})$$

COMPLEMENTS AND SUBSTITUTES

← BACK



Assumption (1*)

1. (No incentives at probability zero) $\frac{w(x)}{x} \rightarrow \infty$ as $x \rightarrow \infty$.
2. (Increasing curvature) $w''' \geq 0$.
3. (Bounded changes in curvature)

$$\frac{3(b + \mu\Delta b)\Delta b}{c(a\Delta b - b\Delta a)} \geq \frac{w'''(u_L)}{w''(u_L)},$$

where $u_L = U - \frac{a + \mu\Delta a}{b + \mu\Delta b}c$.

PRIVATE INFORMATION OF THE PRINCIPAL

- Principal chooses
 - Evaluation structure: observed by agent, basis of performance pay and learning
 - Private evaluation: not observed by agent, basis of learning only for principal
- Joint distribution over posteriors: $m_P(\mu_P, \hat{\mu})$
 - Agent observes $m(\hat{\mu}) = \int m_P(\mu_P, \hat{\mu}) d\mu_P$
- Dynamic game with incomplete information
- Agent updates belief based on
 - First-period evaluation
 - Second-period contract offer

PRIVATE INFORMATION OF THE PRINCIPAL

- Unique PBE with passive beliefs outcome equivalent to optimal contract without private information acquisition iff agent-determined contracts
 - Passive beliefs: no updating based on contract offer, no value of information under agent-determined condition
 - Principal preferred*
- Private information either revealed or not useful
 - If private information isn't used to adjust second period contract: irrelevant
 - Information used to adjust contract offer: revealed to agent
 - Better to also use it as a basis of performance pay

*Among equilibria that satisfy no-holdup: No rent for the agent in the second period on path.

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 - Better to also use it as a basis of performance pay
- Remains an equilibrium when principal *has to* acquire private information
- Unique[†] when private information acquisition strategy observed

*Among equilibria that satisfy no-holdup: No rent for the agent in the second period on path.

[†]Under no-holdup and no-signaling-what-you-don't-know.

UNOBSERVABLE EFFORT

- Suppose effort is not observed by the principal
- After a deviation to low effort, signal s
 - Principal has posterior

$$\hat{\mu}(s) = \mu \frac{p(s|y_L) + (a + b + \Delta a + \Delta b) [p(s|y_H) - p(s|y_L)]}{p(s|y_L) + (a + b + (\Delta a + \Delta b)\mu) [p(s|y_H) - p(s|y_L)]}$$

- Agent interprets signal differently:

$$\mu \frac{p(s|y_L) + (a + \Delta a) [p(s|y_H) - p(s|y_L)]}{p(s|y_L) + (a + \Delta a\mu) [p(s|y_H) - p(s|y_L)]}$$

- Agent has private information about the posterior

UNOBSERVABLE EFFORT

- Incentive compatibility in the second period:
 - Slack if agent more optimistic
 - Violated if agent more pessimistic
- “Belief-manipulation motive”
- Double deviations optimal
- First-period IC dynamic: Kink in the principal’s objective at prior μ

$$\int \left\{ \frac{(b + \mu\Delta b)}{\mu(1 - \mu)\Delta b} (\hat{\mu} - \mu) u(w(\hat{\mu})) - \left[1 - \frac{(b + \mu\Delta b)}{\mu(1 - \mu)\Delta b} (\hat{\mu} - \mu) \right] \max\{0, c\Delta b \frac{\mu - \hat{\mu}}{b + \hat{\mu}\Delta b}\} \right\} m(\hat{\mu}) d\hat{\mu} \geq c$$

UNOBSERVABLE EFFORT

- Under $u = \sqrt{\cdot}$ and $\Delta a = 0$: At most *three* evaluation outcomes
 - Neutral signal: Not informative about effort and ability[‡]
 - Conditional on informative evaluation: binary and tough
- Intuition: Avoid outcomes that allow generation of private information

◀ back

[‡]In simulations: Never used.

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 - Neutral signal: Not informative about effort and ability[‡]
 - Conditional on informative evaluation: binary and tough
- Intuition: Avoid outcomes that allow generation of private information
- More complicated with long-run contracting:
 - Principal can induce a learning motive by providing excessive bonuses in $t = 2$
 - Joint design of information and wages in *both periods*

◀ back

[‡]In simulations: Never used.

LONG RUN COMMITMENT: CONTINUATION VALUE

- Principal commits to contract: (S, p, w, v)
 - a signal structure $S, p(s|y)$, realization conditional on contemporaneous output
 - wages w , and
 - **continuation value v as a function the signal.**

LONG RUN COMMITMENT: CONTINUATION VALUE

- Principal commits to contract: (S, p, w, v)
 - a signal structure $S, p(s|y)$, realization conditional on contemporaneous output
 - wages w , and
 - **continuation value v as a function the signal.**
- Assume $u(x) = 2\sqrt{x}$
 - Theorem 1 goes through, delaying *payments* does not affect the mechanism
 - Optimal evaluation: binary and weakly tough

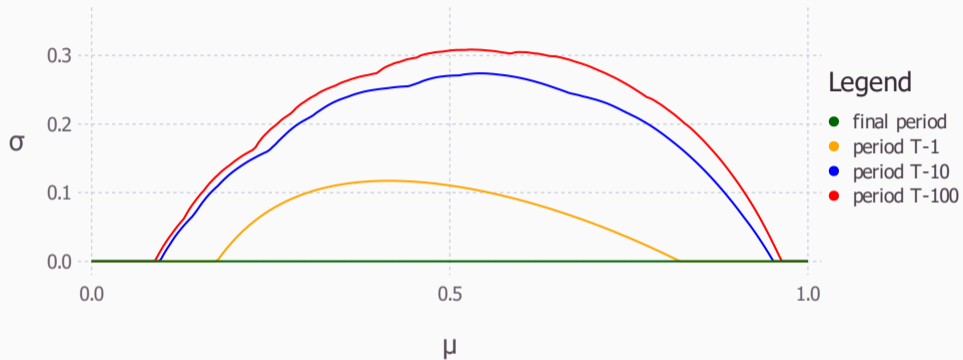
LONG RUN COMMITMENT: FULL COMMITMENT

- Principal commits to long-run contract: $(S_1 \times S_2, p, w)$
 - a signal space $S_1 \times S_2$, p progressively measurable wrt y_t ,
 - and wages w , progressively measurable wrt s_t .
 - Difficult:
 - Agent acquires private info after shirking (effort unobservable to the contract), and
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- ⇒ Characterizing the optimum requires joint design in both periods.

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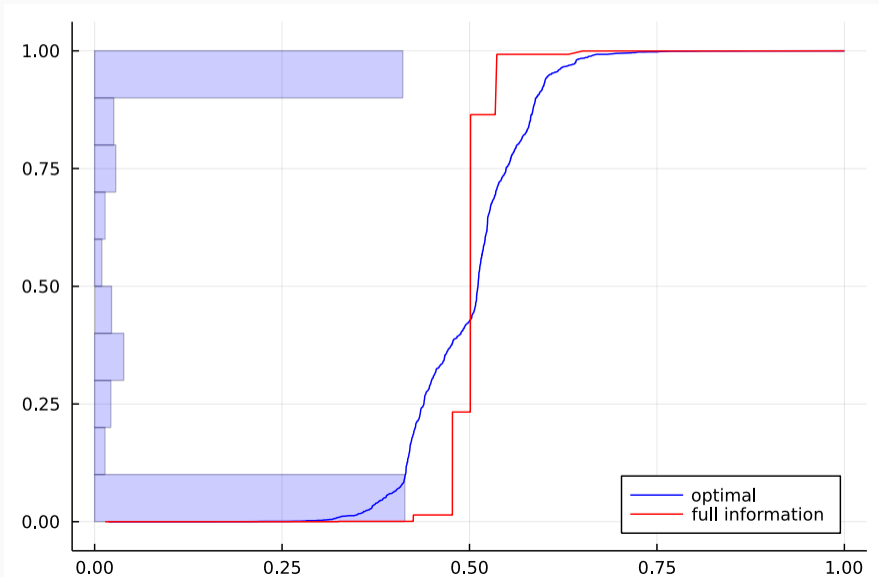
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- ⇒ Characterizing the optimum requires joint design in both periods.
- Optimum is not tractable. Effect is still in place:
 - Consider optimal contract without fully informative evaluation
 - Bonus for high output in period 1 optimally split between both periods
 - Principal can *postpone* information, but it is *costly*

MANY PERIODS



MANY PERIODS

← BACK



Assumption (Bounded changes in curvature)

$$\frac{w'''(u_H)}{w''(u_H)} \geq -\frac{3(b + \mu\Delta b)\Delta b}{c((1-a)\Delta b + b\Delta a)},$$

where $u_H = U + \frac{1-a-\mu\Delta a}{b+\mu\Delta b}c$.