

# The Anatomy of Machine Learning-Based Portfolio Performance

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# The Anatomy of Machine Learning-Based Portfolio Performance

## Abstract

The relevance of asset return predictability is routinely assessed by the economic value that it produces in asset allocation exercises. Specifically, out-of-sample return forecasts are generated based on a set of predictors, increasingly via “black box” machine learning models. The return forecasts then serve as inputs for constructing a portfolio, and portfolio performance metrics are computed over the forecast evaluation period. To shed light on the sources of the economic value generated by return predictability in fitted machine learning models, we develop a methodology based on Shapley values—the *Shapley-based portfolio performance contribution* (SPPC)—to directly estimate the contributions of individual or groups of predictors to portfolio performance. We illustrate the use of the SPPC in an empirical application measuring the economic value of cross-sectional stock return predictability based on a large number of firm characteristics and machine learning.

*JEL classifications:* C53, C55, C58, G11, G17

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# 1. Introduction

Asset return predictability is a leading topic in empirical asset pricing. Out-of-sample tests are now routinely employed, as they are viewed as the most rigorous and informative tests of return predictability, particularly in the era of “big data” and machine learning (e.g., Nagel 2021; Martin and Nagel 2022). In terms of analyzing out-of-sample return predictability, in addition to assessing the statistical accuracy of return forecasts,<sup>1</sup> it is now routine to analyze the economic value of return predictability via asset allocation exercises. Specifically, return forecasts based on a set of predictors serve as inputs for constructing a portfolio. Portfolio performance metrics are then computed over a forecast evaluation period (and perhaps compared to those for a benchmark portfolio) to measure the economic value of return predictability from an investment perspective.

Recently, a spate of studies employs a multitude of firm characteristics and machine learning methods to generate cross-sectional out-of-sample stock return forecasts (e.g., Freyberger, Neuhierl, and Weber 2020; Gu, Kelly, and Xiu 2020; Avramov, Cheng, and Metzker 2023; Han et al. 2023). They construct long-short portfolios by sorting stocks according to their return forecasts for the next month and going long (short) stocks with the highest (lowest) return forecasts. Similarly to studies of aggregate market return predictability,<sup>2</sup> these studies find that long-short portfolios based on machine learning forecasts provide substantive economic value to investors, thereby furnishing strong evidence of cross-sectional stock return predictability.

While there is growing evidence of the importance of stock return predictability in terms of economic value, the existing literature does not provide a general methodology for mea-

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<sup>1</sup>For example, in the context of aggregate equity market return predictability, the popular out-of-sample  $R^2$  statistic (Fama and French 1989; Campbell and Thompson 2008) measures the proportional reduction in mean squared error for a competing forecast based on the information in a set of predictors vis-à-vis a naïve benchmark forecast that ignores the information. Han et al. (2023) develop a modified out-of-sample  $R^2$  statistic for analyzing cross-sectional stock return forecasts.

<sup>2</sup>See Rapach and Zhou (2022) for a review of the literature on aggregate equity market return predictability, including its economic value.

asuring how individual predictors in fitted machine learning models contribute to economic value. In the present paper, we fill this gap in the literature by developing a methodology based on Shapley (1953) values to directly estimate the contributions of individual or groups of predictors to portfolio performance. This allows us to decompose portfolio performance in terms of the underlying predictors—in essence, we “anatomize” economic value as reflected by portfolio performance. Based on the logic of Shapley values, our methodology provides a framework for fairly allocating the contributions of predictors in fitted prediction models with respect to portfolio performance. We call our new measure the *Shapley-based portfolio performance contribution*, which we denote for predictor  $p$  by  $\text{SPPC}_p$ .

Our portfolio performance decomposition based on  $\text{SPPC}_p$  can be viewed as a machine learning model interpretation tool. With the growing popularity of machine learning models, many of which are “black boxes,” numerous model interpretation devices have been developed, including variable importance metrics and measures of interactions and nonlinearities (e.g., Dimopoulos, Bourret, and Lek 1995; Friedman 2001; Štrumbelj and Kononenko 2010, 2014; Goldstein et al. 2015; Ribeiro, Singh, and Guestrin 2016; Lundberg and Lee 2017; Greenwell, Boehmke, and McCarthy 2018; Fisher, Rudin, and Dominici 2019; Apley and Zhu 2020).<sup>3</sup> Existing model interpretation tools are primarily designed to analyze fitted prediction models based on training sample data. While conventional model interpretation tools are informative for investigating the relevance of predictors in fitted models, in the context of analyzing the economic value of return predictability, they do not directly measure how predictors influence portfolio performance per se, which is the ultimate object of interest, and they do not provide an exact decomposition of portfolio performance in terms of the predictors. Our new  $\text{SPPC}_p$  does these things, thereby providing a model interpretation tool for deepening our understanding of the roles of individual or groups of predictors in fitted machine learning models when it comes to the economic value of return predictability.<sup>4</sup>

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<sup>3</sup>See Molnar (2022) for an informative textbook treatment of machine learning model interpretation tools.

<sup>4</sup>Moehle, Boyd, and Ang (2021) propose tools, some of which are based on Shapley values, that are designed to attribute portfolio performance to “features” such as rebalancing frequency, leverage limits, and ESG constraints. Our  $\text{SPPC}_p$  is very different, as it measures the contributions of the predictors in fitted

In presenting the  $\text{SPPC}_p$ , we begin by reviewing the use of Shapley values for interpreting fitted prediction models, as developed by Štrumbelj and Kononenko (2010, 2014) and Lundberg and Lee (2017). To fix ideas, we focus on a setting where we forecast individual stock returns based on firm characteristics using a pooled prediction model, as in, among others, Freyberger, Neuhierl, and Weber (2020), Gu, Kelly, and Xiu (2020), and Avramov, Cheng, and Metzker (2023). While we focus on this setting, the  $\text{SPPC}_p$  can be computed for any situation where we use a fitted prediction model (or ensemble of models) to forecast asset returns, with the return forecasts serving as inputs for constructing a portfolio.

We explain how we extend conventional Shapley values to estimate the contributions of predictors to (1) an out-of-sample return forecast, (2) a portfolio return, and (3) a portfolio performance metric, resulting in the  $\text{SPPC}_p$ . We emphasize that the  $\text{SPPC}_p$  is very flexible: it is model agnostic (i.e., it applies to any prediction model, including all types of machine learning models), can be used for any strategy for mapping the return forecasts to portfolio weights, and can be computed for any portfolio performance metric.<sup>5</sup> The  $\text{SPPC}_p$  is estimated via a sampling-based algorithm, and we discuss computational issues in detail.

We illustrate the use of our new  $\text{SPPC}_p$  measure in an extensive empirical application investigating the economic value of forecasting individual stock returns using a machine learning model and 207 firm characteristics from Chen and Zimmermann (2022). We generate monthly out-of-sample firm-level stock return forecasts via the `XGBoost` algorithm (Chen and Guestrin 2016), a powerful machine learning device based on decision trees that performs well in forecasting competitions in a variety of domains. We use the `XGBoost` forecasts to sort stocks into quintiles and construct a zero-investment portfolio that goes long (short) the fifth (first) quintile, with each leg value weighted. The long-short portfolio based on

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machine learning models to portfolio performance, thereby providing insight into the sources of the economic value generated by return predictability. Jensen et al. (2022) and Aleti, Bollerslev, and Siggard (2023) recently develop measures for estimating the contributions of predictors to portfolio performance metrics in different contexts. We explain how our  $\text{SPPC}_p$  significantly differs from these measures in Section 2.2.

<sup>5</sup>The  $\text{SPPC}_p$  can also be used to measure the contributions of predictors to portfolio performance when machine learning approaches are used to directly estimate optimal portfolio weights (e.g., Kozak, Nagel, and Santosh 2020; Jensen et al. 2022; Chen, Pelger, and Zhu forthcoming)

the XGBoost forecasts performs impressively, generating annualized Sharpe and Calmar ratios of 1.80 and 1.44, respectively, for the 1973:01 to 2021:12 forecast evaluation period, both of which are well above the corresponding ratios for the aggregate market portfolio (0.47 and 0.14, respectively). The XGBoost portfolio also generates economically large and statistically significant alphas in the context of two leading multifactor models, namely, a six-factor model comprised of the five Fama and French (2015) factors and a momentum factor as well as the Hou et al. (2021) augmented q-factor model. In sum, we find that firm-level stock return forecasts based on a large number of firm characteristics and machine learning produce substantial economic value.

After placing the individual firm characteristics into 20 groups based on economic concepts, we estimate the contributions of the predictor groups to portfolio performance using the  $SPPC_p$ . The *Risk*, *Earnings*, *Seasonal momentum*, and *Momentum* groups play leading roles in accounting for the substantive Sharpe and Calmar ratios as well as the sizable alphas generated by the XGBoost portfolio. For example, the XGBoost portfolio increases the Sharpe ratio by 1.33 vis-à-vis the market portfolio for the full 1973:01 to 2021:12 forecast evaluation period; the four groups together account for 0.86 (65%) of the increase. In contrast, the *Sales* and *Ownership* groups contribute negatively to portfolio performance across the different metrics.

The performance of the XGBoost portfolio tends to diminish after 2002, although it still outperforms the market portfolio, especially during business-cycle recessions. To examine how the contributions of the predictor groups to portfolio performance change over time, we use the  $SPPC_p$  to estimate the group contributions for subsamples and rolling windows from the full forecast evaluation period. While the *Risk* and *Momentum* groups typically make substantial positive contributions to portfolio performance through 2002, they often make negative contributions thereafter. Groups making consistently positive and sizable contributions over the full forecast evaluation period include *Earnings*, *Seasonal momentum*, and *Investment*. Overall, the  $SPPC_p$  sheds considerable light on how the predictor groups

contribute to portfolio performance, thereby improving our understanding of the role of predictors in generating economic value with respect to cross-sectional return predictability in a machine learning model.

The rest of the paper is organized as follows. Section 2 provides background on the conventional use of Shapley values for model interpretation and explains our extensions, culminating in the  $SPPC_p$  to estimate the contributions of predictors in machine learning models to portfolio performance. Section 3 reports results for the empirical application. Section 4 concludes.

## 2. Methodology

This section presents our methodology for decomposing portfolio performance in terms of the underlying predictors that guide asset allocation using the  $SPPC_p$ . In line with our application in Section 3, we consider a setting in which we forecast individual stock returns using firm characteristics via a pooled prediction model. It is straightforward to modify the presentation in this section to accommodate other settings.

### 2.1. Shapley Values

As background, we begin with a description of conventional Shapley values, which are generally viewed as the most informative interpretation tool for fitted prediction models. The intuition for using Shapley values for model interpretation is to exploit the analogy between players in a cooperative game earning a payoff and the predictors in a forecasting model, where the payoff corresponds to the model’s prediction.<sup>6</sup> According to the logic of Shapley values, payoffs are fairly allocated to the players in a game. In the context of prediction, we are interested in fairly allocating the contributions of the predictors to a model’s prediction. This is a nontrivial task, especially for models with correlated predictors and interactions between them. Štrumbelj and Kononenko (2010, 2014) and Lundberg and Lee (2017) show

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<sup>6</sup>Parts of this section draw on Borup et al. (2023, Section 2).

how Shapley values can be used to allocate the contributions of the predictors to a prediction made by the model. We adapt their ideas to a panel setting where a model generates predictions for individual stock returns over time based on a set of firm characteristics.<sup>7</sup>

In terms of notation, we index individual predictors by  $p$ , with the index set of predictors denoted by  $S = \{1, \dots, P\}$ . We index cross-sectional units by  $i$  and denote the index set of cross-section units by  $C = \{1, \dots, N\}$ .<sup>8</sup> We denote the  $P$ -vector of firm characteristics (i.e., predictors) for stock  $i$  in period  $t$  by  $\mathbf{x}_{i,t} = [x_{1,i,t} \ \dots \ x_{p,i,t}]^\ell$ , while  $r_{i,t}$  denotes the return on stock  $i$  in period  $t$ . The prediction model is given by

$$r_{i,t+1} = f(\mathbf{x}_{i,t}) + \varepsilon_{i,t+1}, \quad (1)$$

where  $f(\mathbf{x}_{i,t})$  is the conditional expectation (i.e., prediction) function, and  $\varepsilon_{i,t}$  is a zero-mean and serially uncorrelated disturbance term. The fitted model is denoted by  $\hat{f}$ . We use  $W_j = \{t_{j,\text{start}}, \dots, t_{j,\text{end}} - 1\}$  to represent the window of panel data observations used to train the model. The prediction model can be estimated using an expanding or rolling window along the time dimension; for the former (latter), the cardinality of  $W_j$  increases (remains constant). We denote the prediction function evaluated at instance  $\mathbf{x}_{i,t}$  and trained using window  $W_j$  by  $\hat{f}(\mathbf{x}_{i,t}; W_j)$ .

The Shapley value measures the marginal contribution of the predictor  $x_{p,i,t}$  to the prediction  $\hat{f}(\mathbf{x}_{i,t}; W_j)$  given  $S \setminus \{p\}$  (i.e., given the presence of all of the other predictors in the model). By relying on insights from coalitional game theory, Shapley values fairly allocate the marginal contributions among the individual predictors. Formally, adapting Štrumbelj and Kononenko (2010, 2014) to our panel data framework, we can express the Shapley value for predictor  $p$  and instance  $\mathbf{x}_{i,t}$  for a prediction model trained using the panel data

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<sup>7</sup>In this section, we focus on regression prediction. The methodology can be straightforwardly applied to classification prediction. We consider both regression and classification in our empirical application in Section 3.

<sup>8</sup>For notational simplicity, we assume that the number of cross-sectional observations is the same each period. In our empirical application in Section 3, the number of cross-sectional units changes over time. It is straightforward to modify the notation to allow for time variation in the number of cross-sectional units.



observations in window  $W_j$  as

$$\phi_p(\mathbf{x}_{i,t}; W_j) = \sum_{Q \subseteq S \setminus \{p\}} \frac{|Q|!(P - |Q| - 1)!}{P!} [\xi_{Q \cup \{p\}}(\mathbf{x}_{i,t}; W_j) - \xi_Q(\mathbf{x}_{i,t}; W_j)] \quad (2)$$

for  $p \in S$ ,  $i \in C$ , and  $t \in W_j$ , where  $Q$  is a subset of predictors (i.e., a coalition),  $Q \subseteq S \setminus \{p\}$  constitutes the set of all possible coalitions of  $P - 1$  predictors in  $S$  that exclude predictor  $p$ ,  $|Q|$  is the cardinality of  $Q$ ,

$$\xi_Q(\mathbf{x}_{i,t}; W_j) = \mathbb{E} \left[ \hat{f} \mid X_{k,i,t} = x_{k,i,t} \forall k \in Q; W_j \right] \quad (3)$$

is the value function, and  $\mathbb{E}$  is the expectation operator. Equation (3) is the prediction of the fitted model conditional on the predictors in the coalition  $Q$ , with the predictors not in  $Q$  integrated out. Accordingly, the expression in brackets in Equation (2),  $\xi_{Q \cup \{p\}}(\mathbf{x}_{i,t}; W_j) - \xi_Q(\mathbf{x}_{i,t}; W_j)$ , is the change in the prediction of the fitted model when we condition on the predictors in the coalition  $Q$  and predictor  $p$  relative to when we condition on the predictors in  $Q$  only. Equation (2) takes a weighted average of the change in the value function for all possible coalitions of  $P - 1$  predictors that exclude  $p$ . The change in the value function receives the weight  $|Q|!(P - |Q| - 1)!/P!$ , where the weights sum to one. In sum, to measure the marginal contribution of  $p$  to the prediction corresponding to instance  $\mathbf{x}_{i,t}$ , Shapley values rely on coalitions to control for the presence of the other predictors in the model.

Among other attractive properties, the Shapley value in Equation (2) is characterized by local accuracy (or efficiency):

$$\sum_{p \in S} \phi_p(\mathbf{x}_{i,t}; W_j) = \hat{f}(\mathbf{x}_{i,t}; W_j) - \mathbb{E} \left[ \hat{f}; W_j \right] \quad (4)$$

for  $i \in C$  and  $t \in W_j$ , where  $\mathbb{E}[\hat{f}; W_j]$  is the baseline prediction corresponding to the unconditional expectation of  $\hat{f}$ . This is a natural baseline for a prediction model, as it is the forecast based on the empty coalition set. According to Equation (4), the model prediction

corresponding to instance  $\mathbf{x}_{i,t}$  can be exactly decomposed (in terms of the deviation from the baseline prediction) into the sum of the Shapley values for the individual predictors for that instance. Other properties of Shapley values include missingness, symmetry, and linearity.<sup>9</sup>

In general, it is infeasible to exactly compute the Shapley value in Equation (2) for more than a relatively small number of predictors. The issue is that the prediction function contained in the value function needs to be evaluated for all possible coalitions of predictors with and without  $p$ . Štrumbelj and Kononenko (2010, 2014) propose an algorithm based on the sampling-based approach of Castro, Gómez, and Tejada (2009). We develop a refined version of their algorithm to compute the Shapley value in Equation (2). In Section 2.2, we extend the algorithm to estimate the contributions of the individual predictors to portfolio performance.

We begin by expressing Equation (2) in the following equivalent form:

$$\phi_p(\mathbf{x}_{i,t}; W_j) = \frac{1}{P!} \sum_{\mathcal{O} \in \pi(P)} [\xi_{\text{Pre}_p(\mathcal{O})}(\mathbf{x}_{i,t}; W_j) - \xi_{\text{Pre}_p(\mathcal{O})}(\mathbf{x}_{i,t}; W_j)] \quad (5)$$

for  $p \in S$ ,  $i \in C$ , and  $t \in W_j$ , where  $\mathcal{O}$  is an ordered permutation for the predictor indices in  $S$ ,  $\pi(P)$  is the set of all ordered permutations for  $S$ , and  $\text{Pre}_p(\mathcal{O})$  is the set of indices that precede  $p$  in  $\mathcal{O}$ . To implement the algorithm, we make a random draw  $m$  with replacement of an ordered permutation from  $\pi(P)$ , denoted by  $\mathcal{O}_m$ . Using  $\mathcal{O}_m$ , we compute the following:

$$\hat{\theta}_{p,m}(\mathbf{x}_{i,t}; W_j) = \frac{1}{|C||W_j|} \sum_{u \in C} \sum_{s \in W_j} \left[ \hat{f}(\mathbf{x}_{k,i,t} : k \in \text{Pre}_p(\mathcal{O}_m) \cup \{p\}, \mathbf{x}_{l,u,s} : l \in \text{Post}_p(\mathcal{O}_m); W_j) - \hat{f}(\mathbf{x}_{k,i,t} : k \in \text{Pre}_p(\mathcal{O}_m), \mathbf{x}_{l,u,s} : l \in \text{Post}_p(\mathcal{O}_m) \cup \{p\}; W_j) \right] \quad (6)$$

for  $p \in S$ ,  $i \in C$ , and  $t \in W_j$ , where  $\text{Post}_p(\mathcal{O})$  is the set of indices that follow  $p$  in  $\mathcal{O}$ . To integrate out the predictors not in the coalition when computing the conditional expectation in Equation (3), Equation (6) uses “background data” from the training sample (Štrumbelj and Kononenko 2010, 2014; Lundberg and Lee 2017). In effect, Equation (6) samples from the empirical marginal distribution of the training sample for the predictors not in the

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<sup>9</sup>See Molnar (2022) for details on the other properties of Shapley values.

coalition when integrating them out. Because this implicitly assumes that the predictors in and not in the coalition are independently distributed, Lundberg and Lee (2017) suggest sampling from the empirical conditional distribution for the predictors not in the coalition. Nevertheless, to fairly allocate the contributions of the individual predictors, based on Pearl (2009), Janzing, Minorics, and Blöbaum (2020) point out that it is more appropriate to use the empirical marginal distribution. We follow the recommendation of Janzing, Minorics, and Blöbaum (2020) in Equation (6).

The estimate of the Shapley value  $\phi_p(\mathbf{x}_{i,t}; W_j)$  in Equation (5) is given by

$$\hat{\phi}_p(\mathbf{x}_{i,t}; W_j) = \frac{1}{2M} \sum_{m=1}^{2M} \hat{\theta}_{p,m}(\mathbf{x}_{i,t}; W_j) \quad (7)$$

for  $p \in S$ ,  $i \in C$ , and  $t \in W_j$ , where  $M$  is the number of draws. We increase the computational efficiency of the algorithm in two ways. First, we compute Shapley values for each predictor  $p \in S$  for each random draw  $m$  (Castro, Gómez, and Tejada 2009). Second, we employ antithetic sampling as a variance-reduction device by computing  $\hat{\theta}_{p,m}(\mathbf{x}_{i,t}; W_j)$  in Equation (6) for the original order of a randomly drawn ordered permutation and when the order is reversed (Mitchell et al. 2022). Like the actual Shapley value in Equation (2), the estimate of the Shapley value in Equation (7) is characterized by local accuracy:

$$\sum_{p \in S} \hat{\phi}_p(\mathbf{x}_{i,t}; W_j) = \hat{f}(\mathbf{x}_{i,t}; W_j) - \underbrace{\bar{\hat{f}}(W_j)}_{\hat{\phi}_\emptyset(W_j)} \quad (8)$$

for  $i \in C$  and  $t \in W_j$ , where

$$\bar{\hat{f}}(W_j) = \frac{1}{|C||W_j|} \sum_{i \in C} \sum_{t \in W_j} \hat{f}(\mathbf{x}_{i,t}; W_j) \quad (9)$$

is the average in-sample prediction for the model trained using sample  $W_j$ . The average in-sample prediction corresponds to the baseline forecast based on the empty coalition set, denoted by  $\hat{\phi}_\emptyset(W_j)$  in Equation (8).

To this point, we have followed the convention of computing Shapley values for in-sample model predictions corresponding to the training sample observations. For developing the  $\text{SPPC}_p$  in Section 2.2, it is helpful to define the Shapley value corresponding to an out-of-sample observation. Suppose that we train a model using window  $W_j$  and generate an out-of-sample return forecast for stock  $i$  and period  $t_{j,\text{end}} + 1$  based on the fitted model:

$$\hat{r}_{i,t_{j,\text{end}}+1} = \hat{f}(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j) \quad (10)$$

for  $i \in C$ . Modifying Equation (5), we define the Shapley value corresponding to the out-of-sample forecast  $\hat{r}_{i,t_{j,\text{end}}+1}$  as

$$\phi_p(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j) = \frac{1}{P!} \sum_{O \in 2^{\pi(P)}} [\xi_{\text{Pre}_p(O)} \circ \hat{r}_{pg}(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j) - \xi_{\text{Pre}_p(O)}(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j)] \quad (11)$$

for  $p \in S$  and  $i \in C$ . We suitably modify the algorithm to estimate Equation (11). After making a random draw  $m$ , Equation (6) becomes

$$\hat{\theta}_{p,m}(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j) = \hat{r}_{i,t_{j,\text{end}}+1,m,p}(\mathbf{x}_{i,t_{j,\text{end}}+1} ; W_j) - \hat{r}_{i,t_{j,\text{end}}+1,m,\eta p}(\mathbf{x}_{i,t_{j,\text{end}}+1} ; W_j) \quad (12)$$

for  $p \in S$  and  $i \in C$ , where

$$\begin{aligned} \hat{r}_{i,t_{j,\text{end}}+1,m,p}(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j) = \\ \frac{1}{|C| |W_j|} \sum_{u \in 2^C} \sum_{s \in 2^{W_j}} \hat{f}(\mathbf{x}_{k,i,t_{j,\text{end}}} : k \in \text{Pre}_p(\mathcal{O}_m) \cup \{p\}, \mathbf{x}_{l,u,s} : l \in \text{Post}_p(\mathcal{O}_m) ; W_j) \end{aligned} \quad (13)$$

and

$$\begin{aligned} \hat{r}_{i,t_{j,\text{end}}+1,m,\eta p}(\mathbf{x}_{i,t_{j,\text{end}}} ; W_j) = \\ \frac{1}{|C| |W_j|} \sum_{u \in 2^C} \sum_{s \in 2^{W_j}} \hat{f}(\mathbf{x}_{k,i,t_{j,\text{end}}} : k \in \text{Pre}_p(\mathcal{O}_m), \mathbf{x}_{l,u,s} : l \in \text{Post}_p(\mathcal{O}_m) \cup \{p\} ; W_j). \end{aligned} \quad (14)$$

The estimate of  $\phi_p(\mathbf{x}_{i,t_j,\text{end}}; W_j)$  in Equation (11) is then given by

$$\hat{\phi}_p(\mathbf{x}_{i,t_j,\text{end}}; W_j) = \frac{1}{2M} \sum_{m=1}^{2M} \hat{\theta}_{p,m}(\mathbf{x}_{i,t_j,\text{end}}; W_j) \quad (15)$$

for  $p \in S$  and  $i \in C$ .

Observe that we continue to use background data from the training sample in Equation (12) to integrate out the predictors not in a coalition. In this way, we remain “true to the model” that generates the out-of-sample forecast. The estimate of the Shapley value for the out-of-sample prediction in Equation (15) continues to be characterized by local accuracy:

$$\sum_{p \in S} \hat{\phi}_p(\mathbf{x}_{i,t_j,\text{end}}; W_j) = \underbrace{\hat{f}(\mathbf{x}_{i,t_j,\text{end}}; W_j)}_{\hat{r}_{i,t_j,\text{end}+1}} - \hat{\phi}_i(W_j) \quad (16)$$

for  $i \in C$ . Equation (16) says that we can exactly decompose the one-step-ahead out-of-sample return forecast for stock  $i$  into the contributions of the individual predictors.

## 2.2. Decomposing Portfolio Performance

Consider an investor who decides on their allocations across the  $N$  stocks for period  $t_{j,\text{end}} + 1$  based on the set of return forecasts formed using data through period  $t_{j,\text{end}}$  ( $\hat{r}_{i,t_j,\text{end}+1} = \hat{f}(\mathbf{x}_{i,t_j,\text{end}}; W_j)$  for  $i \in C$ ). The allocation to  $i$  generally depends on the entire set of return forecasts for  $t_{j,\text{end}} + 1$ , so we denote the portfolio weight for  $i$  by the function

$$w_{i,t_j,\text{end}+1} \left( \left\{ \hat{f}(\mathbf{x}_{i,t_j,\text{end}}; W_j) \right\}_{i \in C} \right) \quad (17)$$

for  $i \in C$ . The investor could, for example, employ a portfolio optimizer based on the return forecasts or form a long-short portfolio by going long (short) the stocks with the highest (lowest) return forecasts. Our methodology is general, so it applies to any strategy for mapping the return forecasts to the portfolio weights.

The portfolio return for  $t_{j,\text{end}} + 1$  is given by

$$r_{t_{j,\text{end}}+1}^{\text{Port}} = \sum_{i \in \mathcal{C}} w_{i,t_{j,\text{end}}+1} \left( \left\{ \hat{f}(\mathbf{x}_{i,t_{j,\text{end}}}; W_j) \right\}_{i \in \mathcal{C}} \right) r_{i,t_{j,\text{end}}+1}. \quad (18)$$

We can use the logic of Shapley values to decompose the portfolio return in Equation (18). In terms of the algorithm, we modify Equation (12) as follows:

$$\begin{aligned} \hat{\theta}_{p,m} \left( \left\{ \mathbf{x}_{i,t_{j,\text{end}}} \right\}_{i \in \mathcal{C}}; W_j \right) = & \\ & \sum_{i \in \mathcal{C}} \left[ w_{i,t_{j,\text{end}}+1} \left( \left\{ \hat{r}_{i,t_{j,\text{end}}+1,m,p}(\mathbf{x}_{i,t_{j,\text{end}}}; W_j) \right\}_{i \in \mathcal{C}} \right) r_{i,t_{j,\text{end}}+1} \right] - \\ & \sum_{i \in \mathcal{C}} \left[ w_{i,t_{j,\text{end}}+1} \left( \left\{ \hat{r}_{i,t_{j,\text{end}}+1,m,\eta p}(\mathbf{x}_{i,t_{j,\text{end}}}; W_j) \right\}_{i \in \mathcal{C}} \right) r_{i,t_{j,\text{end}}+1} \right] \end{aligned} \quad (19)$$

for  $p \in S$ . Equation (19) measures the change in the portfolio return for period  $t_{j,\text{end}} + 1$  when we condition on the predictors in the coalition including and excluding predictor  $p$ . When integrating out the predictors not in a coalition, we again use background data from the training sample  $W_j$  so that we remain true to the model that generates the set of return forecasts that determines the portfolio weights. To estimate the Shapley-based contribution of predictor  $p$  to the portfolio return, Equation (15) becomes

$$\hat{\phi}_p \left( \left\{ \mathbf{x}_{i,t_{j,\text{end}}} \right\}_{i \in \mathcal{C}}; W_j \right) = \frac{1}{2M} \sum_{m=1}^{2M} \hat{\theta}_{p,m} \left( \left\{ \mathbf{x}_{i,t_{j,\text{end}}} \right\}_{i \in \mathcal{C}}; W_j \right) \quad (20)$$

for  $p \in S$ .

An important issue in implementing the Shapley-based decomposition of the portfolio return is deciding on the return corresponding to the empty coalition set. With the empty coalition set, we have no predictors to determine the portfolio weights in Equation (17), so we need to specify the portfolio return for the empty coalition set, which we denote by  $r_{t_{j,\text{end}}+1}^{\text{Base}}$ , since the portfolio can be viewed as a “baseline” portfolio. We need  $r_{t_{j,\text{end}}+1}^{\text{Base}}$  to compute

Equation (19) when  $p$  is the first element in the ordered permutation  $\mathcal{O}_m$ . Furthermore,  $r_{t_{j,\text{end}}+1}^{\text{Base}}$  appears in the local accuracy condition.

The selection of the baseline portfolio is at the discretion of the researcher. To determine the baseline portfolio, it is sensible to ask, “If I had an empty set of predictors—and so no predictor information—how would I form a portfolio?” A relevant baseline will depend on the context; for example, for a portfolio that broadly invests in equities, the CRSP value-weighted aggregate market portfolio seems a natural choice. The portfolio return decomposition in Equation (20) satisfies local accuracy:

$$\sum_{p \in \mathcal{S}} \hat{\phi}_p \left( \{ \mathbf{x}_{i,t_{j,\text{end}}} \}_{i \in \mathcal{C}} ; W_j \right) = r_{t_{j,\text{end}}+1}^{\text{Port}} - r_{t_{j,\text{end}}+1}^{\text{Base}}. \quad (21)$$

Based on a property of Shapley values, Equation (21) indicates that we can decompose the portfolio return in period  $t_{j,\text{end}} + 1$  (in terms of the deviation from the baseline portfolio return) into the return contributions made by each of the  $P$  predictors.

Finally, we extend our approach to compute the  $\text{SPPC}_p$ . To do so, we need to take into account the entire series of out-of-sample return forecasts and corresponding portfolio returns over the forecast evaluation period. In terms of the time dimension, we assume that the sample of panel data spans  $T$  periods and that data through period  $T_{\text{in}}$  are used to train the model that generates the first set of out-of-sample return forecasts for period  $T_{\text{in}} + 1$ . The model is then retrained using panel data through  $T_{\text{in}} + 1$  to generate the next set of return forecasts for  $T_{\text{in}} + 2$ . Continuing in this manner through the end of the available sample,  $T - T_{\text{in}} = D$  sets of return forecast are generated, where the final model is trained using panel data through  $T - 1$  to generate the last set of return forecasts for  $T$ . We define the index set of training windows used to fit the sequence of models as  $W = \{1, \dots, D\}$ , where  $t_{j,\text{end}}$  corresponds to  $T_{\text{in}}, T_{\text{in}} + 1, \dots, T - 1$  for  $j = 1, 2, \dots, D$ , respectively.

The key insight for computing the  $\text{SPPC}_p$  is to wrap a function corresponding to the performance metric around the portfolio returns. Denoting a performance metric function

by  $\mathcal{M}(\cdot)$ , which depends on the sequence of portfolio returns over the forecast evaluation period, we modify Equation (19) in the algorithm to

$$\begin{aligned} \hat{\theta}_{p,m} \left( \{ \mathbf{x}_{i,t_j,\text{end}} \}_{i \in \mathcal{C}} ; W, \mathcal{M} \right) = \\ \mathcal{M} \left( \left\{ \sum_{i \in \mathcal{C}} \left[ w_{i,t_j,\text{end}+1} \left( \{ \hat{r}_{i,t_j,\text{end}+1,m,p}(\mathbf{x}_{i,t_j,\text{end}} ; W_j) \}_{i \in \mathcal{C}} \right) r_{i,t_j,\text{end}+1} \right] \right\}_{j \in \mathcal{W}} \right) - \\ \mathcal{M} \left( \left\{ \sum_{i \in \mathcal{C}} \left[ w_{i,t_j,\text{end}+1} \left( \{ \hat{r}_{i,t_j,\text{end}+1,m,\rho p}(\mathbf{x}_{i,t_j,\text{end}} ; W_j) \}_{i \in \mathcal{C}} \right) r_{i,t_j,\text{end}+1} \right] \right\}_{j \in \mathcal{W}} \right) \end{aligned} \quad (22)$$

for  $p \in S$ . The Shapley-based estimate of the contribution of predictor  $p$  to the portfolio performance metric is then given by

$$\underbrace{\hat{\phi}_p \left( \{ \mathbf{x}_{i,t_j,\text{end}} \}_{i \in \mathcal{C}} ; W, \mathcal{M} \right)}_{\text{SPPC}_p} = \frac{1}{2M} \sum_{m=1}^{2M} \hat{\theta}_{p,m} \left( \{ \mathbf{x}_{i,t_j,\text{end}} \}_{i \in \mathcal{C}} ; W, \mathcal{M} \right) \quad (23)$$

for  $p \in S$ . Again, the local accuracy property of Shapley values applies, so the contributions of the predictors to the performance metric sum to the metric for the portfolio in excess of that for the baseline portfolio:

$$\sum_{p \in S} \text{SPPC}_p = \mathcal{M} \left( \left\{ r_{t_j,\text{end}+1}^{\text{Port}} \right\}_{j \in \mathcal{W}} \right) - \mathcal{M} \left( \left\{ r_{t_j,\text{end}+1}^{\text{Base}} \right\}_{j \in \mathcal{W}} \right). \quad (24)$$

Our  $\text{SPPC}_p$  in Equation (23) allows a researcher to estimate how an individual predictor contributes to portfolio performance, while Equation (24) indicates that the sum of the  $\text{SPPC}_p$  estimates provide an exact decomposition of portfolio performance relative to the baseline portfolio.

In sum, the Shapley value ascertains the contribution of an individual predictor  $p$  to a prediction by forming a coalition of predictors and measuring the change in value of the prediction when  $p$  is included and excluded in the conditioning set based on the coalition in the fitted prediction model. The change in the value of the prediction corresponding to  $p$



is averaged over many coalitions to arrive at the Shapley value, which provides a procedure for fairly allocating the contribution of  $p$  to the fitted model’s prediction. We extend the logic of the Shapley value to an entity of interest to an investor (e.g., a portfolio return or performance metric). Thus, we measure the contribution of  $p$  to the entity of interest by forming a coalition of predictors and computing the change in value of the entity when  $p$  is included and excluded in the conditioning set based on the coalition in the fitted prediction model. We average the change in value corresponding to  $p$  over many coalitions, providing a Shapley-based approach for fairly allocating the contribution of  $p$  to portfolio performance.

We emphasize that the  $\text{SPPC}_p$  is very general. It is model agnostic, so it applies to any fitted prediction model (linear or nonlinear, parametric or nonparametric). It also accommodates any rule for mapping the return forecasts to portfolio weights as well as any performance metric.

Two recent papers propose methods for measuring the contributions of predictors to portfolio performance metrics. In the context of developing a framework for constructing an “implementable efficient frontier” via machine learning that accounts for transaction costs, Jensen et al. (2022) propose an “economic feature importance” measure of how a feature (i.e., predictor) affects realized utility. The measure is based on permutation feature importance (Breiman 2001), an intuitive approach for assessing feature importance in machine learning models. However, the permutation approach does not possess the attractive properties of Shapley values, including local accuracy. In contrast, because our  $\text{SPPC}_p$  is based on Shapley values, it is characterized by local accuracy, so it exactly decomposes any portfolio performance metric—including realized utility—into the contributions made by the complete set of features.

Aleti, Bollerslev, and Siggaard (2023) predict the intraday aggregate market return based on a large set of cross-sectional predictors and the LASSO (Tibshirani 1996), which they use to implement intraday trading strategies for ETFs. They develop a Shapley-based algorithm to measure the contributions of the predictors to Sharpe ratios and alphas for linear models

with no interactions among the predictors. In contrast, our  $\text{SPPC}_p$  is model agnostic, so it can be applied to any prediction model, including nonlinear machine learning models.

### 2.3. Computational Issues

A challenge in estimating the  $\text{SPPC}_p$  is computational cost. The computational time for estimating the  $\text{SPPC}_p$  is dominated by the need to evaluate the fitted prediction function  $\hat{f}$  many times. When computing the  $\text{SPPC}_p$ , we need to evaluate the change in the out-of-sample return forecast for firm  $i$  when adding predictor  $p$  to the coalition of predictors preceding it in the randomly drawn ordered permutation  $\mathcal{O}_m$ , which in turn requires evaluating  $\hat{r}_{i,t_j,\text{end}+1,m,p}$  and  $\hat{r}_{i,t_j,\text{end}+1,m,\rho p}$  in Equation (13) and Equation (14), respectively. For  $\hat{r}_{i,t_j,\text{end}+1,m,p}$  ( $\hat{r}_{i,t_j,\text{end}+1,m,\rho p}$ ), we need to integrate out the predictors following  $p$  (following and including  $p$ ) in  $\mathcal{O}_m$ . To accomplish this, we effectively average over the panel training sample observations, so we need to evaluate  $\hat{f}$  for each observation in the panel training data twice, once with and once without  $p$  integrated out. We also need to repeat this process for each predictor  $p \in S$ . This, however, allows us to eliminate half of the number of evaluations of  $\hat{f}$ , so we need to evaluate  $\hat{f}$  once for each predictor  $p \in S$  with the predictors following  $p$  integrated out using each observation in the panel training data.<sup>10</sup> To measure the change in the out-of-sample return forecast when adding predictor  $p$  to the coalition of predictors preceding it in  $\mathcal{O}_m$  for all of the firms, we evaluate  $\hat{r}_{i,t_j,\text{end}+1,m,p}$  and  $\hat{r}_{i,t_j,\text{end}+1,m,\rho p}$  for  $i \in C$ . In effect, we need to evaluate  $\hat{f}$  for each predictor for each observation in the panel training data for each firm.

To this point, we have focused on computations for a single month, but we need to perform the computations for each month in the entire out-of-sample period. In total, we

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<sup>10</sup>By way of example, consider three predictors and the ordered permutation  $\mathcal{O}_m = \{3, 2, 1\}$ , so predictor 3 is added to the coalition of predictors first, then 2, then 1. The effect of adding predictor 3 is measured by computing the forecast conditional on predictor 3 with predictors 2 and 1 integrated out and comparing it to the forecast based on the empty coalition set that integrates out all of the predictors. The effect of adding predictor 2 is measured by computing the forecast conditional on predictors 3 and 2 with predictor 1 integrated out and comparing it to the forecast conditional on predictor 3 with predictors 2 and 1 integrated out. Clearly, we do not need to recompute the latter, as we have already computed it in the first step when predictor 3 is added to the empty predictor coalition set.

need to evaluate  $\hat{f}$  for each predictor and each firm for all of the observations in the panel training data and all of the months in the out-of-sample period. Furthermore, we need to do this  $2 \times M$  times for the sampling-based approach (taking into account antithetic sampling).

In the empirical application in Section 3, we analyze the contributions of 20 groups of predictors formed on the basis of economic concepts for the 1973:01 to 2021:12 out-of-sample period (588 months). We have an average of approximately 2,000 firms for each month in the out-of-sample period as well as an average of about 750,000 firm-month observations for the sequence of panel training datasets. There are two dimensions along which to limit computational costs: (1) the number of randomly drawn ordered permutations ( $M$ ) and (2) the proportion of training sample observations to use when integrating out predictors. A decrease in each leads to a proportional reduction in computational time. For our empirical application, we set  $M = 50$  (for a total of  $2 \times 50 = 100$  ordered permutations with antithetic sampling) and use 10% of the training sample observations when integrating out predictors.<sup>11</sup>

Thus, as a first step, we need to evaluate fitted prediction functions approximately  $20 \times 588 \times 2,000 \times 0.10 \times 750,000 \times 50 \times 2 = 176,400,000,000,000$  times to compute the required forecasts in Equations (13) and (14) for the out-of-sample period. In this computationally expensive first step, we used 306 and 274 core-months of Intel Xeon Platinum 8260 and Intel Xeon Gold 6148 processors, respectively, with AVX-512 enabled. To substantially reduce computational time after this step, note that Equations (13) and (14) are the lowest unit in any decomposition of a portfolio performance metric. We store the forecasts on disk and cache Equations (13) and (14) in memory when we compute the  $SPPC_p$  for a specific performance metric. The benefits of this cannot be overstated. After the extensive  $306 + 274 = 580$  core-months of computations in the first step, we can compute all of the predictor contributions for any performance metric nearly instantly because we no longer

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<sup>11</sup>It is standard to set  $M$  to a relatively low value and use a subsample of the training sample observations when computing conventional Shapley values; for example, the popular SHAP package in python uses defaults of  $M = 10$  and 100 observations from the training sample (corresponding to roughly 0.01% of the training sample observations on average in our application). We use more rigorous settings to improve estimation accuracy.

need to evaluate  $\hat{f}$  and integrate out predictors over the training sample observations. Using the computed forecasts from the first step, we compute the series of portfolio returns inside the curly brackets in Equation (22). To compute the  $SPPC_p$  for any performance metric, we only need to evaluate the metric wrapped around the series of portfolio returns (which is typically much less expensive than evaluating  $\hat{f}$ ) about  $20 \times 50 \times 2 = 2,000$  times, which incurs no meaningful computational time for the performance metrics considered in the empirical application in this paper.<sup>12</sup>

### 3. Empirical Application

In this section, we use the  $SPPC_p$  from Section 2 to analyze a leading question in empirical asset pricing: Which types of firm characteristics are important for determining cross-sectional expected stock returns? In line with recent studies, we analyze the relevance of firm characteristics using out-of-sample tests (e.g., Lewellen 2015; Green, Hand, and Zhang 2017; Freyberger, Neuhierl, and Weber 2020; Gu, Kelly, and Xiu 2020; Avramov, Cheng, and Metzker 2023; Han et al. 2023). As in these studies, we forecast one-month-ahead cross-sectional returns using a large number of firm characteristics. The cross-sectional return forecasts are then used to form zero-investment long-short portfolios.

#### 3.1. Data

We use data for a large set of firm characteristic data from Chen and Zimmermann (2022), which are available at the [Open Source Asset Pricing](#) website. The data are comprised of 207 firm characteristics from the voluminous literature on cross-sectional expected returns. We use data spanning 1960:01 to 2021:12 (744 months). Following Freyberger, Neuhierl, and Weber (2020) and Gu, Kelly, and Xiu (2020), we transform each characteristic each month by cross-sectionally ranking the characteristics and then mapping the ranks into the  $[-1, 1]$  interval. Monthly firm-level stock return data are from CRSP. We consider all firms listed

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<sup>12</sup>We plan to post the code used to compute the  $SPPC_p$  estimates for the performance metrics reported in the empirical application in Section 3.

**Table 1. Characteristic Groups**

The table provides groups for 207 firm characteristics from Chen and Zimmermann (2022) used in the empirical application in Section 3. The characteristics are grouped according to 20 economic categories. The characteristic descriptions are from the [Open Source Asset Pricing](#) website; more information on the data and their sources is provided there.

| (1)<br>Description                      | (2)<br>Description                   | (3)<br>Description             |
|---|--------------------------------------|--------------------------------|
| <b>Panel A: Earnings (9)</b>            |                                      |                                |
| Excluded expenses                       | Earnings consistency                 | Earnings streak length         |
| Earnings announcement return            | Earnings surprise streak             | Analyst earnings per share     |
| Decline in analyst coverage             | Earnings surprise                    | Earnings-to-price ratio        |
| <b>Panel B: Earnings forecast (10)</b>  |                                      |                                |
| Earnings forecast to price              | Long-vs-short EPS forecasts          | Earnings forecast revisions    |
| EPS forecast revision                   | Long-term EPS forecast               | Up forecast                    |
| Change in forecast and accrual          | Predicted analyst forecast error     | EPS forecast dispersion        |
| Down forecast EPS                       |                                      |                                |
| <b>Panel C: Financing (10)</b>          |                                      |                                |
| Convertible debt indicator              | Net equity financing                 | Leverage component of BM       |
| Change in current operating liabilities | Net external financing               | Market leverage                |
| Change in financial liabilities         | Book leverage (annual)               | Net debt to price              |
| Net debt financing                      |                                      |                                |
| <b>Panel D: Financing alt (7)</b>       |                                      |                                |
| Composite equity issuance               | Initial public offerings             | Share issuance (5 year)        |
| Composite debt issuance                 | Share issuance (1 year)              | Spinoffs                       |
| Debt issuance                           |                                      |                                |
| <b>Panel E: Investment (14)</b>         |                                      |                                |
| Cash to assets                          | Growth in book equity                | Investment to revenue          |
| Net operating assets                    | Change in equity to assets           | Change in PPE and inv/assets   |
| Real estate holdings                    | Change in long-term investment       | Growth in advertising expenses |
| Tangibility                             | Change in net operating assets       | Advertising expense            |
| Asset growth                            | Growth in long term operating assets |                                |

on NYSE, AMEX, and NASDAQ with a market value on CRSP at the end of the previous month and a non-missing value for common equity in the firm’s annual financial statement. We compute the excess return for each stock in a given month using the CRSP risk-free return.<sup>13</sup>

Table 1 lists the 207 firm characteristics from Chen and Zimmermann (2022) along with their descriptions from [Open Source Asset Pricing](#). To keep computational costs manageable,

<sup>13</sup>As in Gu, Kelly, and Xiu (2020), we fill in missing values for a firm characteristic in a given month with the cross-sectional median for the available characteristic observations for that month.

**Table 1** (continued)

| (1)<br>Description                  | (2)<br>Description                   | (2)<br>Description                |
|-------------------------------------|--------------------------------------|-----------------------------------|
| <b>Panel F: Investment alt (12)</b> |                                      |                                   |
| Change in capital inv (ind adj)     | Inventory growth                     | Deferred revenue                  |
| Change in capex (2 years)           | Change in net noncurrent op assets   | Change in net financial assets    |
| Change in capex (3 years)           | Change in net working capital        | Employment growth                 |
| Brand capital investment            | Change in current operating assets   | Total accruals                    |
| <b>Panel G: Lead lag (9)</b>        |                                      |                                   |
| Customer momentum                   | Customers momentum                   | Price delay coeff                 |
| Earnings surprise of big firms      | Suppliers momentum                   | Price delay SE adjusted           |
| Industry return of big firms        | Price delay R square                 | Conglomerate return               |
| <b>Panel H: Liquidity (11)</b>      |                                      |                                   |
| Pastor-Stambaugh liquidity beta     | Probability of informed trading      | Days with zero trades (version 1) |
| Bid-ask spread                      | Size                                 | Days with zero trades (version 2) |
| Amihud's illiquidity                | Share turnover volatility            | Days with zero trades (version 3) |
| Price                               |                                      |                                   |
| <b>Panel I: Momentum (11)</b>       |                                      |                                   |
| Firm age—momentum                   | Momentum (12 month)                  | Momentum in high volume stocks    |
| 52 week high                        | Momentum (6 month)                   | Momentum based on FF3 residuals   |
| Industry momentum                   | Junk stock momentum                  | Trend factor                      |
| Intermediate momentum               | Momentum and LT reversal             |                                   |
| <b>Panel J: Ownership (11)</b>      |                                      |                                   |
| Sin stock (selection criteria)      | Takeover vulnerability               | Inst own and idio vol             |
| Active shareholders                 | Inst own and forecast dispersion     | Short interest                    |
| Breadth of ownership                | Inst own and market to book          | Governance index                  |
| Inst own among high short interest  | Inst own and turnover                |                                   |
| <b>Panel K: Profitability (14)</b>  |                                      |                                   |
| Mohanram G-score                    | Gross profits / total assets         | Return on assets (qtrly)          |
| Piotroski F-score                   | Inventory growth                     | Net income / book equity          |
| Cash productivity                   | Operating profits / book equity      | Taxable income to income          |
| Cash-based operating profitability  | Operating profitability R&D adjusted | O score                           |
| Change in taxes                     | Operating leverage                   |                                   |
| <b>Panel L: R&amp;D (8)</b>         |                                      |                                   |
| Citations to R&D expenses           | Organizational capital               | IPO and no R&D spending           |
| Patents to R&D expenses             | R&D over market cap                  | Unexpected R&D increase           |
| R&D capital-to-assets               | R&D ability                          |                                   |

we consolidate the predictors into 20 groups based on economic concepts.<sup>14</sup> We use the 34 categories in Chen and Zimmermann (2022) as a starting point and make various adjustments

<sup>14</sup>Harvey, Liu, and Zhu (2016), McLean and Pontiff (2016), Freyberger, Neuhierl, and Weber (2020), and Hou, Xue, and Zhang (2020) also categorize characteristics into five to six groups based on economic concepts. We specify a larger number of more narrowly defined economic groups, as we use the  $SPPC_p$  to estimate the contributions of the groups to various performance metrics.

**Table 1** (continued)

| (1)<br>Description                     | (2)<br>Description                   | (3)<br>Description                |
|--|--------------------------------------|-----------------------------------|
| <b>Panel M: Reversal (7)</b>           |                                      |                                   |
| Intangible return using BM             | Intangible return using Sale2P       | Medium-run reversal               |
| Intangible return using CFtoP          | Long-run reversal                    | Short-term reversal               |
| Intangible return using EP             |                                      |                                   |
| <b>Panel N: Risk (12)</b>              |                                      |                                   |
| Frazzini-Pedersen beta                 | Coskewness                           | Idiosyncratic risk                |
| CAPM beta                              | Return skewness                      | Idiosyncratic risk (3F model)     |
| Tail risk beta                         | Idiosyncratic skewness (3F model)    | Idiosyncratic risk (AHT)          |
| Coskewness using daily returns         | Systematic volatility                | Maximum return over month         |
| <b>Panel O: Risk alt (12)</b>          |                                      |                                   |
| Real dirty surplus                     | Industry concentration (equity)      | IPO and age                       |
| Pension funding status                 | Volatility smirk near the money      | Credit Rating Downgrade           |
| Industry concentration (sales)         | Put volatility minus call volatility | Exchange Switch                   |
| Industry concentration (assets)        | Cash-flow to price variance          | Firm age based on CRSP            |
| <b>Panel P: Sales (10)</b>             |                                      |                                   |
| Change in asset turnover               | Percent operating accruals           | Sales growth over overhead growth |
| Abnormal accruals                      | Percent total accruals               | Revenue growth rank               |
| Accruals                               | Sales growth over inventory growth   | Order backlog                     |
| Change in order backlog                |                                      |                                   |
| <b>Panel Q: Seasonal momentum (10)</b> |                                      |                                   |
| Momentum without the seasonal part     | Off season reversal years 16 to 20   | Return seasonality years 11 to 15 |
| Off season long-term reversal          | Return seasonality years 2 to 5      | Return seasonality years 16 to 20 |
| Off season reversal years 6 to 10      | Return seasonality years 6 to 10     | Return seasonality last year      |
| Off season reversal years 11 to 15     |                                      |                                   |
| <b>Panel R: Valuation (12)</b>         |                                      |                                   |
| Predicted div yield next month         | Dividend seasonality                 | Change in recommendation          |
| Efficient frontier index               | Share repurchases                    | Consensus recommendation          |
| Dividend initiation                    | Equity duration                      | Analyst recs and short-interest   |
| Dividend omission                      | Analyst optimism                     | Analyst value                     |
| <b>Panel S: Valuation ratio (11)</b>   |                                      |                                   |
| Book-to-market and accruals            | Cash flow to market                  | Sales-to-price                    |
| Total assets to market                 | Enterprise component of BM           | Net payout yield                  |
| Book to market using most recent ME    | Enterprise multiple                  | Payout yield                      |
| Book to market using December ME       | Sales-to-price                       |                                   |
| <b>Panel T: Volume (6)</b>             |                                      |                                   |
| Past trading volume                    | Option volume to average             | Volume to market equity           |
| Option to stock volume                 | Share volume                         | Volume trend                      |

to arrive at our 20 groups, with a goal of having groups that are reasonably similar in size. As shown in Table 1, the number of characteristics in a group ranges from six (*Volume*) to 14 (*Investment* and *Profitability*), so no groups are inordinately larger than others. Defining the

groups quite narrowly enables us to differentiate between types of characteristics in terms of a wide variety of economic concepts. Owing to the linearity property of Shapley values, all of the results for the  $SPPC_p$  in Section 2.2 hold for groups of individual characteristics.

### 3.2. Portfolio Construction and Prediction Models

Similarly to a number of recent studies (e.g., Freyberger, Neuhierl, and Weber 2020; Gu, Kelly, and Xiu 2020; Avramov, Cheng, and Metzker 2023; Han et al. 2023), we construct a zero-investment long-short portfolio that goes long (short) stocks with highest (lowest) machine learning return forecasts for the next month. We use 1960:01 to 1972:12 (156 months) as the initial in-sample estimation period and generate firm-level out-of-sample return forecasts and long-short portfolio returns for 1973:01 to 2021:12 (588 months). To keep the fitted prediction model timely, we retrain the model each month as additional data become available using a rolling window to generate the one-month-ahead firm-level return forecasts.

We compute return forecasts using both classification and regression prediction models. For the classification model, there are five classes, from the bottom 20% to the top 20% of stocks in terms of their returns. We describe the classification and regression prediction models in more detail below, after explaining how we construct the long-short portfolios.

To construct the long-short portfolio for month  $t+1$  based on information through month  $t$ , we proceed as follows. We generate return forecasts for all available stocks for month  $t+1$  using data through month  $t$ . Before forming the portfolio, to limit the role of small-cap stocks, we drop stocks with market capitalization below the NYSE 20th percentile at the end of month  $t$ . For the classification model, we take long (short) positions in those stocks predicted to be in the top (bottom) class in month  $t+1$ .<sup>15</sup> To further limit the role of small-cap stocks, the long and short legs are value weighted. We scale the weights in the long and short legs to sum to 1 and  $-1$ , respectively. For the regression model, we sort

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<sup>15</sup>For the classification model, note that the number of stocks in the long leg does not necessarily equal the number in the short leg.



stocks in terms of their return forecasts and take long (short) positions in those stocks in the top (bottom) 20% of sorted stocks. We again value weight the long and short legs and scale them to sum to 1 and  $-1$ , respectively.

We generate monthly firm-level out-of-sample return forecasts based on the 207 firm characteristics listed in Table 1 using the XGBoost algorithm (Chen and Guestrin 2016). XGBoost is based on decision trees, which allow for nonlinearities in predictive relations via multiway interactions and higher-order effects of predictors. A decision tree partitions the predictor space into non-overlapping regions and assigns a prediction (or score) for the target in each region. The classification and regression tree (CART) algorithm (Breiman et al. 1984) is typically used to partition the predictor space by applying a sequence of splitting rules. The split at the top of a tree is the “root node,” subsequent splits are “internal nodes,” and the final set of subgroups that define the predictive regions at the bottom of the tree are the “terminal” or “leaf nodes.” Decision trees can be used for both classification and regression problems. For a classification problem, the prediction is the class with the highest probability in a given leaf node; for a regression problem, the prediction is the average value of the target observations in a given leaf node.

XGBoost employs gradient boosting (Breiman 1997; Friedman 2001), which entails constructing an ensemble prediction function additively, where each function in the sequence is a relatively simple model; in the case of a decision tree, each function is a “shallow” tree. Simple models typically have low variance but relatively high bias. Gradient boosting seeks to lower the bias and thus improve out-of-sample performance in light of the bias-variance trade-off by fitting a decision tree to the residuals for the previous tree in the sequence. To help guard against overfitting and further improve out-of-sample performance, stochastic gradient boosting (Friedman 2002) refines conventional gradient boosting by using a randomly drawn subsample of the training data when fitting each decision tree in the sequence. XGBoost is a well known and powerful algorithm that employs stochastic gradient boosting

to fit prediction models based on decision trees.<sup>16</sup> It is a leading performer in forecasting competitions and compares favorably to other popular machine learning methods, particularly when the data are “tabular,” as in our application (e.g., Elsayed et al. 2021; Grinsztajn, Oyallon, and Varoquaux 2022).

An important step for improving out-of-sample performance is tuning the hyperparameters for the XGBoost algorithm.<sup>17</sup> We use a “walk-forward” procedure that respects the time-series dimension of the panel data to tune the hyperparameters. When computing the first set of out-of-sample return forecasts for 1973:01, we reserve the last 36 months (1970:01 to 1972:12) of the 1960:01 to 1972:12 initial in-sample estimation sample as a validation period for tuning the hyperparameters. We first train prediction models via XGBoost using data for 1960:01 to 1969:12 and the different combinations of the hyperparameter values. We plug the characteristic values for 1969:12 into the fitted models to generate return forecasts for 1970:01 and compute long-short portfolio weights and the associated portfolio return corresponding to the different combinations of hyperparameter values. Next, we train prediction models via XGBoost using data for 1960:01 to 1970:01 and the different combinations of the hyperparameter values, plug the characteristic values for 1970:01 into the fitted models to generate return forecasts for 1970:02, and compute long-short portfolio weights and the associated portfolio return corresponding to the different combinations of hyperparameter values. We continue in this manner through the end of the validation period and compute Sharpe ratios over the validation period for the long-short portfolio returns corresponding to the different combinations of hyperparameter values. We select the combination of hyperparameter values that produces the highest Sharpe ratio over the validation period. Then,

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<sup>16</sup>For the classification (regression) problem, we use log loss (mean squared error) as the objective function when training the prediction model.

<sup>17</sup>We tune the following XGBoost hyperparameters: “max\_depth,” “reg\_alpha,” “reg\_lambda,” “subsample,” “colsample\_bytree,” “min\_child\_weight”; we set “n\_estimators” to 100. See the [documentation](#) on “XGBoost Parameters” for details on the hyperparameters. Because we tune a large number of hyperparameters and consider a wide grid of values for each, it is extremely computationally expensive to consider all possible combinations of hyperparameter values. Instead of an exhaustive search, we use [Optuna](#) (Akiba et al. 2019), which employs the Tree-structured Parzen Estimator (TPE) algorithm to conduct a smart search. This substantially reduces computational costs while still making it likely that the selected combination of hyperparameter values is nearly optimal.

using the selected combination of hyperparameter values and the 1960:01 to 1972:12 sample, we train the prediction model via XGBoost, plug the 1972:12 characteristic values into the fitted model, and generate the set of return forecasts for the first out-of-sample month (1973:01).

To generate the next set of out-of-sample return forecasts for 1973:02, we use 1960:02 to 1973:01 as the estimation period (so we use a rolling estimation window). We tune the hyperparameters using the walk-forward procedure, with the last 36 months of the estimation period serving as the validation sample. Using the tuned hyperparameters and the 1960:02 to 1973:01 estimation sample, we train the prediction model via XGBoost, plug the 1973:01 characteristic values into the fitted model, and produce the set of return forecasts for 1973:02. Continuing in this fashion, we generate firm-level return forecasts based on the 207 firm characteristics and XGBoost for each month of the forecast evaluation period. We generate return forecasts using both classification and regression prediction models, which we denote by XGBoost(c) and XGBoost(r), respectively. The firm-level monthly return forecasts serve as inputs for constructing the long-short portfolios, as described above. The return forecasts and long-short portfolio weights are based on information available at the time of forecast formation so that there is no “look-ahead” bias in the long-short portfolio returns.

We focus on XGBoost forecasts in the empirical application, which is designed to illustrate the use of the  $SPPC_p$  in analyzing the roles of return predictors in contributing to portfolio performance. In future research, we plan to analyze more exhaustively how return predictors contribute to portfolio performance for forecasts generated using other popular machine learning techniques, such as random forests (Breiman 2001) and deep neural networks. Nevertheless, as shown in Section 3.3, the long-short portfolio based on the XGBoost(c) forecasts exhibits quite impressive performance, so the XGBoost algorithm provides an informative machine learning device for analyzing the contributions of cross-sectional stock return predictors to portfolio performance.

### 3.3. Decomposing Portfolio Performance

Table 2 reports performance metrics for the long-short portfolios based on the XGBoost(c) and XGBoost(r) return forecasts for the 1973:01 to 2021:12 forecast evaluation period. For reference, metrics are also reported for the CRSP value-weighted aggregate market portfolio. The XGBoost(c) portfolio delivers impressive performance overall. Its annualized mean return is 22.58%, while its annualized volatility is 12.53%. These statistics compare to values of 7.44% and 15.86%, respectively, for the market portfolio excess return. The mean and volatility for the XGBoost(c) portfolio translate into an annualized Sharpe ratio of 1.80, which is nearly four times larger than that for the market portfolio (0.47). The maximum drawdown for the XGBoost(c) portfolio is only 15.70%, leading to an annualized Calmar ratio of 1.44. Again, the maximum drawdown and Calmar ratio compare quite favorably to those for the market portfolio (54.36% and 0.14, respectively).

To examine if a long-short portfolio generates a significant risk-adjusted return, we estimate alphas for two leading multifactor models. The first is a six-factor model comprised of the five Fama and French (2015) factors and a momentum factor (FF6).<sup>18</sup> The second is the Hou et al. (2021) augmented q-factor model (Q5), which adds an expected growth factor to the four factors from the original q-factor model (Hou, Xue, and Zhang 2015).<sup>19</sup> The XGBoost(c) portfolio generates economically sizable annualized alphas of 19.45% and 16.29% for the FF6 and Q5 multifactor models, respectively. Both alpha estimates are significant at the 1% level. This indicates that exposures to popular systematic risk factors from the literature cannot account for the average return of the XGBoost(c) portfolio. Indeed, the risk-adjusted average returns (alphas) in the last two columns of Table 2 are reasonably close to the unadjusted average return in the second column for the XGBoost(c) portfolio.

Although the long-short portfolio based on the XGBoost(r) return forecasts outperforms the market portfolio, it does not perform as well as the long-short portfolio based on the XG-

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<sup>18</sup>The factor data for the FF6 model are from Kenneth French’s [Data Library](#).

<sup>19</sup>The factor data for the augmented q-factor model are from Lu Zhang’s [website](#).

**Table 2. Portfolio Performance**

The table reports performance metrics for zero-investment long-short portfolios that invest in available stocks in a given month. The long-short portfolio is constructed by sorting stocks according to their excess return forecasts for the available stocks in a given month based on the XGBoost model in the first column. The excess return forecasts are based on the 207 firm characteristics in Table 1. “XGBoost(c)” (“XGBoost(r)”) is a classification (regression) model. Before forming the portfolio, stocks with market capitalization below the NYSE 20th percentile are dropped. The portfolio based on the XGBoost(c) model goes long (short) stocks predicted to be in the top (bottom) quintile of excess returns; the portfolio based on the XGBoost(r) model goes long (short) the 20% of stocks with the highest (lowest) excess return forecasts. The long and short legs are value weighted. The forecast evaluation period is 1973:01 to 2021:12. “MDD” is the maximum drawdown. “Ann. FF6 alpha” is the annualized alpha for a multifactor model that includes the five Fama and French (2015) factors and a momentum factor. “Ann. Q5 alpha” is the annualized alpha for the Hou et al. (2021) augmented q-factor model;  $t$ -statistics for the alphas are in brackets; \*, \*\*, and \*\*\* indicate significance at the 10%, 5%, and 1% levels, respectively. “Market” is the CRSP value-weighted market portfolio.

| (1)        | (2)       | (3)             | (4)               | (5)    | (6)               | (7)              | (8)              |
|------------|-----------|-----------------|-------------------|--------|-------------------|------------------|------------------|
| Model      | Ann. mean | Ann. volatility | Ann. Sharpe ratio | MDD    | Ann. Calmar ratio | Ann. FF6 alpha   | Ann. Q5 alpha    |
| XGBoost(c) | 22.58%    | 12.53%          | 1.80              | 15.70% | 1.44              | 19.45%<br>[9.82] | 16.29%<br>[6.93] |
| XGBoost(r) | 9.33%     | 13.06%          | 0.71              | 36.12% | 0.26              | 5.02%<br>[2.75]  | 3.15%<br>[1.11]  |
| Market     | 7.44%     | 15.86%          | 0.47              | 54.36% | 0.14              | —                | —                |

Boost(c) return forecasts. The XGBoost(r) portfolio produces an annualized mean return of 9.33%. Together with an annualized volatility of 13.06%, this leads to an annualized Sharpe ratio of 0.71, which is over 50% higher than that for the market portfolio but well below half that for the XGBoost(c) portfolio. The XGBoost(r) portfolio’s maximum drawdown of 36.12% is more than 30% lower (twice as large) than that for the market (XGBoost(c)) portfolio. Accordingly, although the annualized Calmar ratio of 0.26 for the XGBoost(r) portfolio is nearly twice that of the market portfolio, it is only about a fifth of that for the XGBoost(c) portfolio. The XGBoost(r) portfolio provides alphas of 5.02% and 3.15% for the FF6 and Q5 models, respectively; the first is significant at the 1% level, while the second is

insignificant at conventional levels. The alphas for the XGBoost(r) portfolio are well below those for the XGBoost(c) portfolio.

Overall, the results in Table 2 show that XGBoost return forecasts based on the 207 firm characteristics serve as valuable inputs for long-short portfolios. The long-short portfolio constructed using the XGBoost(c) return forecasts that are based on a classification model performs especially well in terms of Sharpe and Calmar ratios as well as risk-adjusted returns in the context of leading multifactor models from the literature. In what follows, we employ the  $SPPC_p$  in Equation (23) to estimate the contributions of each of the 20 predictor groups in Table 1 to the performance metrics for the XGBoost(c) portfolio. Although we focus on decomposing the performance metrics for the XGBoost(c) portfolio, which performs the best, we reiterate that the  $SPPC_p$  can be used to decompose the performance of any portfolio constructed from return forecasts based on a set of predictors. If a portfolio performs poorly, our method can identify the predictors that are primarily responsible for the subpar performance.

It is perhaps not surprising that the XGBoost(c) model works better for constructing the long-short portfolio than the XGBoost(r) model. XGBoost(c) is a classification model, and forming the long-short portfolio also entails classification, as the portfolio goes long (short) the 20% of stocks with the highest (lowest) expected returns. Of course, we need return forecasts based on a regression model in some situations, such as constructing mean-variance optimal portfolios. Again, the  $SPPC_p$  can be used to estimate the contributions of the return predictors to portfolio performance in this context.

Next, we use the  $SPPC_p$  in Equation (23) to estimate the contributions of each of the 20 predictor groups for the XGBoost(c) portfolio to the performance metrics in Table 2. As discussed in Section 2.2, to operationalize our method, we need to select the return corresponding to the empty coalition set, which serves as a baseline. For the average return, volatility, Sharpe ratio, maximum drawdown, and Calmar ratio, a natural baseline is the excess return for the CRSP value-weighted market portfolio. If an investor does not have

access to any predictors (the empty coalition set), it seems reasonable to simply hold the market portfolio, so we estimate the contribution of each predictor group to the metrics in the second through sixth columns for the XGBoost(c) portfolio in terms of the deviation from the market portfolio. When measuring the contributions of the predictor groups to the multifactor alphas, an appropriate economic baseline is zero. This is the risk-adjusted return that we expect when the factors adequately capture the main sources of systematic risk in the economy, so the predictors do not add economic value.

Table 3 reports the contributions of the 20 predictor groups for the performance metrics for the XGBoost(c) portfolio. The top four contributions for each metric in terms of improving portfolio performance are in bold. According to the local accuracy property in Equation (24), the baseline contribution and those of the 20 predictor groups sum to the total in the last row of Table 3 (apart from rounding), where the last row equals the corresponding value for the XGBoost(c) portfolio in Table 2.

Beginning with the mean return in Table 3, the baseline value for the market portfolio is 7.44%. Since the mean return for the XGBoost(c) portfolio is 22.58%, the 20 predictor groups together increase the average return by 15.14 percentage points. The top four predictor groups are *Risk*, *Momentum*, *Earnings*, and *Seasonal momentum*, with contributions of 4.82, 4.50, 2.50, and 1.58 percentage points, respectively. These four groups collectively contribute to an increase in the average return of 13.40 percentage points, which is nearly 90% of the increase provided by the XGBoost(c) portfolio. Other groups making contributions above 0.50 percentage points are *Lead lag*, *Investment*, *Profitability*, and *Earnings forecast* (1.13, 1.13, 0.97, and 0.89 percentage points, respectively). A handful of groups make sizable negative contributions to the average return, including *Reversal*, *Ownership*, *Volume*, and *Sales* (−1.66, −0.96, −0.70, and −0.50 percentage points, respectively). With respect to volatility, the XGBoost(c) portfolio lowers it by 3.33 percentage points vis-à-vis the market portfolio. The largest contributors to the reduction in volatility are *Valuation ratio*, *Volume*,

**Table 3. Portfolio Performance Contributions**

The table reports the contributions of the 20 predictor groups to the performance metrics in Table 2 for the long-short portfolio based on the XGBoost(c) return forecasts. The contributions are estimated using the  $SPPC_p$  in Equation (23). Table 1 lists the individual firm characteristics in each of the 20 predictor groups. The forecast evaluation period is 1973:01 to 2021:12. The numbers in a column may not add to the value in the “Total” row due to rounding; 0.00 indicates less than 0.005 in absolute value. The top four contributions for each metric in terms of improving portfolio performance are in bold.

| (1)               | (2)         | (3)          | (4)               | (5)          | (6)               | (7)            | (8)           |
|-------------------|-------------|--------------|-------------------|--------------|-------------------|----------------|---------------|
| Predictor group   | Ann. mean   | Ann. vol.    | Ann. Sharpe ratio | MDD          | Ann. Calmar ratio | Ann. FF6 alpha | Ann. Q5 alpha |
| Baseline          | 7.44%       | 15.86%       | 0.47              | 54.36%       | 0.14              | 0%             | 0%            |
| Risk              | <b>4.82</b> | -0.16        | <b>0.35</b>       | -3.03        | <b>0.24</b>       | <b>4.34</b>    | <b>4.29</b>   |
| Earnings          | <b>2.50</b> | -0.29        | <b>0.20</b>       | -3.54        | 0.10              | <b>2.72</b>    | <b>2.02</b>   |
| Seasonal momentum | <b>1.58</b> | <b>-0.85</b> | <b>0.16</b>       | <b>-7.72</b> | <b>0.14</b>       | <b>2.38</b>    | <b>2.49</b>   |
| Momentum          | <b>4.50</b> | 2.34         | <b>0.15</b>       | 4.58         | 0.08              | <b>3.25</b>    | <b>2.16</b>   |
| Lead lag          | 1.13        | -0.52        | 0.10              | -3.85        | 0.06              | 0.95           | 0.57          |
| Investment        | 1.13        | -0.26        | 0.10              | <b>-6.78</b> | 0.11              | 1.70           | 0.95          |
| Valuation ratio   | 0.28        | <b>-1.24</b> | 0.09              | <b>-6.63</b> | <b>0.15</b>       | 0.38           | 0.58          |
| Risk alt          | 0.48        | -0.63        | 0.09              | <b>-7.09</b> | <b>0.17</b>       | 1.27           | 0.76          |
| Profitability     | 0.97        | -0.35        | 0.06              | -3.38        | 0.07              | 0.61           | -0.88         |
| Earnings forecast | 0.89        | 0.26         | 0.05              | 0.76         | 0.04              | 0.85           | 0.92          |
| Valuation         | 0.04        | <b>-1.06</b> | 0.05              | -3.73        | 0.02              | 0.77           | 0.48          |
| Financing         | 0.21        | 0.02         | 0.02              | -0.12        | 0.02              | 0.14           | 0.29          |
| Financing alt     | 0.25        | -0.09        | 0.02              | -0.69        | 0.02              | 0.70           | 0.29          |
| Volume            | -0.70       | <b>-1.18</b> | 0.02              | -3.17        | 0.04              | -0.43          | 0.17          |
| Liquidity         | 0.18        | 1.26         | 0.02              | 3.47         | 0.08              | -0.19          | 0.35          |
| Investment alt    | -0.06       | 0.06         | 0.00              | -1.78        | 0.02              | 0.15           | 0.08          |
| R&D               | 0.06        | 0.07         | 0.00              | -0.87        | 0.00              | 0.42           | -0.03         |
| Reversal          | -1.66       | -0.38        | -0.03             | 3.11         | -0.02             | -0.32          | 1.46          |
| Sales             | -0.50       | 0.00         | -0.04             | 1.01         | -0.02             | -0.18          | -0.65         |
| Ownership         | -0.96       | -0.32        | -0.06             | 0.79         | -0.03             | -0.09          | -0.01         |
| Total             | 22.58%      | 12.53%       | 1.80              | 15.70%       | 1.44              | 19.45%         | 16.29%        |

*Valuation*, and *Seasonal Momentum* (-1.24, -1.18, -1.06, and -0.85 percentage points, respectively).

In terms of the Sharpe ratio in Table 3, the baseline value for the market portfolio is 0.47. Since the Sharpe ratio for the XGBoost(c) portfolio is 1.80, the 20 predictor groups



together increase the Sharpe ratio by a sizable 1.33. The top four predictor groups are *Risk*, *Earnings*, *Seasonal momentum*, and *Momentum*, with contributions of 0.35, 0.20, 0.16, and 0.15, respectively. These four groups collectively contribute to an increase in the Sharpe ratio of 0.86 or 65% of the total increase. The remaining predictor groups can be divided into three categories. First, there are groups making smaller but still noteworthy contributions in the range of 0.05 to 0.10, led by *Lead lag* and *Investment*, both with contributions of 0.10. Second, a set of groups makes minor contributions of essentially zero to 0.02. Third, three groups that contributed negatively to the average return—*Reversal*, *Sales*, and *Ownership*—also make negative contributions to the Sharpe ratio (−0.03, −0.04, and −0.06, respectively).

The XGBoost(c) portfolio reduces the maximum drawdown for the market portfolio from 54.36% all the way to 15.70%, a substantive reduction of 38.66 percentage points. The groups most responsible for the decrease include *Seasonal momentum*, *Risk alt*, *Investment*, and *Valuation ratio*, with contributions of −7.72, −7.09, −6.78, and −6.63 percentage points, respectively. Other groups lowering the maximum drawdown by more than three percentage points are *Lead lag*, *Valuation*, *Earnings*, *Profitability*, *Volume*, and *Risk* (−3.85, −3.73, −3.54, −3.38, −3.17, and −3.03 percentage points, respectively).

The results for the Calmar ratio are broadly similar to those for the Sharpe ratio. The XGBoost(c) portfolio increases the Calmar ratio from 0.14 for the market portfolio to 1.44, a substantial increase of 1.30. *Risk* is the predictor group that makes the largest contribution (0.24) to the increase in the performance metric. In addition to *Risk*, groups making contributions of 0.10 or more include *Risk alt*, *Valuation ratio*, *Seasonal momentum*, *Investment*, and *Earnings* (0.17, 0.15, 0.14, 0.11, and 0.10, respectively). Like the Sharpe ratio, *Reversal*, *Sales*, and *Ownership* make negative contributions (−0.02, −0.02, and −0.03, respectively).

Turning to the alphas for the FF6 and Q5 multifactor models in Table 3, the top four predictor groups in terms of contributions to the Sharpe ratio are also the top four in terms of contributions to the FF6 and Q5 alphas. For the FF6 model, *Risk*, *Momentum*, *Earnings*, and *Seasonal momentum* contribute 4.34, 3.25, 2.72, and 2.38 percentage points, respectively,

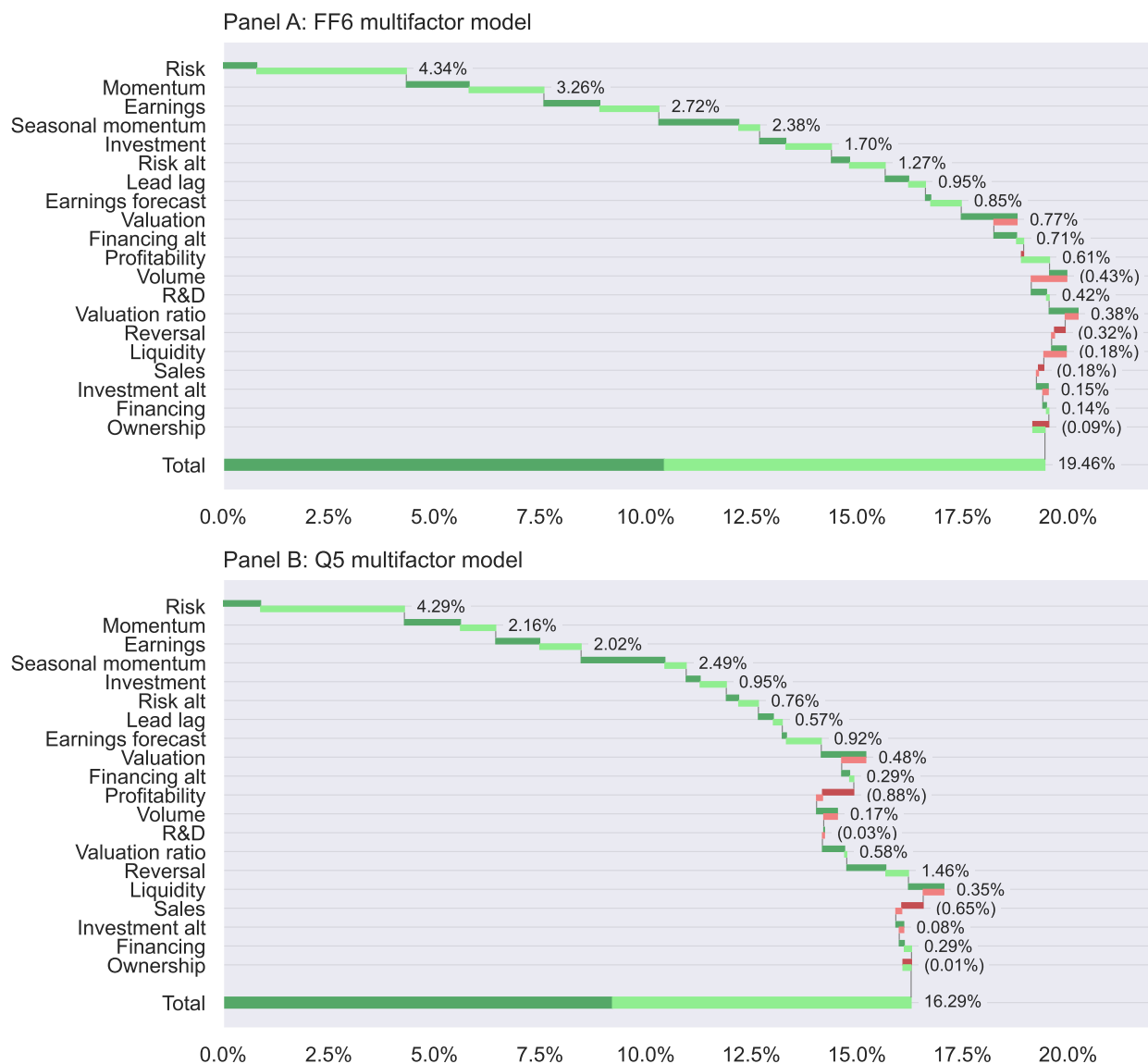
to alpha, which accounts for 12.69 percentage points of the total alpha for the XGBoost(c) portfolio of 19.45%. Other groups contributing more than 50 basis points include *Investment*, *Risk alt*, *Lead lag*, *Earnings forecast*, *Valuation*, *Financing alt*, and *Profitability* (1.70, 1.27, 0.95, 0.85, 0.77, 0.70, and 0.61 percentage points, respectively). *Reversal*, *Sales*, and *Ownership* continue to make negative contributions (−0.32, −0.18, and −0.09 percentage points, respectively), along with *Volume* and *Liquidity* (−0.43 and −0.19 percentage points, respectively).

For the Q5 model, *Risk*, *Seasonal momentum*, *Momentum*, and *Earnings* provide contributions of 4.29, 2.49, 2.16, and 2.02 percentage points, respectively, to alpha. These contributions comprise 10.96 percentage points of the total alpha of 16.29%. Other noteworthy contributions in excess of 50 basis points are made by *Investment*, *Earnings forecast*, *Risk alt*, *Valuation ratio*, and *Lead lag* (0.95, 0.92, 0.76, 0.58, and 0.57 percentage points, respectively). *Sales* and *Ownership* again make negative contributions (−0.65 and −0.01 percentage points, respectively), as do *Profitability* and *R&D* (−0.88 and −0.03 percentage points, respectively).

Overall, the  $SPPC_p$  values reported in Table 3 enable us to identify the predictor groups that are primarily responsible for the strong performance of the XGBoost(c) portfolio according to the metrics reported in Table 2. Four groups—*Risk*, *Earnings*, *Seasonal momentum*, and *Momentum*—stand out in Table 3 as leading contributors to the economic value provided by cross-sectional return predictability. These groups make the largest contributions to the Sharpe and Calmar ratios as well as the alphas for the FF6 and Q5 multifactor models. There are also groups that consistently detract from portfolio performance, especially *Sales* and *Ownership*.

It is interesting to note that the leading predictor groups often contain variables that are used to construct factors via sorting that appear in the FF6 and Q5 models. Nevertheless, the XGBoost(c) portfolio generates large alphas in the context of both models. This indicates that XGBoost(c) processes the information in cross-sectional return predictors in a manner

that differs substantially from the construction of factors in leading multifactor models to produce substantive economic value.



**Figure 1. Alpha Long- and Short-Leg Contributions**

Each panel depicts a waterfall diagram with each predictor group’s contribution to alpha for the long-short portfolio based on the XGBoost(c) return forecasts in terms of the long and short legs. The contributions are estimated using the  $SPPC_p$  in Equation (23). The dark (light) green segments are the positive contributions of the long (short) leg; the dark (light) red segments are the negative contributions of the long (short) leg. Panel A (B) reports results for the FF6 (Q5) multifactor model. The numbers correspond to the contributions of the long and short legs together reported in the last two columns of Table 3; parentheses indicate a negative number.

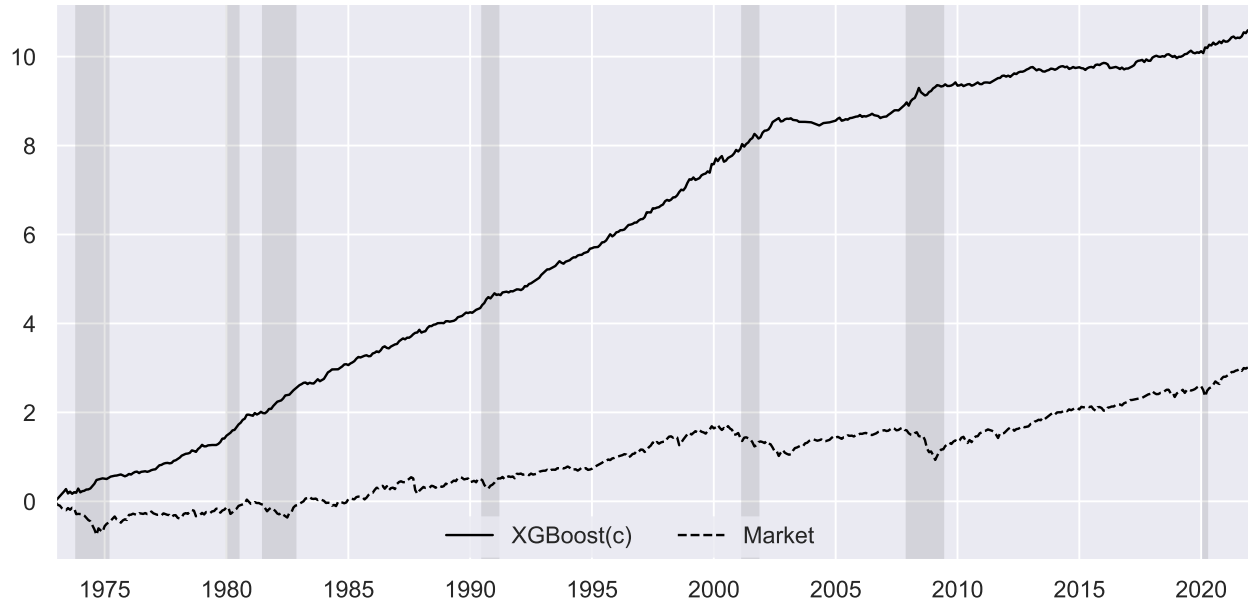
Researchers are often interested in how the long and short legs separately affect the performance of long-short portfolios. We can use the  $SPPC_p$  to address this issue. As an example, Figure 1 presents waterfall diagrams depicting the contributions of the predictor groups to the long and short legs of the long-short portfolio based on the XGBoost(c) return forecasts for the FF6 and Q5 multifactor model alphas. The diagram includes the group contributions to the alphas reported in the last two columns of Table 3, with negative numbers in parentheses. Panel A (B) reports results for the FF6 (Q5) model. The dark (light) green segments are the positive contributions to the risk-adjusted return on the long (short) leg<sup>20</sup>; the dark (light) red segments are the negative contributions to the risk-adjusted return on the long (short) leg. The base of the waterfall shows the total contributions of the long and short legs to the alpha. For both multifactor models, the long and short legs contribute approximately equally to the long-short portfolio alpha.

There are interesting contrasts in the contributions of predictor groups across the long and short legs. Consider, for example, *Risk*, which makes the largest contributions to the long-short portfolio alpha for both models. In both cases, the contribution of *Risk* to the alpha is considerably larger for the short leg. Other groups whose short-leg contributions are substantially larger than their long-leg contributions for both models include *Investment* and *Earnings forecast*. In contrast, the long-leg contributions are relatively large for *Seasonal momentum*. For *Momentum* and *Earnings*, two of the leading predictor groups for both models, the groups' long- and short-leg contributions are fairly similar.

To this point, we have computed predictor group contributions for long-short portfolio performance metrics over the full 1973:01 to 2021:12 forecast evaluation period. The  $SPPC_p$  can be used to estimate predictor contributions for any subsample of interest. To provide motivation for subsample analysis, Figure 2 shows the cumulative log return for the XGBoost(c) portfolio for the full 1973:01 to 2021:12 out-of-sample period. For reference, the cumulative log excess return for the market portfolio is also shown. The XGBoost(c)

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<sup>20</sup>We use the negative of the return on the short leg, as this represents a positive contribution to the long-short portfolio alpha.



**Figure 2. Cumulative Log Returns**

The figure depicts the cumulative log return for the long-short portfolio based on the XGBoost(c) return forecasts and the cumulative log excess return for the CRSP value-weighted market portfolio. Vertical bars indicate business-cycle recessions as dated by the National Bureau of Economic Research.

portfolio performs especially well through approximately 2002, after which it “flattens out” to an extent.<sup>21</sup> The XGBoost(c) portfolio performs considerably better than the market portfolio during business-cycle recessions throughout the entire 1973:01 to 2021:12 forecast evaluation period. After 2002, the XGboost(c) portfolio continues to perform particularly well during recessions—especially the Great Recession—but its performance is less impressive during expansions *via-à-vis* the pre-2003 period. Investor learning about cross-sectional return predictability from academic studies (McLean and Pontiff 2016) provides at least a partial potential explanation for the decrease in performance for the XGBoost(c) portfolio during the second subsample.

Table 4 provides additional information on differences in long-short portfolio performance over time by reporting the performance metrics from Table 2 for the 1973:01 to 2002:12 and 2003:01 to 2021:12 subsamples. Panel A (B) of Table 4 provides results for the XGBoost(c)

<sup>21</sup>Green, Hand, and Zhang (2017) make a similar finding for a long-short portfolio constructed from sorted return forecasts generated using linear Fama and MacBeth (1973) regressions based on 94 firm characteristics.

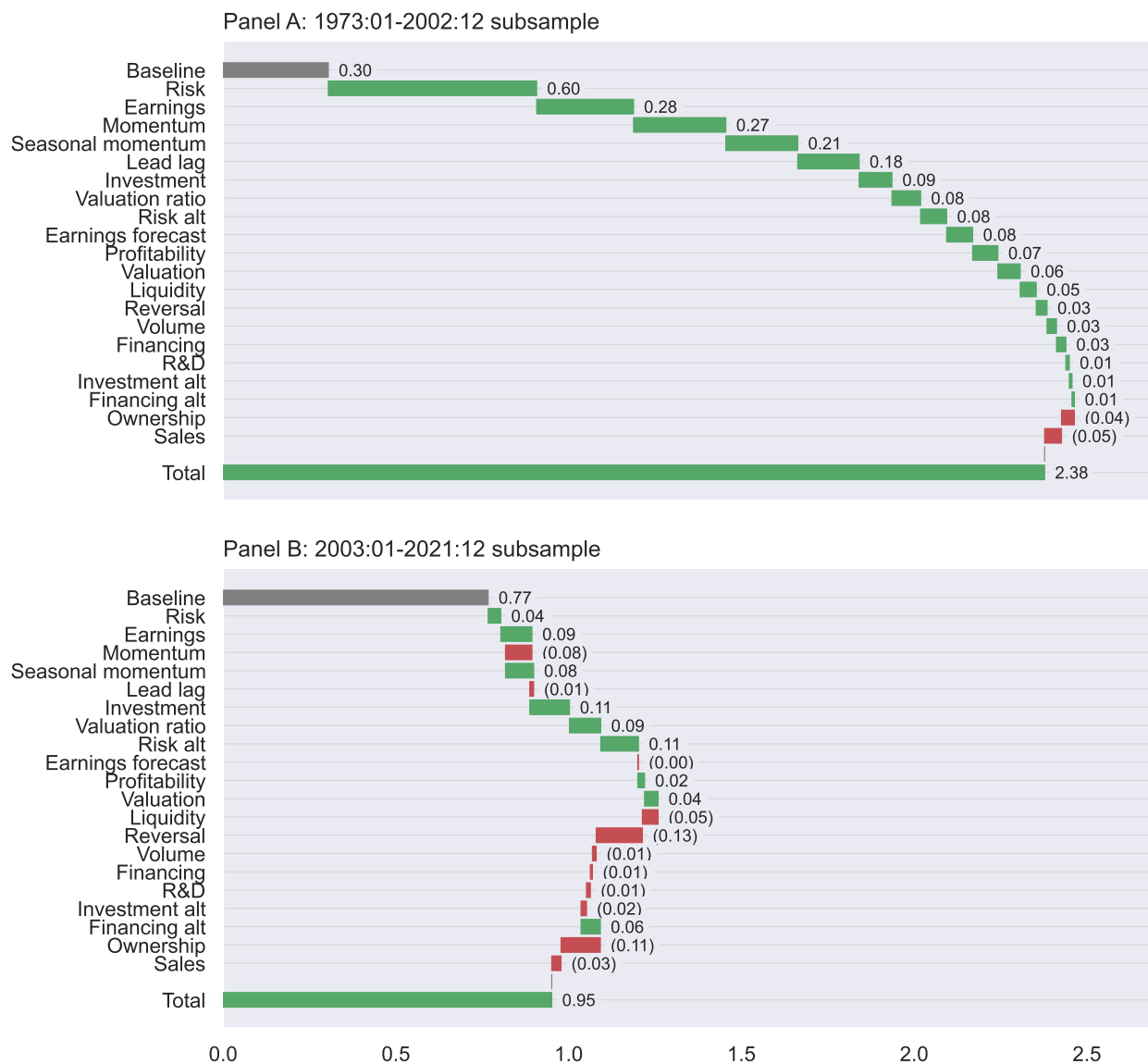
**Table 4. Portfolio Performance for Subsamples**

Panel A reports performance metrics from Table 2 for the long-short portfolio based on the XGBoost(c) return forecasts for the 1973:01 to 2002:12 and 2003:01 to 2021:12 subsamples. “MDD” is the maximum drawdown. “Ann. FF6 alpha” is the annualized alpha for a multifactor model that includes the five Fama and French (2015) factors and a momentum factor. “Ann. Q5 alpha” is the annualized alpha for the Hou et al. (2021) augmented q-factor model;  $t$ -statistics for the alphas are in parentheses; \*, \*\*, and \*\*\* indicate significance at the 10%, 5%, and 1% levels, respectively. “Market portfolio” in Panel B is the CRSP value-weighted market portfolio.

| (1)                                  | (2)       | (3)             | (4)               | (5)    | (6)               | (7)               | (8)              |
|--------------------------------------|-----------|-----------------|-------------------|--------|-------------------|-------------------|------------------|
| Subsample                            | Ann. mean | Ann. volatility | Ann. Sharpe ratio | MDD    | Ann. Calmar ratio | Ann. FF6 alpha    | Ann. Q5 alpha    |
| <b>Panel A: XGBoost(c) portfolio</b> |           |                 |                   |        |                   |                   |                  |
| 1973:01–2002:12                      | 29.74%    | 12.51%          | 2.38              | 12.06% | 2.47              | 24.54%<br>[11.51] | 22.25%<br>[7.66] |
| 2003:01–2021:12                      | 11.29%    | 11.86%          | 0.95              | 15.70% | 0.72              | 9.68%<br>[3.93]   | 8.53%<br>[2.73]  |
| <b>Panel B: Market portfolio</b>     |           |                 |                   |        |                   |                   |                  |
| 1973:01–2002:12                      | 5.04%     | 16.56%          | 0.30              | 51.43% | 0.10              | –                 | –                |
| 2003:01–2021:12                      | 11.23%    | 14.63%          | 0.77              | 51.51% | 0.22              | –                 | –                |

(market) portfolio. According to the different metrics, the performance of the XGBoost(c) portfolio generally declines from the first to the second subsample, in line with Figure 2. The annualized average return for the XGBoost(c) portfolio falls from 29.74% in the first subsample to 11.29% in the second. With limited changes in volatility and the maximum drawdown over the subsamples, the annualized Sharpe (Calmar) ratio declines from 2.38 to 0.95 (2.47 to 0.72). The average return, Sharpe ratio, and Calmar ratio increase for the market portfolio from the first subsample to the second, but they remain below those for the XGBoost(c) portfolio for both subsamples. Stark differences remain in the maximum drawdown between the XGBoost(c) and market portfolios for the two subsamples, with values of 12.06% and 15.70% (51.43% and 51.51%) for the former (latter) for the first and second subsamples, respectively. The annualized alphas for the XGBoost(c) portfolio fall from 24.54% to 9.68% (22.25% to 8.53%) from the first subsample to the second for the FF6

(Q5) model; nevertheless, the alphas remain economically sizable and statistically significant at the 1% level for both models for the second subsample.



**Figure 3. Sharpe Ratio Contributions for Subsamples**

Each panel depicts a waterfall diagram with each predictor group’s contribution to the Sharpe ratio for the long-short portfolio based on the XGBoost(c) return forecasts. The contributions are estimated using the  $SPPC_p$  in Equation (23). Panel A (B) reports results for the 1973:01 to 2002:12 (2003:01 to 2021:21) subsample. Parentheses indicate a negative number.

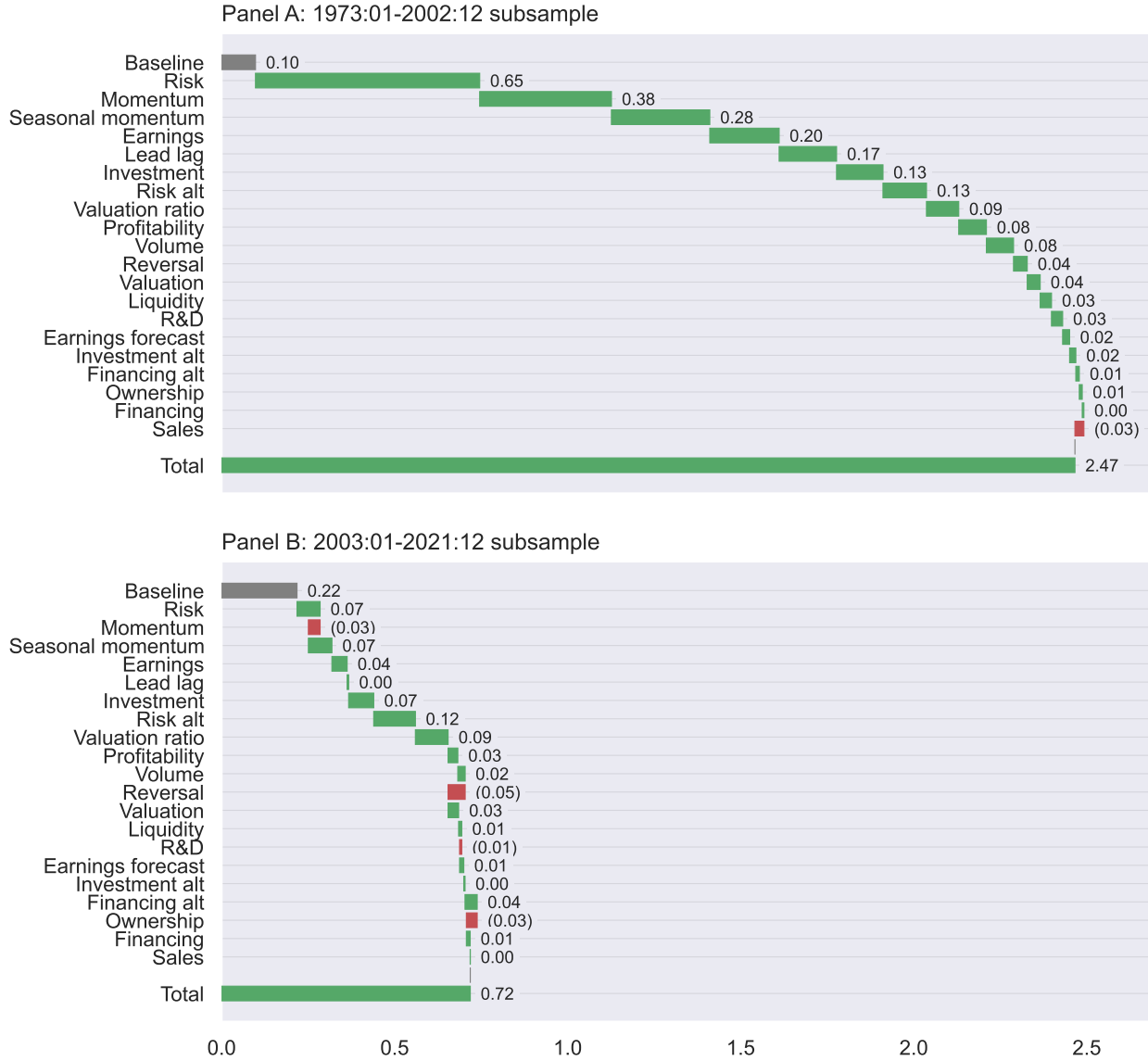
Overall, Figure 2 and Table 4 indicate that the performance of the XGBoost(c) portfolio deteriorates to a degree from the 1973:01 to 2002:12 to the 2003:01 to 2021:12 subsample but that it continues to outperform the market portfolio and deliver sizable alphas. Next, we use

the  $SPPC_p$ , to estimate the contributions of the predictor groups to the performance metrics for the two subsamples. Figure 3 provides waterfall diagrams showing the contributions of the groups to the Sharpe ratio, with the market portfolio continuing to serve as the benchmark. For the 1973:01 to 2002:12 subsample in Panel A, 18 of the 20 groups increase the Sharpe ratio for the XGBoost(c) portfolio relative to that for the market portfolio; the two exceptions are *Ownership* and *Sales*. *Risk* makes the largest contribution of 0.60, which is twice as large as the Sharpe ratio for the baseline market portfolio (0.30). Other groups making contributions above 0.20 in the first subsample include *Earnings*, *Momentum*, and *Seasonal momentum* (0.28, 0.27, and 0.21, respectively).

The contributions of the predictor groups often change markedly for the 2003:01 to 2021:12 subsample in Panel B. The baseline Sharpe ratio for the market portfolio increases to 0.77, while the Sharpe ratio for the XGBoost(c) portfolio is 0.95, so the contributions sum to 0.18. Nine (eleven) of the groups contribute positively (negatively) to the Sharpe ratio. The contribution of *Risk* falls from 0.60 in Panel A to 0.04 in Panel B. The contribution of *Momentum* goes from sizably positive (0.27) to negative ( $-0.08$ ) as we move from Panel A to B. Despite making a positive contribution (0.05) in Panel A, *Reversal* reverses to making the largest negative contribution ( $-0.13$ ) in Panel B.

Figure 4 is an analogous version of Figure 3 for the Calmar ratio. The overall story is similar, although many more of the predictor groups (17 out of 20) make a positive contribution in the second subsample in Figure 4. For the first subsample, *Risk*, *Momentum*, *Seasonal momentum*, and *Earnings* make contributions that are twice as large or larger than the Calmar ratio for the baseline market portfolio (0.10). With the exception of *Sales*, all of the groups contribute positively to the Calmar ratio in Panel A. The Calmar ratio for the baseline market portfolio increases to 0.22 in the second subsample; given the Calmar ratio of 0.72 for the XGBoost(c) portfolio for the second subsample, the total contribution of the groups is 0.50 (while it is 2.37 for the first subsample). As in Figure 3, *Momentum* goes from making a sizably positive contribution (0.38) in Panel A of Figure 4 to a negative



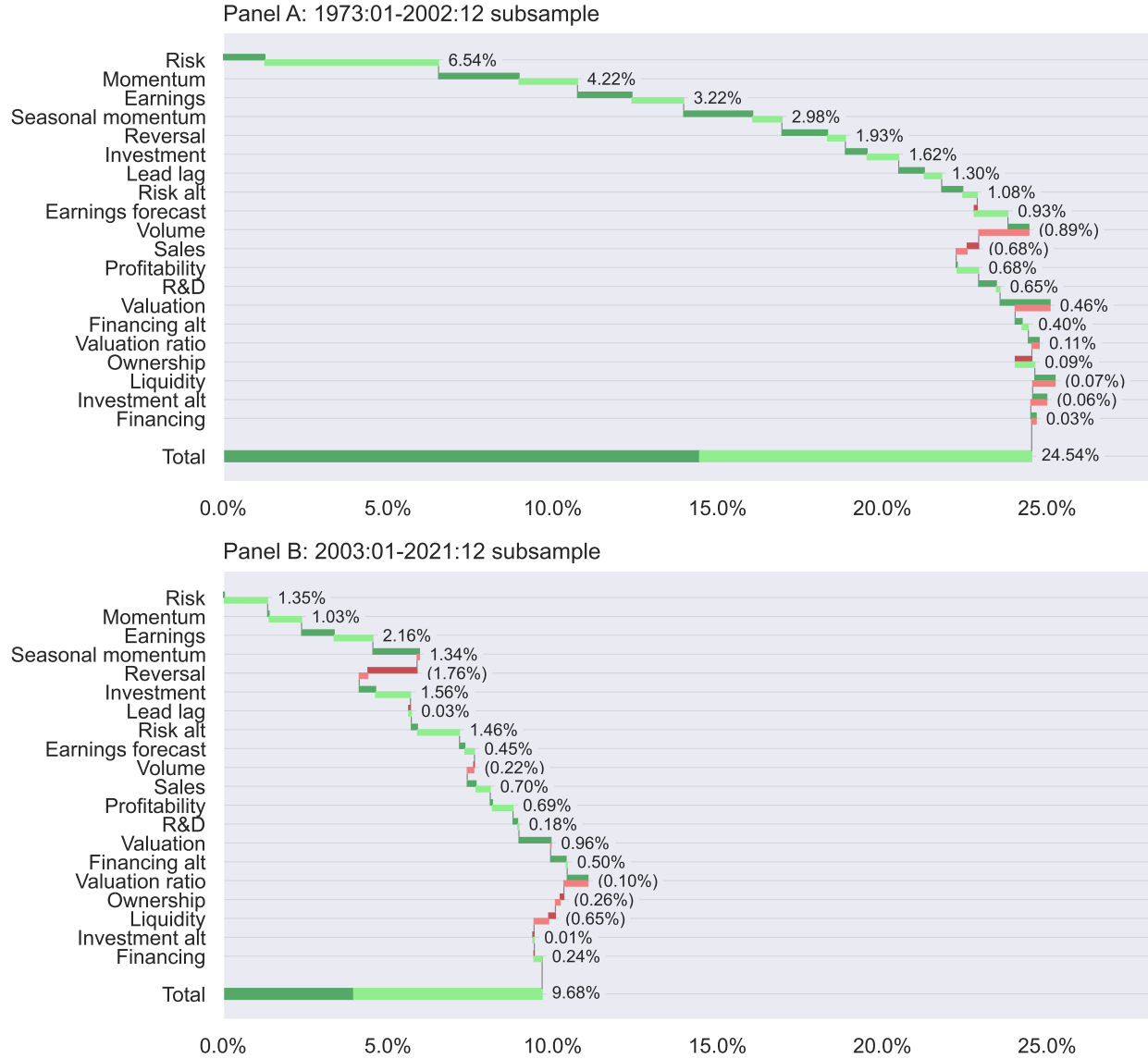


**Figure 4. Calmar Ratio Contributions for Subsamples**

Each panel depicts a waterfall diagram with each predictor group’s contribution to the Calmar ratio for the long-short portfolio based on the XGBoost(c) return forecasts. The contributions are estimated using the  $SPPC_p$  in Equation (23). Panel A (B) reports results for the 1973:01 to 2002:12 (2003:01 to 2021:21) subsample. Parentheses indicate a negative number.

contribution ( $-0.03$ ) in Panel B, and *Reversal* goes from making a positive contribution (0.04) in Panel A to the largest negative contribution ( $-0.05$ ) in Panel B.

Figures 5 and 6 report analogous results to Figure 1 in terms of the contributions to the multifactor alphas for the two subsamples. With respect to the alpha for the FF6 model in Figure 5, the results for the first subsample in Panel A are similar to those for



**Figure 5. FF6 Alpha Long- and Short-Leg Contributions for Subsamples**

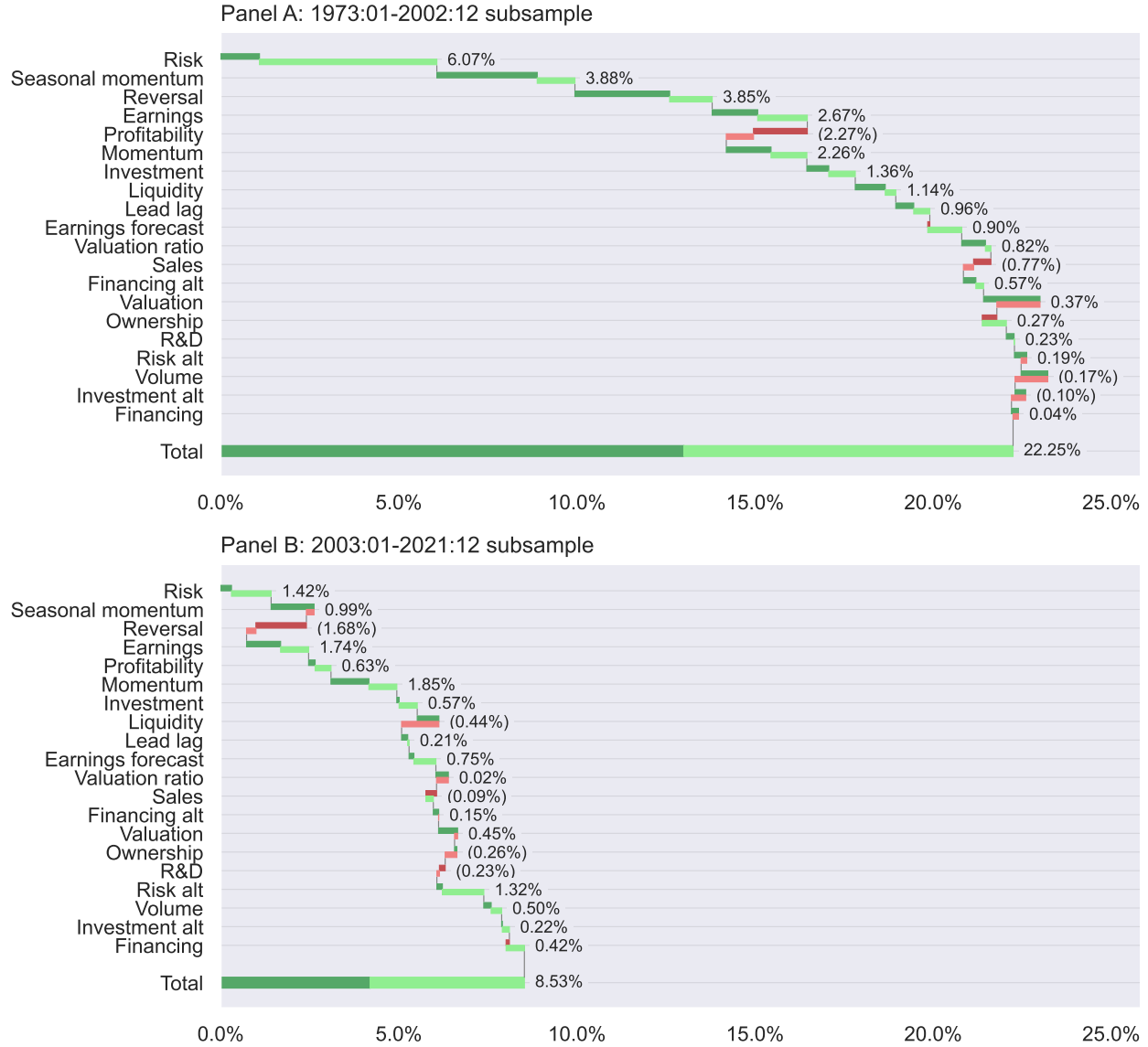
Each panel depicts a waterfall diagram with each predictor group’s contribution to alpha for the long-short portfolio based on the XGBoost(c) return forecasts in terms of the long and short legs. The contributions are estimated using the  $SPPC_p$  in Equation (23). Alpha is measured in the context of the FF6 multifactor model. The dark (light) green segments are the positive contributions of the long (short) leg; the dark (light) red segments are the negative contributions of the long (short) leg. Panel A (B) reports results for the 1973:01 to 2002:12 (2003:01 to 2021:21) subsample. Parentheses indicate a negative number.

the full forecast evaluation period in Panel A of Figure 1. *Risk*, *Momentum*, *Earnings*, and *Seasonal momentum* make sizable contributions in the first subsample in Figure 5, with the contribution of *Risk* falling predominantly on the short leg, while the contributions of the

other groups are more evenly distributed across the long and short legs. The alpha falls from 24.54% to 9.68% from the first to the second subsample. *Risk*, *Momentum*, *Earnings*, and *Seasonal momentum* continue to make positive contributions, but their magnitudes are reduced. As with the Sharpe and Calmar ratios over the subsamples, *Reversal* evinces a reversal of its own, making a contribution of 1.93 percentage points in the first subsample (primarily via the long leg), which subsequently falls to  $-1.76$  percentage points in the second subsample (again primarily via the long leg).

The subsample results in Figure 6 for the alpha for the Q5 model are broadly similar to those in Figure 5 for the FF6 model. *Reversal* exhibits an even stronger reversal in Figure 6 as we move from the first to the second subsample. Its contribution is a substantive 3.85 percentage points in the first subsample but falls to  $-1.68$  percentage points in the second (both effects are primarily concentrated in the long leg). *Liquidity* also exhibits a marked turnaround in its contributions across the subsamples, going from a positive contribution of 1.14 percentage points in the first subsample to a negative contribution of  $-0.44$  percentage points in the second.

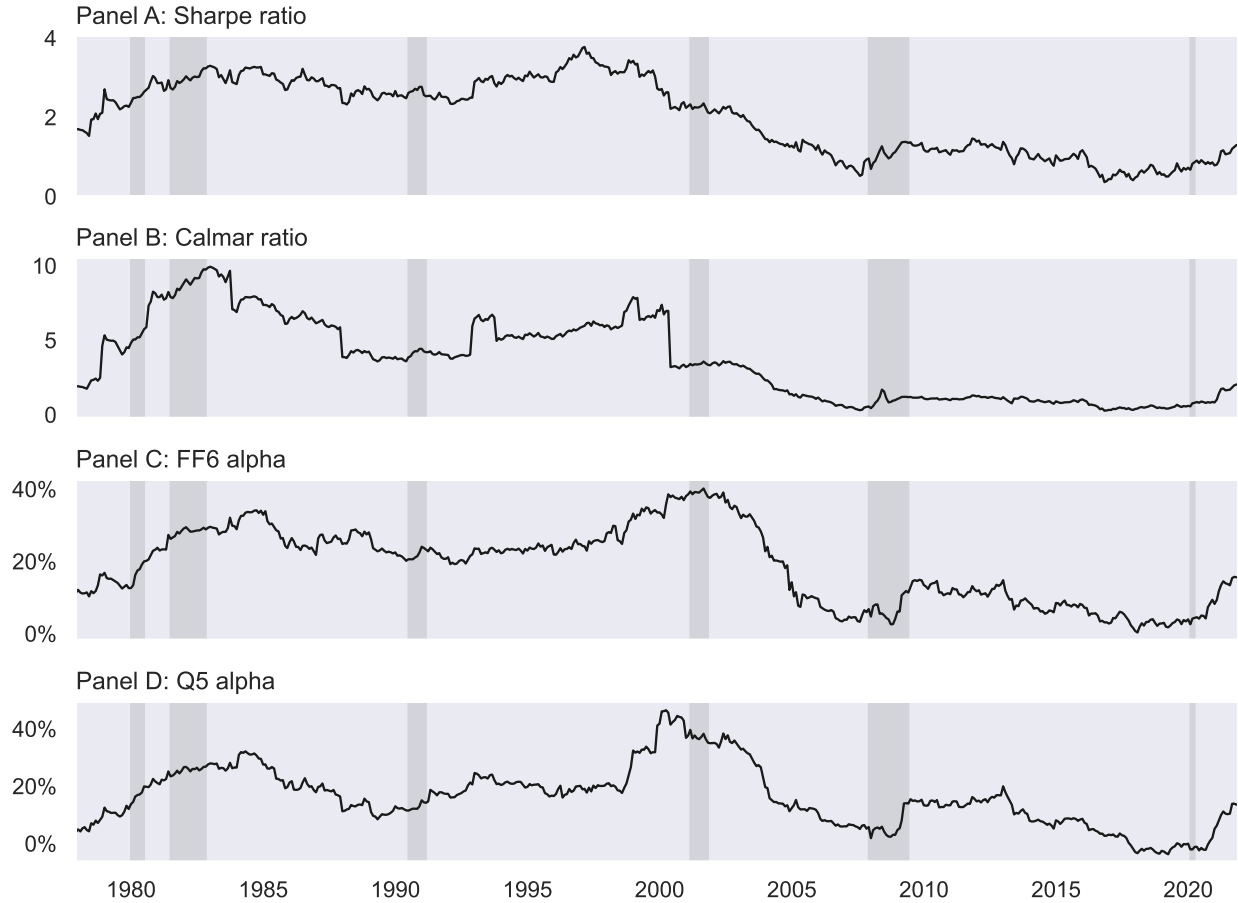
Table 4 and Figures 3 to 6 investigate changes in portfolio performance and the predictor group contributions by dividing the full forecast evaluation period into non-overlapping subsamples. Another popular strategy for examining how results change over time is the use of rolling windows of data over the forecast evaluation period. Again, the  $SPPC_p$  can be employed in this context. We compute performance metrics for the XGBoost(c) portfolio using 60-month rolling windows and then estimate the predictor group contributions via the  $SPPC_p$  for the rolling windows. Figure 7 displays the sequences of Sharpe and Calmar ratios as well as FF6 and Q5 alphas computed using the rolling windows. The performance metrics tend to fall when data beyond 2002 are included in the window. In addition, there is a tendency for the metrics to increase when the windows incorporate data from recessions. This is clearly evident for the Sharpe ratio and the alphas around the Great Recession. The



**Figure 6. Q5 Alpha Long- and Short-Leg Contributions for Subsamples**

Each panel depicts a waterfall diagram with each predictor group’s contribution to alpha for the long-short portfolio based on the XGBoost(c) return forecasts in terms of the long and short legs. The contributions are estimated using the  $SPPC_p$  in Equation (23). Alpha is measured in the context of the Q5 multifactor model. The dark (light) green segments are the positive contributions of the long (short) leg; the dark (light) red segments are the negative contributions of the long (short) leg. Panel A (B) reports results for the 1973:01 to 2002:12 (2003:01 to 2021:21) subsample. Parentheses indicate a negative number.

performance metrics also markedly increase for windows that include data near the end of the sample, corresponding to the advent of the COVID-19 crisis.

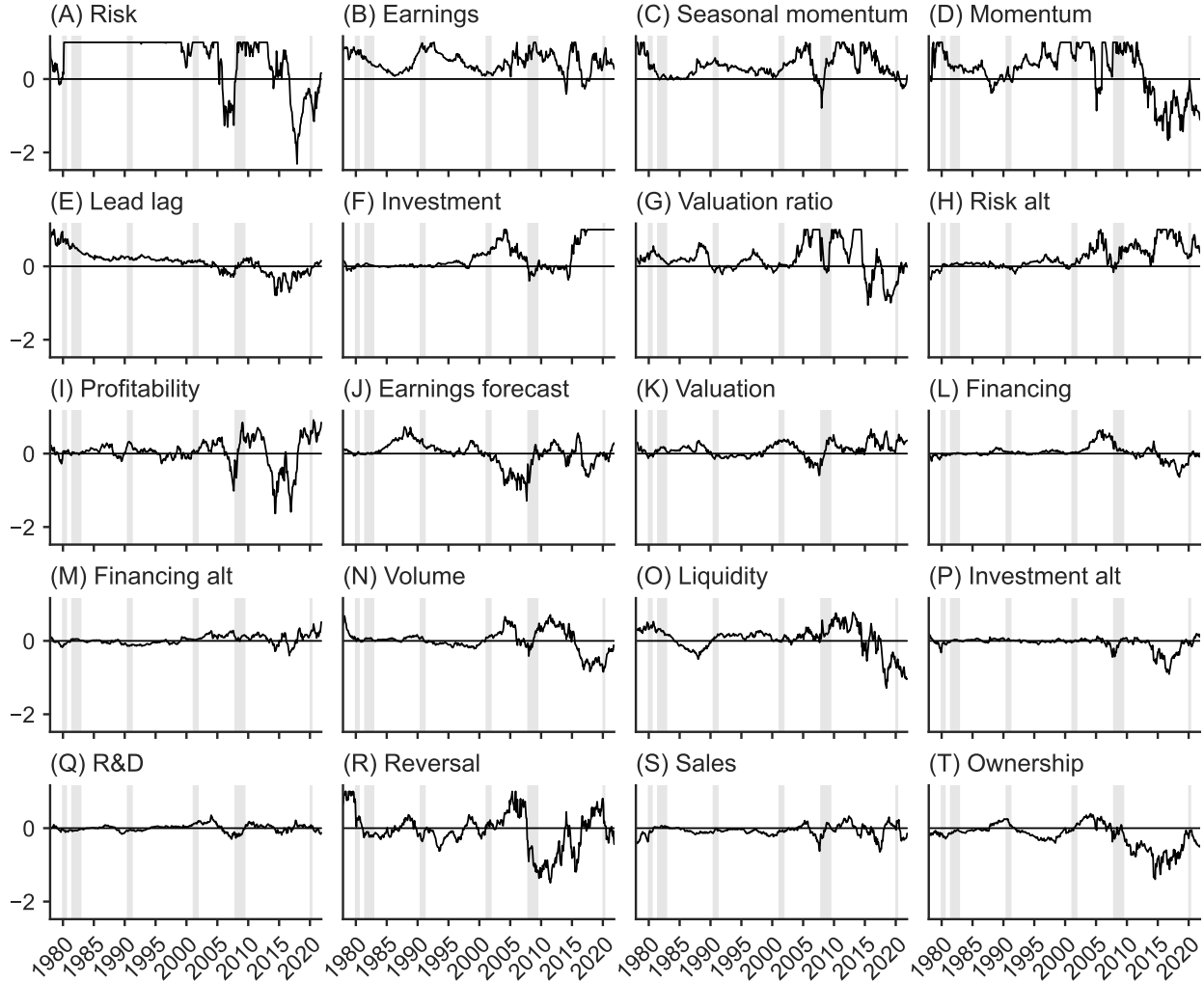


**Figure 7. Portfolio Performance for 60-Month Rolling Windows**

Each panel depicts the performance metric in the panel heading for the long-short portfolio based on the XGBoost(c) return forecasts. The metrics are computed using 60-month rolling windows over the 1973:01 to 2021:12 forecast evaluation period. The horizontal axis corresponds to the end of the 60-month rolling window. Vertical bars indicate business-cycle recessions as dated by the National Bureau of Economic Research.

Figures 8 and 9 depict the contributions of the 20 predictor groups to the Sharpe and Calmar ratios, respectively, computed for the 60-month rolling windows. For a given window, we standardize the contributions by the maximum group contribution for that window.<sup>22</sup> The results in Figures 8 and 9 are similar and reveal noteworthy patterns in the group contributions over time. For example, *Risk* and *Momentum* frequently make among the largest contributions for windows ending through the early 2000s, while they subsequently often

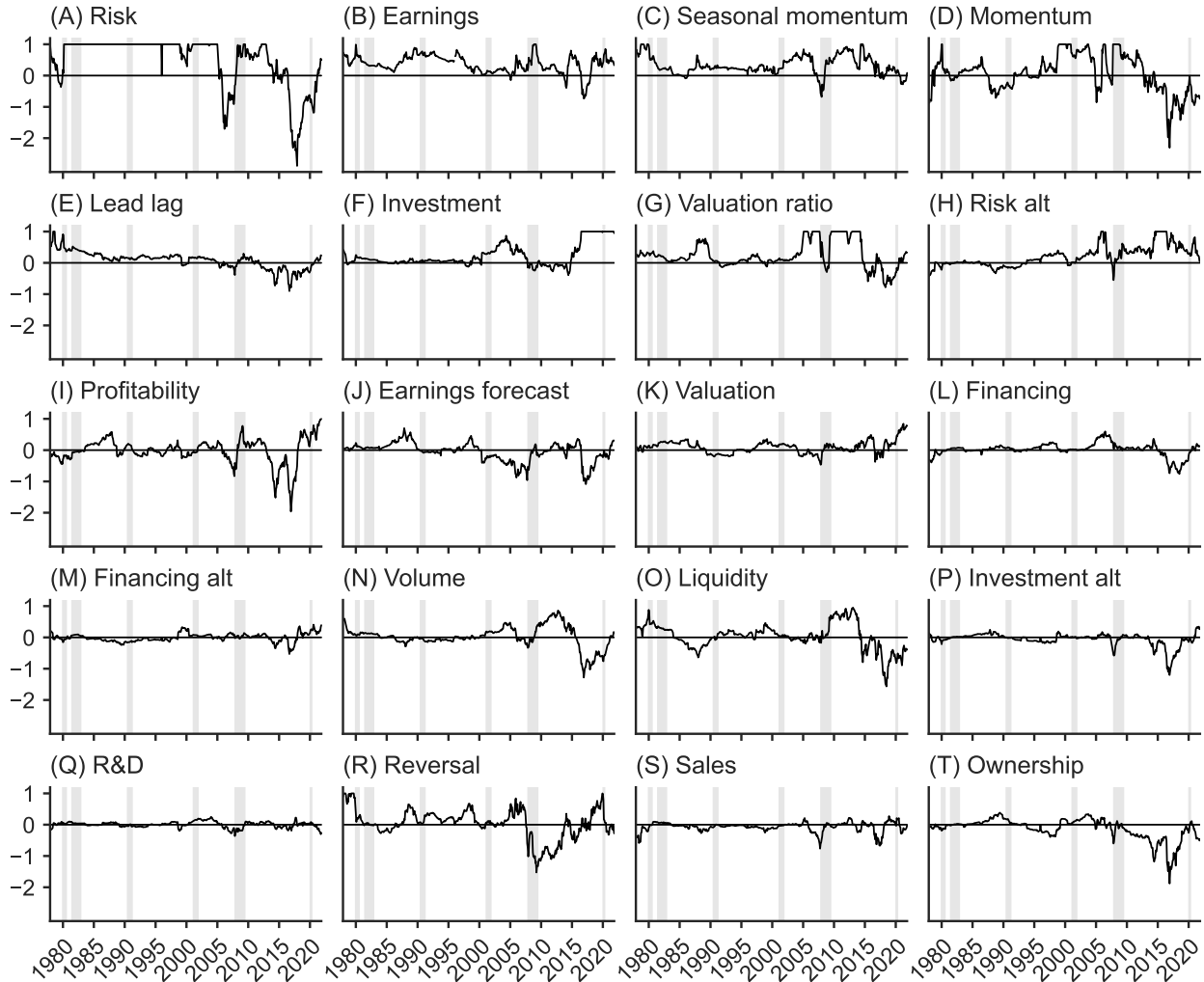
<sup>22</sup>Thus, a line in Figure 8 has a maximum value of one when the group’s contribution is equal to the maximum contribution for that window; a standardized contribution of  $-1$  means that the group makes a negative contribution that is equal in magnitude to the maximum contribution for that window.



**Figure 8. Sharpe Ratio Contributions for 60-Month Rolling Windows**

The figure depicts the contributions of the 20 predictor groups to the annualized Sharpe ratios for the long-short portfolio based on the XGBoost(c) return forecasts. The Sharpe ratios are computed using 60-month rolling windows over the 1973:01 to 2021:12 forecast evaluation period. The horizontal axis corresponds to the end of the 60-month rolling window. The contributions are estimated using the  $SPPC_p$  in Equation (23) and are standardized by the maximum contribution to the Sharpe ratio in a given rolling window. Vertical bars indicate business-cycle recessions as dated by the National Bureau of Economic Research.

make sizable negative contributions. Other groups making contributions that substantially vary between positive and negative values include *Profitability*, *Earnings forecast*, and *Reversal*. Groups making more consistent positive contributions over time include *Earnings* and *Seasonal momentum*. In general, the contributions in Figures 8 and 9 appear more stable for

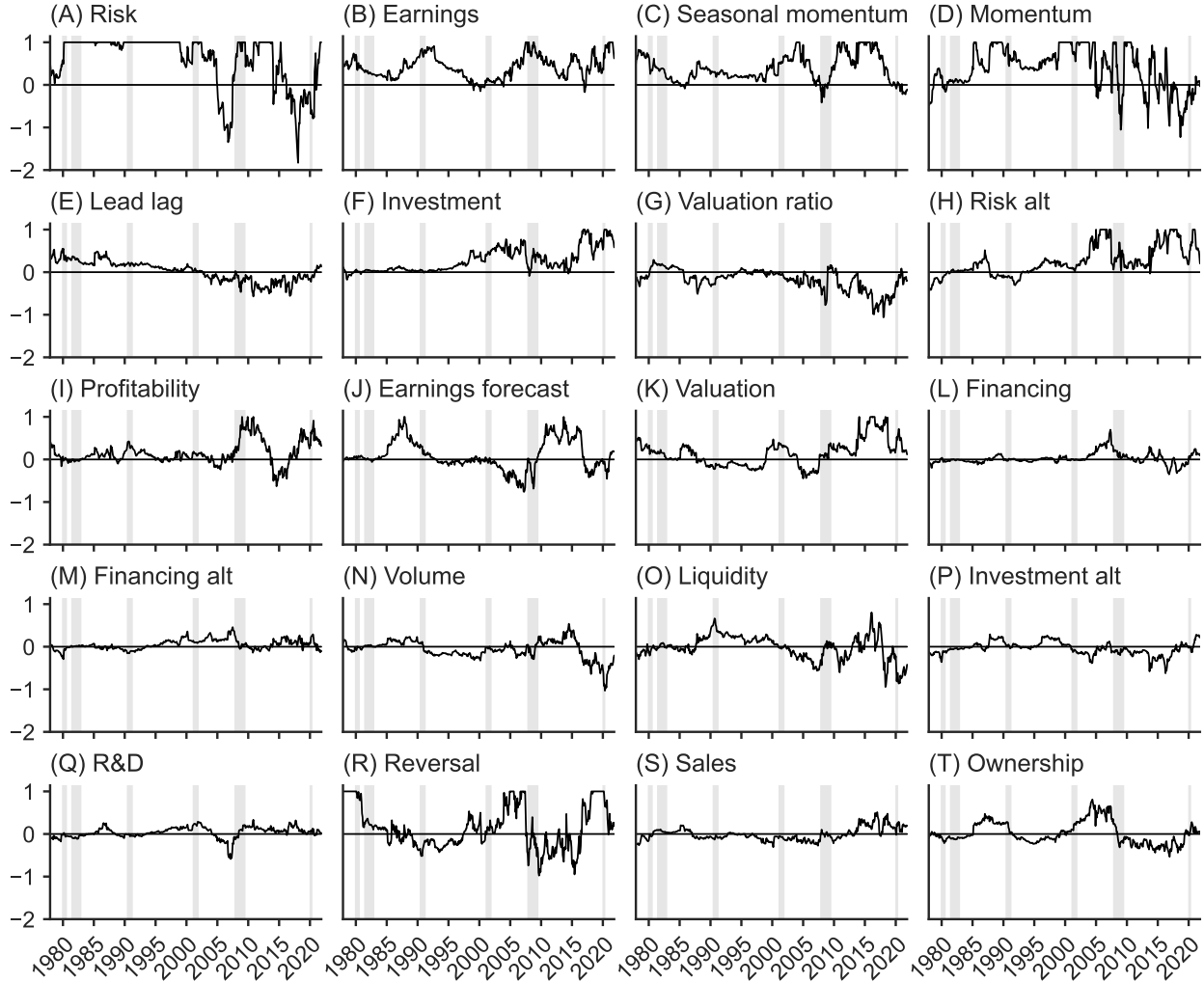


**Figure 9. Calmar Ratio Contributions for 60-Month Rolling Windows**

The figure depicts the contributions of the 20 predictor groups to the annualized Calmar ratios for the long-short portfolio based on the XGBoost(c) return forecasts. The Calmar ratios are computed using 60-month rolling windows over the 1973:01 to 2021:12 forecast evaluation period. The horizontal axis corresponds to the end of the 60-month rolling window. The contributions are estimated using the  $SPPC_p$  in Equation (23) and are standardized by the maximum contribution to the Calmar ratio in a given rolling window. Vertical bars indicate business-cycle recessions as dated by the National Bureau of Economic Research.

windows ending through the early 2000s; for windows ending after that, the contributions fluctuate more.

Figures 10 and 11 show the contributions of the predictor groups to the alphas based on the FF6 and Q5 multifactor models, respectively, computed based on the 60-month rolling windows. The two figures tell a similar story with respect to the contributions to the alphas

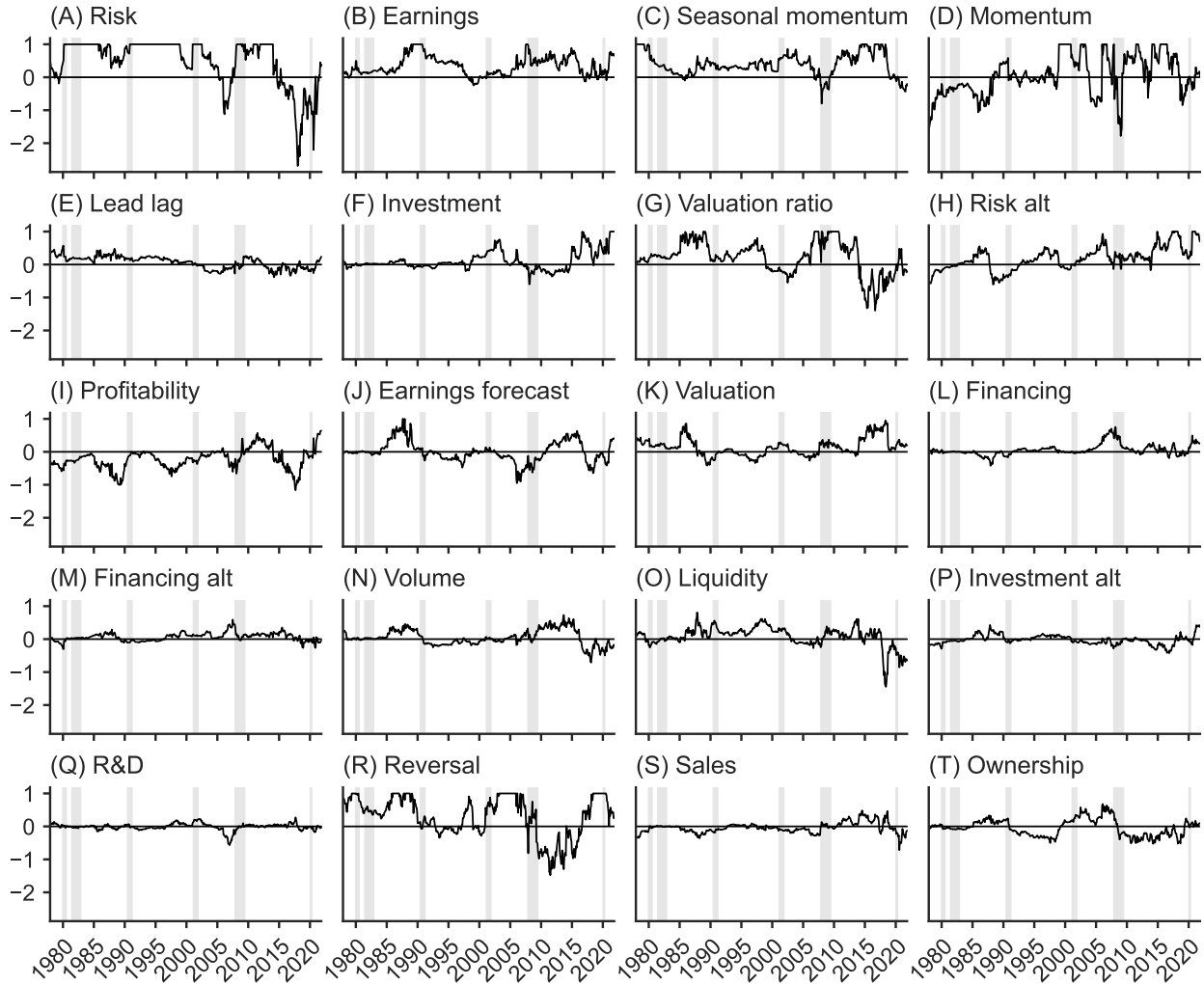


**Figure 10. FF6 Alpha Contributions for 60-Month Rolling Windows**

The figure depicts the contributions of the 20 predictor groups to the annualized alphas for the long-short portfolio based on the XGBoost(c) return forecasts. The alphas are estimated in the context of the FF6 multifactor model and computed using 60-month rolling windows over the 1973:01 to 2021:12 forecast evaluation period. The horizontal axis corresponds to the end of the 60-month rolling window. The contributions are estimated using the  $SPPC_p$  in Equation (23) and are standardized by the maximum contribution to the alpha in a given rolling window. Vertical bars indicate business-cycle recessions as dated by the National Bureau of Economic Research.

over time. For windows ending prior to the early 2000s, *Risk* nearly always contributes positively and sizably to the alphas, but it often makes large negative contributions thereafter. *Momentum*, *valuation ratio*, and *Reversal* also often make substantive negative contributions after the early 2000s. *Earnings*, *Seasonal momentum*, and *Investment* make sizable positive contributions on a reasonably consistent basis over time. Overall, similarly to Figures 8





**Figure 11. Q5 Alpha Contributions for 60-Month Rolling Windows**

The figure depicts the contributions of the 20 predictor groups to the annualized alphas for the long-short portfolio based on the XGBoost(c) return forecasts. The alphas are estimated in the context of the Q5 multifactor model and computed using 60-month rolling windows over the 1973:01 to 2021:12 forecast evaluation period. The horizontal axis corresponds to the end of the 60-month rolling window. The contributions are estimated using the  $SPPC_p$  in Equation (23) and are standardized by the maximum contribution to the alpha in a given rolling window. Vertical bars indicate business-cycle recessions as dated by the National Bureau of Economic Research.

and 9, the contributions tend to exhibit greater fluctuations in Figures 10 and 11 after the early 2000s.

## 4. Conclusion

Asset return predictability is now commonly assessed in terms of economic value as reflected by portfolio performance metrics. A researcher generates out-of-sample return forecasts for one or more assets, increasingly using a large set of predictors and a machine learning model. The return forecasts then serve as inputs to construct a portfolio over the forecast evaluation period, and portfolio performance metrics are used to measure the economic value of return predictability from an investment perspective. While measuring the economic value of return predictability is important for assessing the relevance of return predictability, it is also vital to understand the sources of the economic value provided by return predictability.

The information in the underlying predictors in fitted machine learning models is the ultimate source of return predictability and its associated economic value. However, the existing literature does not provide a general procedure for decomposing economic value as measured by a portfolio performance metric into the contributions of the underlying predictors. The present paper fills this gap in the literature by developing the  $SPPC_p$ , a new model interpretation tool founded on Shapley values that directly estimates the contributions of individual or groups of predictors in fitted prediction models to portfolio performance. Based on the logic of Shapley value, the  $SPPC_p$  fairly allocates the predictor contributions to the portfolio performance metric. The  $SPPC_p$  values for the set of predictors provide an exact decomposition of the performance metric in terms of the underlying predictors, thereby anatomizing machine learning-based portfolio performance. The  $SPPC_p$  is very flexible: it can be used for any prediction model, any strategy for mapping return forecasts to portfolio weights, and any performance metric. In sum, the  $SPPC_p$  provides a powerful tool for deepening our understanding of the sources of the economic value produced by return predictability.

We illustrate the use of the  $SPPC_p$  in an empirical application investigating firm-level stock return predictability based on 207 firm characteristics from Chen and Zimmermann

(2022). We use the XGBoost algorithm, a powerful machine learning device, to generate monthly out-of-sample return classification forecasts based on the firm characteristics for 1973:01 to 2021:12, where the individual stocks are predicted to be in quintiles in terms of their returns for the next month. Based on the forecasts, we construct a zero-investment portfolio that goes long (short) stocks predicted to be in the top (bottom) quintile. To minimize the role of small-cap stocks when forming the portfolio, we drop stocks with market capitalization below the NYSE 20th percentile and employ value weighting in the long and short legs. The long-short portfolio delivers substantial economic value in terms of Sharpe and Calmar ratios as well as risk-adjusted returns in the context of leading multifactor models.

We categorize the firm characteristics into 20 groups according to economic concepts and estimate the  $SPPC_p$  for the predictor groups and portfolio performance metrics. Groups making the largest positive contributions to portfolio performance over the full 1973:01 to 2021:12 forecast evaluation period include *Risk*, *Earnings*, *Seasonal momentum*, and *Momentum*, while *Sales* and *Ownership* make negative contributions. The performance of the long-short portfolio generally declines after 2002, but it still performs relatively well, especially during business-cycle recessions. To shed light on the sources of the change in portfolio performance over time, we estimate the  $SPPC_p$  for the predictor groups for subsamples and rolling windows from the full forecast evaluation period. The  $SPPC_p$  estimates reveal that the contributions of the *Risk* and *Momentum* groups to the performance metrics typically decrease substantively after 2002, often becoming negative. In contrast, the *Earnings*, *Seasonal momentum*, and *Investment* groups make positive and sizable contributions to portfolio performance on a relatively consistent basis over time, indicating that these characteristic groups are more reliable predictors of cross-sectional stock returns in a machine learning framework when it comes to economic value.

Due to its flexibility, in future research, the  $SPPC_p$  can be used to analyze predictor contributions to portfolio performance in a variety of settings. We focus on the XGBoost

algorithm to forecast individual stock returns in the empirical application in the present paper; the empirical application can be extended to analyze predictor contributions for alternative machine learning models as well as ensembles of models. The voluminous literature on aggregate stock market return predictability considers a lengthy list of predictors, and it would be informative to measure the contributions of predictors in machine learning models to the economic value generated by aggregate market return predictability. In addition to equities, our methodology can be used to investigate predictor contributions to economic value for portfolios formed from any asset class or combinations of asset classes. It would be illuminating to analyze predictor contributions in machine learning models to portfolio performance for a range of asset classes and to explore whether common patterns of predictor importance exist.

Our methodology can also be used to estimate the contributions of predictors to mean-variance efficient (MVE) portfolios, whose weights relate to the stochastic discount factor. For example, Kozak, Nagel, and Santosh (2020), Jensen et al. (2022), and Chen, Pelger, and Zhu (forthcoming) develop machine learning methods for estimating the weights of MVE portfolios based on large numbers of firm characteristics. The  $SPPC_p$  can be adapted to this setting to estimate the contributions of the firm characteristics to the performance of the MVE portfolio over an out-of-sample period, thereby providing further insight into the key drivers of the stochastic discount factor.

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