

# Optimal Short-Time Work Policy in Recessions

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## **The Great and Covid-19 recessions renewed interests in key labor econ questions**

1. How do we prevent workers from unemployment?
2. How do we insure workers from income losses?

## **Policy makers in Europe relied on two policy instruments**

1. Unemployment insurance (UI) system
2. Short-time work (STW) system

# What is UI and STW?

**UI** partially replaces income when workers become unemployed

**STW** is a subsidy scheme to combat job losses

1. **Benefits:** Replaces part of worker's wage if hours reduced
2. **Eligibility:** Hours worked fall below a certain level

## **In recessions**

- STW systems became more generous
- UI systems unaltered

## **Natural question to ask**

Why and how should we use STW and UI together?

## **Literature**

- Extensive literature on optimal UI but not on STW
- Interplay between STW and UI conceptually nebulous (Cahuc 2024)
- No theory on how to adjust STW over the business cycle

## **This paper**

- Derives expression for optimal combination of STW and UI in SaM
- Allows STW to adjust optimally over the business cycle

## **Optimal Interplay STW and UI**

- The UI system provides income insurance
- The STW system combats distortions of UI system
  - ⇒ STW allows UI to provide more generous benefits

## **Reaction of STW to a recession**

- STW benefits shall increase (consistent with actual policy)
- Eligibility condition must be tightened (contrasts actual policy)

## **Problem: STW cannot reach social planner solution**

- Cannot influence job-finding rates
- Subsidizes reduction of working hours
  - ⇒ trade-off between employment stabilisation and stabilisation of working hours

# Model

## Canonical search and matching model (DMP) augmented with

1. Risk averse workers
2. Flexible hours choice
3. Endogenous separations (caused by idiosyncratic productivity shocks)
4. Lay-off costs (wasteful)
5. Aggregate productivity shocks (cause the recession)
6. Rigid-salaries (counter-cyclical bargaining power of workers)

## Policy measures

1. Unemployment insurance
2. Short-time work
3. Production tax  
(finances UI and STW system, balanced budget every period)

Additional Model Slides

## Value of firm producing regularly

$$J_t(\epsilon) = y_t(\epsilon, h_t(\epsilon)) - w_t(h_t(\epsilon)) - \tau_{J,t} + E_t \left[ Q_{t,t+1}^f \cdot \mathcal{J}_{t+1} \right]$$

$\epsilon$  : idiosyncratic productivity (i.i.d.)

Production Technology

Formel  $\mathcal{J}_t, \mathcal{V}_t$

**Eligibility condition**  $h_t(\epsilon) < D_t$ , with STW threshold  $h_t(\epsilon_{stw,t}) = D_t$

## Value of firm on STW

$$J_{stw,t}(\epsilon) = y_t(\epsilon, h_{stw,t}(\epsilon)) - \underbrace{w_t(h_{stw,t}(\epsilon))}_{\text{Less working hours, less pay}} - \tau_{J,t} + E_t \left[ Q_{t,t+1}^f \cdot \mathcal{J}_{t+1} \right]$$

**Separations:**  $\epsilon < \epsilon_{s,t}$ , lay-off costs  $F$ , severance payments  $w_{eu,t}$  plus taxes  $\tau_{J,t}$ .



## Job-creation condition (vacancy posting)

$$\underbrace{\frac{k_v}{q_t}}_{\text{Expected Recruitment Costs Worker}} = \underbrace{E_t \left[ Q_{t,t+1}^f \cdot \mathcal{J}_{t+1} \right]}_{\text{Expected Value of a Worker for a Firm}}$$

$\mathcal{J}_t$  : value firm before the idiosyncratic productivity threshold realized

### Value of an employed worker outside STW

$$V_t(\epsilon) = u\left(w_t(h_t(\epsilon)) - v(h_t(\epsilon))\right) + \beta \cdot E_t[\mathcal{V}_{t+1}] \quad \text{with } u'(\cdot) > 0, u''(\cdot) < 0$$

### Value of an employed worker on STW

$$V_{stw,t}(\epsilon) = u\left(\underbrace{w_t(h_{stw,t}(\epsilon))}_{\text{Reduced Income from Firm}} + \underbrace{(\bar{h} - h_{stw,t}(\epsilon)) \cdot \tau_{stw,t}}_{\text{Net Transfer STW}} - v(h_{stw,t}(\epsilon))\right) + \beta \cdot E_t[\mathcal{V}_{t+1}]$$

### Value of an unemployed worker

$$U_t = u(b_t) + \beta \cdot E_t[f_t \cdot \mathcal{V}_{t+1} + (1 - f_t) \cdot U_{t+1}]$$

$b_t$  : UI benefits

$f_t$  : job-finding rate

# Decisions: Nash-Bargaining

## Generalized Nash-Bargaining

Takes place **before** the temporary productivity  $\epsilon$  has been revealed:

$$\max_{w_t(h), w_{eu,t}, h_t(\epsilon), h_{stw,t}(\epsilon), \epsilon_{s,t}} (\mathcal{J}_t)^{1-\eta_{t-1}} \cdot (\mathcal{V}_t - U_t)^{\eta_{t-1}}$$

$\mathcal{V}_t$  : Value of worker for firm before idiosyncratic productivity is realized

$\eta_t$  : Bargaining power of the worker

Formel  $\mathcal{J}_t, \mathcal{V}_t$

## Take Away

Contract contingent on the realization of idiosyncratic productivity shock containing:

- Salary
- Working hours
- Separations

# Outcome Nash-Bargaining

1. Firms fully insure workers income against idiosyncratic productivity shocks

Insurance

2. Working hours on STW are downward distorted

Working Hours

3. STW reduces separations by reducing the salary commitment of firms in bad times

Separations

# Optimal Combination of UI and STW Policy in Steady State

# Optimal UI benefits in steady state

## Optimal UI benefits in steady state

$$\underbrace{(1 - n) \cdot (u'(b) - u'(\tilde{c}^w))}_{\text{Provide Additional Income Insurance}} = \underbrace{(LV + LS)}_{\text{Additional Distortions UI}} \cdot \beta \cdot \left( -\frac{\partial J}{\partial b} \right)$$

**LV:** Additional welfare loss via fewer vacancy postings

**LS:** Additional welfare loss via more separations

## Take away

- UI provides insurance against income losses
- No full insurance  $u'(\tilde{c}) \neq u'(b) \rightarrow$  trade-off insurance against distortions
- UI benefits decrease vacancy postings and increase separations
- STW cannot combat social costs from reduced vacancies **LV**
- STW can reduce social costs from more separation **LS**

# Optimal STW benefits in steady state

## Optimal STW benefits in steady state

$$(\bar{h} - h_{stw}(\epsilon_s)) \cdot \tau_{stw} = \underbrace{\frac{\beta \cdot (1 - f)}{1 - \beta \cdot (1 - G(\epsilon_s)) \cdot (1 - f)} \cdot \left[ b + \frac{1 - n}{n} \cdot b \right]}_{\text{Fiscal Externality UI System} > 0}$$

$$- \underbrace{\frac{1}{g(\epsilon_s)} \cdot \left[ \frac{\partial \Omega}{\partial \tau_{stw}} \right] \cdot \left[ -\frac{1}{\frac{\partial \epsilon_s}{\partial \tau_{stw}}} \right]}_{\text{Additional Welfare Costs of larger STW benefits} > 0} - \underbrace{\tilde{BE}}_{\text{Bargaining Effect}}$$

## Take away

- STW reacts on the fiscal externality of UI system → less inefficient separations
- STW does not stimulate vacancy postings
- STW does not provide income insurance on the firm

Extended Formula

Welfare Cost Penalty

# Optimal STW benefits in steady state

## Optimal STW benefits in steady state

$$(\bar{h} - h_{stw}(\epsilon_s)) \cdot \tau_{stw} = \underbrace{\frac{\beta \cdot (1 - f)}{1 - \beta \cdot (1 - G(\epsilon_s)) \cdot (1 - f)} \cdot \left[ b + \frac{1 - n}{n} \cdot b \right]}_{\text{Fiscal Externality UI System} > 0} - \underbrace{\frac{1}{g(\epsilon_s)} \cdot \left[ \frac{\partial \Omega}{\partial \tau_{stw}} \right] \cdot \left[ -\frac{1}{\frac{\partial \epsilon_s}{\partial \tau_{stw}}} \right]}_{\text{Additional Welfare Costs of larger STW benefits} > 0} - \underbrace{\tilde{BE}}_{\text{Bargaining Effect}}$$

## Take away

- Search costs important via job-finding rate  $f$
- Important influence on optimal STW benefits!

Extended Formula

Welfare Cost Penalty



**Optimal STW benefits increase when job-finding rates fall**

$$-\frac{\partial \tau_{stw}}{\partial f} > 0$$

## **Intuition**

Smaller job-finding rate → workers stay unemployed for longer  
→ social costs of separations increase  
(workers receive UI benefits for longer)  
→ larger STW benefits

# Optimal STW Benefits in Steady State

## Optimal STW benefits in steady state

$$\begin{aligned}
 (\bar{h} - h_{stw,t}(\epsilon_{s,t})) \cdot \tau_{stw} &= \underbrace{\frac{\beta \cdot (1-f)}{1 - \beta \cdot (1 - G(\epsilon_s)) \cdot (1-f)} \cdot \left[ b + \frac{1-n}{n} \cdot b \right]}_{\text{Fiscal Externality UI} > 0} \\
 &- \underbrace{\frac{1}{g(\epsilon_s)} \cdot \left[ \frac{\partial \Omega}{\partial \tau_{stw}} \right] \cdot \left[ -\frac{1}{\frac{\partial \epsilon_s}{\partial \tau_{stw}}} \right]}_{\text{Additional Welfare Costs of larger STW benefits} > 0} - \underbrace{\tilde{BE}}_{\text{Bargaining Effect}}
 \end{aligned}$$

## Take away

- Ramsey planner faces trade-off:

reduction of inefficient separations    vs.    inefficient reduction in working hours.

- Ramsey planner prevents not all inefficient separations → smaller STW benefits

## Optimal eligibility condition on separation threshold without STW

$$y(h_{stw}^{-1}(D), D) - v(D) + \frac{k_v}{q} + (1 - f) \cdot \beta \cdot \frac{\mathcal{V} - U}{u'(\tilde{c}^w)} = 0$$

## Why this eligibility condition?

- *Looser eligibility condition*: Hours distortions spread, no matches rescued → not optimal!
- *Tighter eligibility condition*: Lose most productive matches on STW → not optimal!

## Take away

- Eligibility condition restricts number of firms on STW  
→ keeps distortionary effects of STW low

# Optimal Eligibility Condition in Steady State

## Optimal eligibility condition on separation threshold without STW

$$y(h_{stw}^{-1}(D), D) - v(D) + \frac{k_v}{q} + (1 - f) \cdot \beta \cdot \frac{\mathcal{V} - U}{u'(\tilde{c}^w)} = 0$$

### Take away

- Also job-finding rate crucial determinant of eligibility condition!

**Optimal eligibility condition falls if the job-finding rate falls**

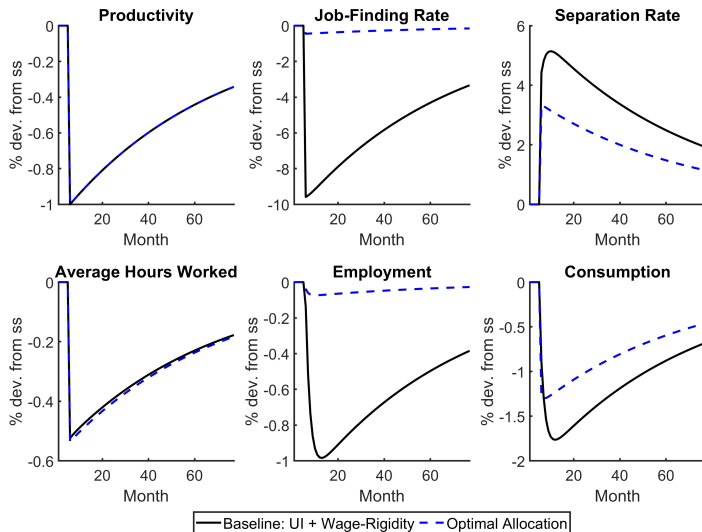
$$-\frac{\partial D}{\partial f} < 0$$

## **Intuition**

- Smaller job-finding rate → harder for workers to find a new job
- workers accept cut in working hours and thus salary
- matches can survive on lower working hours without STW
- stricter eligibility to keep hours distortions low

# Optimal STW Policy, Applied to a Recession

# Distortionary Effects of UI grow in Recessions.

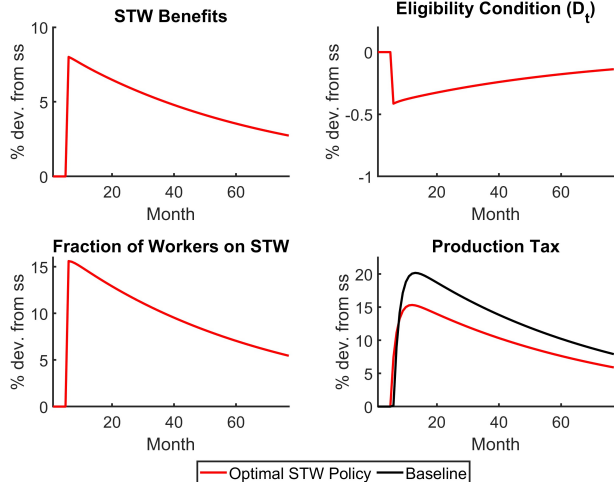


Negative productivity shock  
+ wage-rigidity

- fall in job-finding rate
- UI distortions grow
- inefficient separations
- Deviation from Planner

Compared to Data

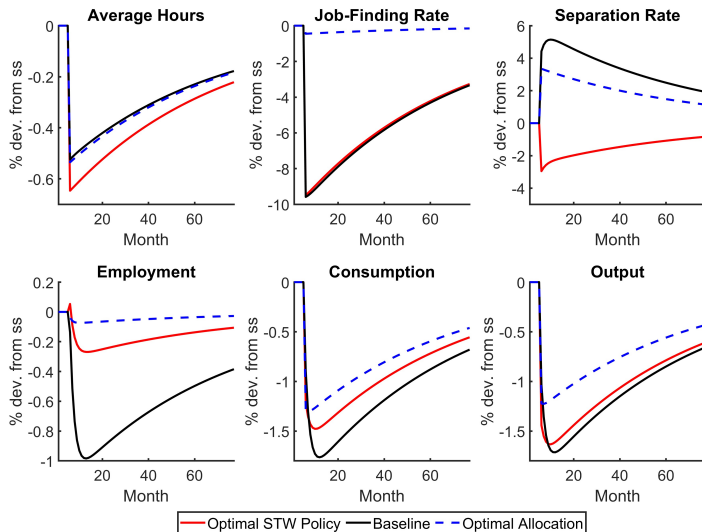
# Optimal STW Benefits grow, Eligibility falls in Recessions



- STW benefits react to more distortions of UI
- Firms and workers choose lower working hours: thus, more eligible for STW
- STW system keeps self financing



# Optimal STW Policy stabilizes the Business Cycle



Policy:

1. Job-finding rate cannot be stabilized
2. Separation rate oversteers

Allocation:

- + Consumption and employment stabilized
- STW distorts hours and reduces stabilization consumption

Fixed STW System

Influence Hours Distortion





# Conclusion

- 1. STW is a complement, not a substitute to the UI system**
  - STW internalizes fiscal externality of UI System
  - STW reduces fiscal costs
- 2. Search frictions matter: variation in job-finding rate require STW to adjust**
  - Optimal STW benefits increase in recessions
  - Optimal eligibility condition must be tightened in recessions
- 3. STW cannot reach the social planner solution**
  - Destabilizes working hours
  - Cannot stabilize job-finding rate

# Thank you for your Attention!

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# Literature I

-  Balleer, Almut et al. (2016). "Does short-time work save jobs? A business cycle analysis". In: *European Economic Review* 84.C, pp. 99–122. DOI: 10.1016/j.euroecorev.2015. URL: <https://ideas.repec.org/a/eee/eecrev/v84y2016icp99-122.html>.
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## Literature II

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-  Jung, Philip and Keith Kuester (2015). “Optimal Labor-Market Policy in Recessions”. In: *American Economic Journal: Macroeconomics* 7.2, pp. 124–56. DOI: 10.1257/mac.20130028. URL: <https://www.aeaweb.org/articles?id=10.1257/mac.20130028>.
-  Shimer, Robert (2005). “The Cyclical Behavior of Equilibrium Unemployment and Vacancies”. In: *American Economic Review* 95.1, pp. 25–49. URL: <https://ideas.repec.org/a/aea/aecrev/v95y2005i1p25-49.html>.

# Appendix

# Literature



- Braun and Brügemann (2017)
  - Looks at combination of UI and STW in implicit contract model
  - This paper: generalization to SaM allows to derive optimal policy over business cycle
- Balleer et al. (2016), Cooper, Meyer, and Schott (2017)
  - STW in a SaM, business cycle, inflexible hours, STW as flexibilization tool
  - This paper: flexible hours, STW as a state-contingent wage-subsidy, optimal policy.
- Cahuc, Kramarz, and Nevoux (2021)
  - Partial equilibrium model, emphasizes empirical relevance of distortion of working hours
  - This paper: similar modeling of STW, STW as subsidy that increases joint surplus

# Appendix: Model

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# Labor Market Flows

- Unit mass of workers:
  - Employed  $n_t$  or unemployed  $u_t$
  - If employed: either on or off STW
- Law of motion of employment:

$$n_t = (1 - G(\epsilon_{s,t-1})) \cdot n_{t-1} + m_{t-1}$$

$G(\epsilon_{s,t})$  : Endogenous separation rate

- Matching function:

$$m_t = \chi \cdot v_t^{1-\gamma} \cdot (1 - n_t + G(\epsilon_{s,t}) \cdot n_t)^\gamma$$

$v_t$  : vacancies

- Job-finding, job-filling rates and labor market tightness:

$$f_t = \chi \cdot (\theta_t)^{1-\gamma}, \quad q_t = \chi \cdot (\theta_t)^{-\gamma}, \quad \theta_t = \frac{v_t}{1 - n_t + G(\epsilon_{s,t}) \cdot n_t}$$

# Production Technology

- Production function:

$$y_t(\epsilon, h_t(\epsilon)) = \underbrace{a_t \cdot \epsilon}_{\text{Firm Specific Productivity}} \cdot \underbrace{h_t(\epsilon)^\alpha}_{\text{Hours Worked}} - \underbrace{(\mu_\epsilon - \epsilon) \cdot c_f}_{\text{Resource Cost Shock}}$$

- Idiosyncratic productivity shock  $\epsilon$  is i.i.d. and follows a log-normal distribution:

$$\epsilon_j \sim \mathcal{LN}(\mu, \sigma^2) \text{ with } \mu_\epsilon = E[\epsilon_j] = \exp\left(\mu + \frac{1}{2} \cdot \sigma^2\right)$$

- Aggregate productivity shock follows AR(1)-process

$$a_t = \mu_a + \rho_a \cdot (a_{t-1} - \mu_a) + \zeta_t, \quad \rho_a \in [0, 1), \quad \zeta_t \sim \mathcal{N}(0, \sigma_a^2)$$

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Costain-Reiter Puzzle

**Profits are redistributed towards firm owners**

$$V_t^F = \tilde{u}(\Pi_t/\nu_t) + \beta \cdot E_t \left[ V_{t+1}^F \right]$$

$\nu_t$  : number of firm owners

## Expected Value of Firm and Worker at Nash-Bargaining

- The STW threshold  $\epsilon_{stw,t}$  is implicitly defined by:  $h_t(\epsilon_{stw,t}) = D_t$
- Expected value of a worker for a firm at Nash-Bargaining:

$$\mathcal{J}_t = \int_{\epsilon_{stw,t}}^{\infty} J_t(\epsilon) dG(\epsilon) + \int_{\epsilon_{s,t}}^{\epsilon_{stw,t}} J_{stw,t}(\epsilon) dG(\epsilon) - G(\epsilon_{s,t}) \cdot (w_{eu,t} + \tau_{J,t} + F)$$

- Expected value of a worker at Nash-Bargaining can be defined by:

$$\mathcal{V}_t = \int_{\epsilon_{stw,t}}^{\infty} V_t(\epsilon) dG(\epsilon) + \int_{\epsilon_{s,t}}^{\epsilon_{stw,t}} V_{stw,t}(\epsilon) dG(\epsilon) + G(\epsilon_{s,t}) \cdot (u(w_t) - u(b_t) + U_t)$$

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## **Introduction of rigid salaries:**

Following Jung and Kuester (2015), the bargaining power of workers increases in recessions:

$$\eta_t = \exp(-\gamma_w \cdot a_t), \quad \gamma_w > 0$$

## **Motivation:**

Rigid salaries solve the Shimer Puzzle (see Shimer (2005))

# Government Budget Constraint

## Government Budget Constraint:

Government finances period expenditure by same period income from taxes (no financial markets).

$$\underbrace{n_t \cdot \tau_{J,t}}_{\text{Tax Income}} = \underbrace{(1 - n_t) \cdot b_t}_{\text{Fiscal Costs UI System}} + \underbrace{n_t \cdot \int_{\epsilon_{s,t}}^{\epsilon_{stw,t}} (\bar{h} - h_{stw,t}(\epsilon)) \cdot \tau_{stw,t} dG(\epsilon)}_{\text{Fiscal Costs STW System}}$$

## Implication:

UI system gets more expensive in recessions as more workers use the system. This increases the tax the government has to charge.



# Appendix

# Details Theory

**Firms insure workers against idiosyncratic productivity shocks:**

$$\underbrace{c_t(\epsilon) - v(h_t(\epsilon))}_{\tilde{c}_t} = \underbrace{c_{stw,t}(\epsilon) - v(h_{stw,t}(\epsilon))}_{\tilde{c}_{stw,t}} = c_{eu,t}$$

⇒ Same period utility in and outside STW and from severance payments

⇒ Firms stock-up income on STW

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## Hours worked outside STW:

Outside STW, working hours are set optimally (like in competitive equilibrium)

$$\underbrace{\frac{\partial y(\epsilon, h_t(\epsilon))}{\partial h}}_{\text{Marginal Product of Labor}} = \underbrace{v'(h_t(\epsilon))}_{\text{Marginal Disutility of Labor}}$$

[Graph](#)

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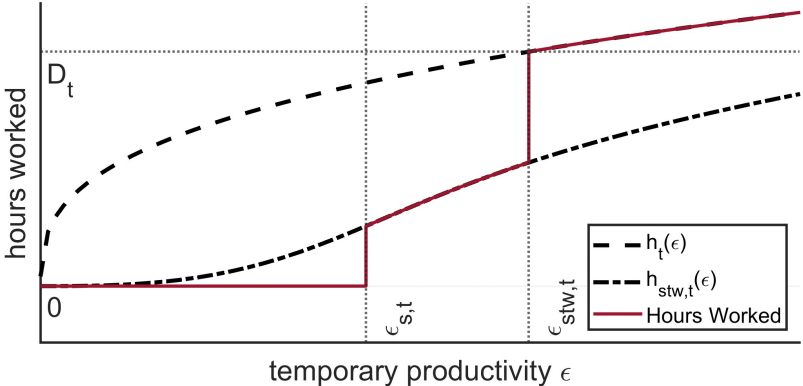
## Hours worked on STW:

Are distorted downwards by STW compensation (distortion of working hours)

$$\underbrace{\frac{\partial y(\epsilon, h_{stw,t}(\epsilon))}{\partial h}}_{\text{Marginal Product of Labor}} = \underbrace{v'(h_{stw,t}(\epsilon))}_{\text{Marginal Disutility of Labor}} + \underbrace{T_{stw,t}}_{\text{STW Benefits}}$$

[Graph](#)

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## Separation Threshold is determined by:

$$y_t(\epsilon_{s,t}, h_{stw,t}(\epsilon_{s,t})) + (\bar{h} - h_{stw}(\epsilon_{s,t})) \cdot \tau_{stw,t} + \frac{k_v}{q_t} + (1 - f_t) \cdot \frac{\beta \cdot E_t [\mathcal{V}_{t+1} - U_{t+1}]}{u'(\tilde{c}_t)} = 0$$

## Intuition:

1. Employed worker's income is insured by firm  $\rightarrow$  don't want to quit
2. STW reduces the costs of salary-commitment in bad times  $\rightarrow$  less likely to fire workers
3. Higher benefits  $\rightarrow$  salaries paid by firms reduced  $\rightarrow$  less separations

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# Ramsey Problem

Planner chooses STW benefits  $\tau_{stw,t}$ , eligibility condition  $D_t$  and UI benefits  $b_t$ .

$$W_t^G = \max_{D_t, \tau_{stw,t}, b_t} (1 - n_t) \cdot u(b_t) + n_t \cdot u(\tilde{c}_t^w) \\ + \nu_t \cdot \tilde{u} \left( \underbrace{\left[ \int_{\epsilon_{s,t}}^{\infty} y_t(\epsilon) - v(h_t(\epsilon)) dG(\epsilon) - n_t \cdot \Omega_t - \tilde{c}_t^w - (1 - n_t) \cdot b_t - v_t \cdot k_v - \rho_t \cdot n_t \cdot F \right]}_{\text{Utility of Firm Owners w/o hours distortion}} / \nu_t \right) \\ + \beta \cdot E_t W_{t+1}^G$$

**subject to**

Labor Market Equilibrium

Additional Assumption: number of firm owners  $\nu_t$  are set so  $\tilde{c}_t^w = c_t^f$

$\Rightarrow$  no distributional conflicts between firm owners and workers!

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## Optimal UI benefits in steady state

$$(1 - n) \cdot (u'(b) - u'(\tilde{c}^w)) = (LV + LS) \cdot \frac{u'(\tilde{c}^w)}{1 - \eta} \left( -\frac{\partial J}{\partial b} \right)$$

Welfare loss fewer vacancy postings (LV) and more separations (LS):

$$LV = \frac{1}{M} \cdot \underbrace{\frac{\eta - \gamma}{(1 - \gamma) \cdot (1 - \eta)}}_{\text{Deviation Hosios Condition}} + \frac{1}{M} \cdot \underbrace{\frac{b + \frac{1-n}{n} \cdot b}{1 - \beta \cdot (1 - f) \cdot (1 - G(\epsilon_s))}}_{\text{Fiscal Externality UI System}} \cdot \frac{k_v}{q}$$

$$LS = \frac{1}{M} \cdot \frac{n \cdot (\gamma - f \cdot \eta)}{(1 - \gamma) \cdot (1 - \eta) \cdot m} \cdot \left( \underbrace{\frac{\beta \cdot (1 - f) \cdot (b + \frac{1-n}{n} \cdot b)}{1 - \beta \cdot (1 - f) \cdot (1 - G(\epsilon_s))}}_{\text{Fiscal Externality UI System}} - \underbrace{\tau_{stw,t} \cdot (\bar{h} - h_{stw,t}(\epsilon_s))}_{\text{STW Subsidy}} \right)$$

### Take away:

- STW cannot eliminate low vacancy postings
- STW can eliminate all inefficient separations → allows for more generous UI benefits



# Optimal UI benefits in steady state - with optimal STW system

## Optimal UI benefits in steady state

$$(1 - n) \cdot (u'(b) - u'(\tilde{c}^w)) = (LV + LS) \cdot \frac{u'(\tilde{c}^w)}{1 - \eta} \left( -\frac{\partial J}{\partial b} \right)$$

Welfare costs vacancy posting and separations (given STW):

$$LV = \frac{1}{M'} \cdot \underbrace{\frac{\eta - \gamma}{1 - \eta}}_{\text{Deviation Hosios Condition}} + \frac{1}{M'} \cdot \frac{b + \frac{1-n}{n} \cdot b}{1 - \beta \cdot (1 - f) \cdot (1 - G(\epsilon_s))} / \frac{k_v}{q}$$
$$LS + LSTW = \frac{1}{M'} \cdot \frac{n \cdot (\gamma - f \cdot \eta)}{(1 - \gamma) \cdot (1 - \eta) \cdot m} \cdot \underbrace{\left( \frac{\partial \Omega}{\partial \tau_{stw}} / (\bar{h} - h_{stw}(\epsilon_s)) + \frac{\partial \Omega}{\partial \epsilon_{stw}} / \frac{\partial y(\epsilon_{stw}, h)}{\partial \epsilon_{stw}} \right)}_{\text{STW cannot combat all inefficient separations due to hours distortions}}$$

## Take away:

- Planner decides against eliminating all inefficient separations due to hours distortions!
- Trade-off: Stabilizing employment vs. stabilizing working hours

## Bargaining Effect:

$$\tilde{B}E = \frac{\frac{BE \cdot (LS + LV + LSTW)}{n \cdot u'(\tilde{c}^w)}}{1 + \frac{\beta \cdot (1 + \eta \cdot BE) \cdot (LS + LV + LSTW)}{n \cdot u'(\tilde{c}^w)}} \cdot \frac{1 - f(\theta)}{1 - \eta} \cdot \frac{k_v}{q(\theta)}$$

$$\text{with } BE = \frac{\left(-\frac{u''(\tilde{c}^w)}{u'(\tilde{c}^w)}\right) \cdot \frac{u(\tilde{c}^w) - u(b)}{u'(\tilde{c}^w)}}{1 + (1 - \eta) \cdot \left(-\frac{u''(\tilde{c}^w)}{u'(\tilde{c}^w)}\right) \cdot \frac{u(\tilde{c}^w) - u(b)}{u'(\tilde{c}^w)}}$$

Sending workers on STW is costly for the firm

- salary reduction needed, but: MU of workers go up
- more difficult to reduce wages
- less vacancies, more separations!

## Optimal STW benefits in steady state

$$(\bar{h} - h_{stw}(\epsilon_s)) \cdot \tau_{stw} = \underbrace{\frac{\beta \cdot (1 - f)}{1 - \beta \cdot (1 - G(\epsilon_s)) \cdot (1 - f)}}_{\text{Fiscal Externality UI} > 0} \cdot \left[ b + \frac{1 - n}{n} \cdot b \right]$$

$$- \underbrace{\frac{1}{g(\epsilon_s)} \cdot \left[ \frac{\partial \Omega}{\partial \tau_{stw}} \right] \cdot \left[ -\frac{1}{\frac{\partial \epsilon_s}{\partial \tau_{stw}}} \right]}_{\text{Additional Welfare Costs of larger STW Benefits} > 0} - \underbrace{\tilde{BE}}_{\text{Bargaining Effect}}$$

What is the welfare cost penalty?

## Welfare costs of STW due to distortion of working hours

$$\Omega_t = \int_{\epsilon_{s,t}}^{\epsilon_{stw,t}} \left[ \underbrace{y_t(\epsilon) - v(h_t(\epsilon))}_{\text{No Hours Distortion}} - \underbrace{y_{stw,t}(\epsilon) + v(h_{stw,t}(\epsilon))}_{\text{With Hours Distortion}} \right] dG(\epsilon) \geq 0$$

Difference between output minus disutility from work with and without hours distortion

## Eligibility and STW benefits influence welfare costs of STW

$$\underbrace{\frac{\partial \Omega_t}{\partial \tau_{stw,t}}}_{\text{More STW benefits}} > 0, \quad \underbrace{\frac{\partial \Omega_t}{\partial D_t}}_{\text{Looser Eligibility}} > 0, \quad \underbrace{\frac{\partial^2 \Omega_t}{\partial D_t \partial \tau_{stw,t}}}_{\text{both}} > 0$$

### Intuition:

1. Larger STW benefits  $\rightarrow$  larger incentive to reduce hours  $\rightarrow$  larger hours distortion
2. Looser eligibility  $\rightarrow$  more workers on STW  $\rightarrow$  larger hours distortion
3. Looser eligibility + larger benefits  $\rightarrow$  even larger hours distortion

# Appendix: Calibration

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Table 1: Business Cycle Properties US Data

	$v$	$f$	$\rho$	$u$	$\theta$	$\bar{h}$	$p$	
Standard Deviation	20.13	14.31	8.2	20.49	39.67	0.81	1.91	
Autocorrelation	0.95	0.95	0.77	0.95	0.96	0.92	0.9	
Correlation	$v$	1	0.85	-0.55	-0.92	0.98	0.55	0.19
	$f$	-	1	-0.29	-0.93	0.91	0.38	0.09
	$\rho$	-	-	1	0.6	-0.59	-0.63	-0.4
	$u$	-	-	-	1	-0.98	-0.55	-0.23
	$\theta$	-	-	-	-	1	0.57	0.22
	$\bar{h}$	-	-	-	-	-	1	0.46
	$p$	-	-	-	-	-	-	1

Notes: The table lists the second moments of the US data.  $u$ ,  $v$ ,  $f$ ,  $\bar{h}$ , and  $G(\epsilon_s)$  are expressed as quarterly averages of monthly series.  $p$  is the seasonally adjusted average labor productivity in the non-farm business sector. All variables are reported as log-deviations from a HP trend with smoothing parameter  $10^5$ .

Table 2: Business Cycle Properties Baseline Model

	$v$	$f$	$\rho$	$u$	$\theta$	$\bar{h}$	$p$	
Standard Deviation	19.8	14.31	8.2	21.26	40.88	0.76	1.91	
Autocorrelation	0.95	0.97	0.97	0.98	0.97	0.97	0.97	
Correlation	$v$	1	1	-0.99	-0.98	1	1	1
	$f$	-	1	-1	-1	1	1	1
	$\rho$	-	-	1	1	-1	-1	-1
	$u$	-	-	-	1	-1	-1	-1
	$\theta$	-	-	-	-	1	1	1
	$\bar{h}$	-	-	-	-	-	1	1
	$p$	-	-	-	-	-	-	1

Notes: The table reports the second moments of the model. As in the data, all variables are quarterly averages of monthly series and reported as log-deviations.  $p$  denotes the average output per person, that is  $p = E[y_t(\epsilon)|\epsilon \geq \epsilon_{s,t}]$ .



## Costain and Reiter (2008) - Puzzle

### **Costain and Reiter (2008)-Puzzle:**

SaM cannot simultaneously produce realistic business cycle fluctuations and a realistic elasticity of unemployment

### **Workaround:**

wage-rigidity ( $\gamma_w$  calibrated to match s.d. job-finding rate) + large surplus calibration

### **Problem:**

Large continuation value implies no separation incentives with idiosyncratic shocks

**Workaround:** idiosyncratic resource cost shock,  $c_f$  calibrated to match separation rate

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**Data** - Elasticity of unemployment with respect to UI benefits: 2-3

**Model** - Elasticity of unemployment with respect to UI benefits: 2,73

Table 2: Parameters

Parameter	Description	Value	Reason
$\rho$	Target ss separation rate	0.03	Data
$f$	Target ss job-finding rate	0.41	Data
$q$	Target ss vacancy filling rate	0.338	Haan, Ramey, and Watson (2000)
$\beta$	Discount rate	0.996	Jung and Kuester (2015)
$\psi$	Inverse Frisch-elasticity	1.5	Domeij and Floden (2006)
$\gamma$	Elasticity matching function with respect to unemployment	0.65	Shimer (2005).
$\eta$	Bargaining power worker	0.65	Implements Hosios-Condition
$\gamma_w$	Coefficient reaction bargaining power to productivity shock	15.5	s.d. job-finding rate 14.31 in data
$F$	Separation costs	1.01	s.d. separation rate of 8.2 in data
$b$	UI benefits	0.4	40% replacement rate of wage
$\alpha$	Labor elasticity production function	0.65	Christoffel and Linzert (2010)
$\bar{h}$	"Normal" hours worked	0.834	Mean hours worked in baseline
$\rho_a$	Autocorr. productivity shock	0.985	Jung and Kuester (2015)
$\mu_a$	Mean aggregate productivity	1.0	Normalization
$\sigma_a \cdot 100$	s.d. aggregate productivity	0.259	s.d. labor prod. of 1.91 in data
$\mu$	Parameter steering mean of lognormal distribution	0.082	Normalize wage to 1
$\sigma$	Parameter steering variance of lognormal distribution	0.12	Krause and Lubik (2007)
$\chi$	Matching parameter	0.383	Calculated by target ss
$k_v$	Vacancy posting costs	0.139	Calculated by target ss
$c_f$	Strength resource cost shock	10.441	Calculated by target ss

# Fixed STW system

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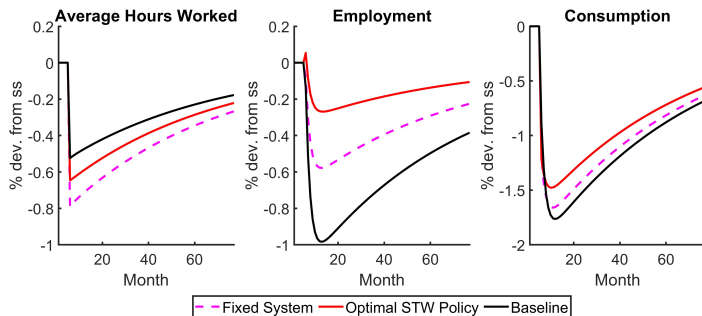
### **How important is it to adjust STW over the business cycle?**

Balleer et al. (2016) argue that STW acts as an automatic stabilizer

#### **Assumptions:**

1. STW is set optimally in steady state
2. STW is not adjusted over the business cycle

# Fixed STW system



Observation:

- Stabilizes employment but not consumption!
- No automatic stabilization!
- Contrasts: Balleer et al. (2016)

Reason:

- Eligibility condition not adjusted
- More firms on STW
- Average hours fall
- Outweighs employment effect

**Appendix:**

# **Optimal STW Policy with and without Moral Hazard**

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# What influences optimal STW benefits?

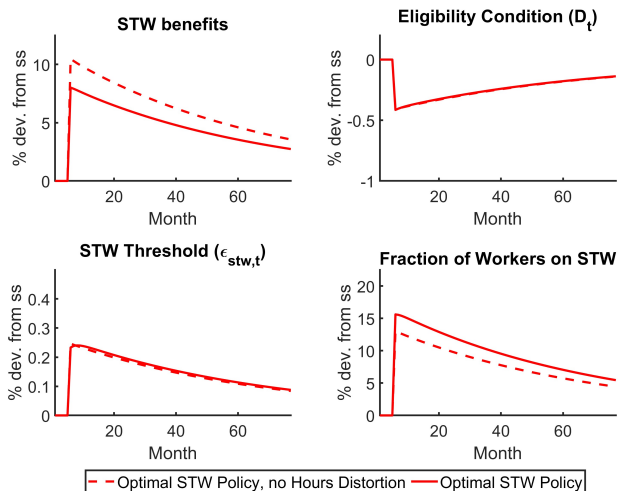
**Optimal STW benefits decrease in number of workers on STW:**

$$\frac{\partial (\bar{h} - h_{stw}(\epsilon_s)) \tau_{stw}}{\partial \epsilon_{stw}} = - \frac{\partial^2 \Omega}{\partial \tau_{stw} \partial \epsilon_{stw}} \cdot \left[ - \frac{1}{\frac{\partial \epsilon_s}{\partial \tau_{stw}}} + \frac{\partial \tau_{stw}}{\partial n} \right] - \frac{\partial \Omega}{\partial \tau_{stw}} \cdot \left[ \frac{1}{\frac{\partial \epsilon_s}{\partial \tau_{stw} \partial \epsilon_{stw}}} \right] < 0$$

**Intuition:**

- Looser eligibility → larger benefits reach more firms
- larger hours distortion
- choose smaller benefits to reduce distortion
- Less effective combating inefficient job losses

# Moral Hazard of STW reduces Ability to stabilize Business Cycles

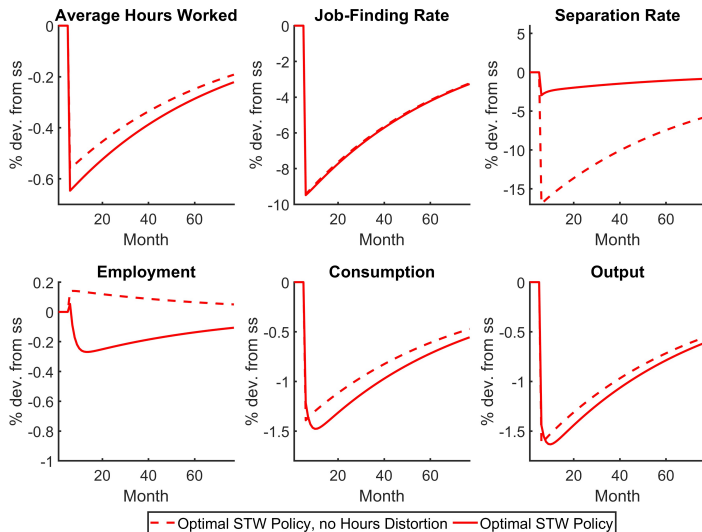


More workers on STW

- More distortion working hours
- Smaller STW benefits



# Moral Hazard of STW reduces Ability to stabilize Business Cycles



Distortions of STW grows since more firms are on STW

Implication:

- Set smaller Net-Subsidy
- Separation rate cannot be oversteered to the optimal level
- Consumption and employment less well stabilized

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