

# Exchange Rates and Monetary Policy with Heterogeneous Agents: Sizing up the Real Income Channel

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Exciting literature: [Farhi-Werning, Cugat, De Ferra-Mitman-Romei, Giagheddu, Zhou, Kekre-Lenel, Guo-Ottonello-Perez, ...]

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  - In the paper: similar result for monetary policy shocks
- How large is  $\chi$ ? Low in short run, higher in long run [Ruhl, Boehm-Levchenko-Pandalai-Nayar]
  - model generates **contractionary depreciation** after capital flow shock

## HANK meets Gali-Monacelli

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## Model overview

- Discrete time, small open economy (SOE) model
  - No aggregate uncertainty + small shocks (first order perturb. wrt aggregates)
- Two goods
  - “Home”:  $H$ , produced at home. Price  $P_{Ht}$  at home,  $P_{Ht}^*$  abroad
  - “Foreign”:  $F$ , produced abroad. Price  $P_{Ft}$  at home,  $P_{Ft}^* = 1$  abroad
  - Consumed in bundles. Price  $P_t$  of bundle at home,  $P_t^* = 1$  abroad
- Two classes of agents
  - large mass of foreign households with fixed real  $C^*$
  - mass 1 of domestic households, **subject to idiosyncratic income risk**

- Domestic **HA: intertemporal problem**

$$\max_{\{c_{it}\}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta_i^t \left\{ \frac{c_{it}^{1-\sigma}}{1-\sigma} - v(N_t) \right\}$$

$$c_{it} + a_{it+1} = (1 + r_t^p) a_{it} + e_{it} \frac{W_t}{P_t} N_t \quad a_{it+1} \geq 0 \quad C_t \equiv \int c_{it} di$$

- $a_{it}$  = position in domestic mutual fund

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- Domestic production and market clearing:  $Y_t = N_t = C_{Ht} + C_{Ht}^*$

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- Standard nominal wage rigidity [Erceg-Henderson-Levin, Auclert-Rognlie-Straub]

$$\pi_{wt} = \kappa_w \left( \frac{v'(N_t)/u'(C_t)}{\mu_w W_t/P_t} - 1 \right) + \beta \pi_{wt+1}$$

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- For now, domestic central bank targets CPI-based real interest rate

$$i_t = r_t + \pi_{t+1}$$

- Mutual fund and foreign agents trade two types of assets:
  - shares in home firms with price  $v_t = (v_{t+1} + \text{div}_{t+1}) / (1 + r_t)$
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- Without agg. uncertainty, portfolios indeterminate  $\Rightarrow$  assume 100% equity
  - study optimal portfolio in alternative complete-market HA model

- Calibrate to a typical emerging economy such as Mexico
- Set  $\alpha = 0.40$  to match import share of output in 2019 and balanced trade
- HA:  $\beta$  heterogeneity to match Peruvian data on MPCs [Hong 2020]
- EIS  $\sigma^{-1} = 1$
- Allow for general substitution elasticities  $\eta, \gamma$  for now.



## Response to exchange rate shocks

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# Setup

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  - microfoundation: shock to discount factor  $\beta$  abroad
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$$dQ_t = \sum_{s \geq t} \frac{di_{t+s}^*}{1+r}$$

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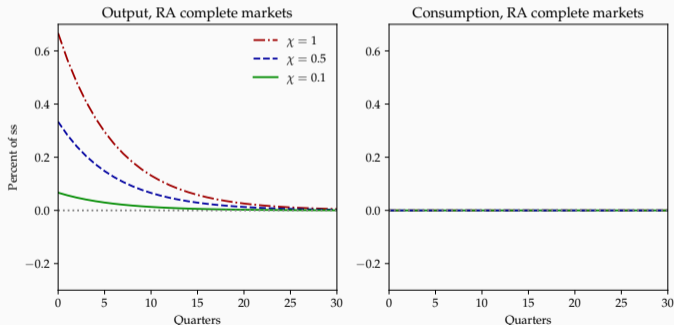
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- $Q_t \uparrow$  (real depreciation),  $\frac{P_{Ht}}{P_t} \downarrow$  and  $\frac{P_{Ht}}{\mathcal{E}_t} \downarrow$
- Use good market condition to study effect on output:

$$Y_t = (1 - \alpha) \left( \frac{P_{Ht}}{P_t} \right)^{-\eta} C_t + \alpha \left( \frac{P_{Ht}}{\mathcal{E}_t} \right)^{-\gamma} C^*$$

# Textbook RA complete markets model

- In **RA**: complete markets +  $r$  constant  $\Rightarrow C_t = C$
- Only channel: **expenditure switching** with trade elasticity  $\chi \equiv \eta(1 - \alpha) + \gamma$ 
  - home and foreign households substitute towards cheaper home goods



( $i_t^*$  shock of quarterly persistence  $\rho = 0.85$  and impact effect of 1% on  $Q$ .)

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$$\frac{W_t}{P_t}N_t = \frac{1}{\mu} \frac{P_{Ht}}{P_t} Y_t \quad \text{div}_t = \left(1 - \frac{1}{\mu}\right) \frac{P_{Ht}}{P_t} Y_t$$

- **Real income channel**  $\rightarrow$  lower value of goods sold ( $P_H$ ) relative to bought ( $P$ )
- **Multiplier channel**  $\rightarrow$  higher production ( $Y$ )



## Neutrality result for $\chi = 1$

### Theorem

$$\chi = 1 \quad \Rightarrow \quad dY^{HA} = dY^{RA}$$

Heterogeneity is **irrelevant** for output effect of exchange rate

- **Multiplier channel** undoes **real income channel**,  $\frac{P_{Ht}}{P_t} Y_t = \text{const}$ 
  - Households pay more for consumption, but work more because of the boom

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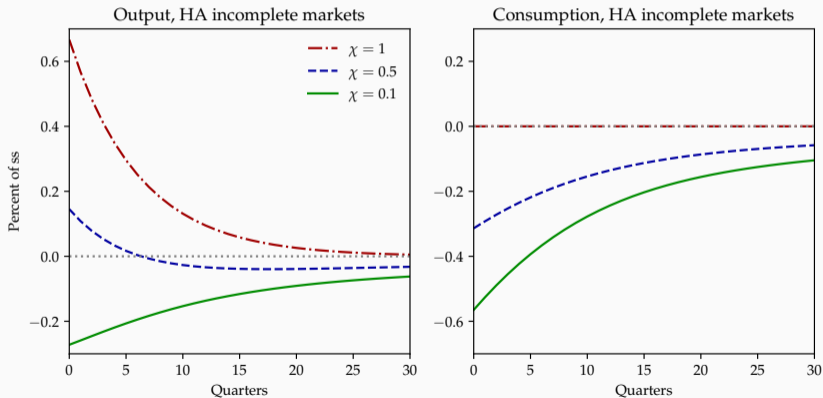
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  - Households pay more for consumption, but work more because of the boom
- More generally, for  $d\mathbf{Q} \geq 0$ , can show  $d\mathbf{Y}^{HA} < d\mathbf{Y}^{RA}$  if and only if  $\chi < 1$ .

## Contractionary devaluations in output for low $\chi$

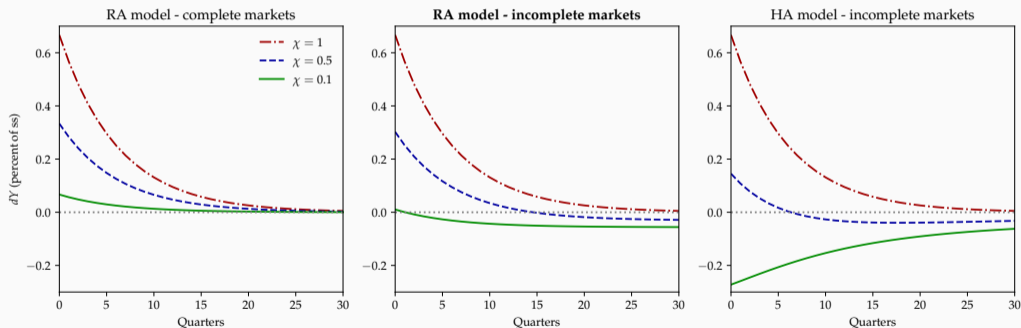
- With  $\chi$  small, **HA** model can generate **contractionary devaluations!**
  - Boom in exports does not offset change in relative prices anymore



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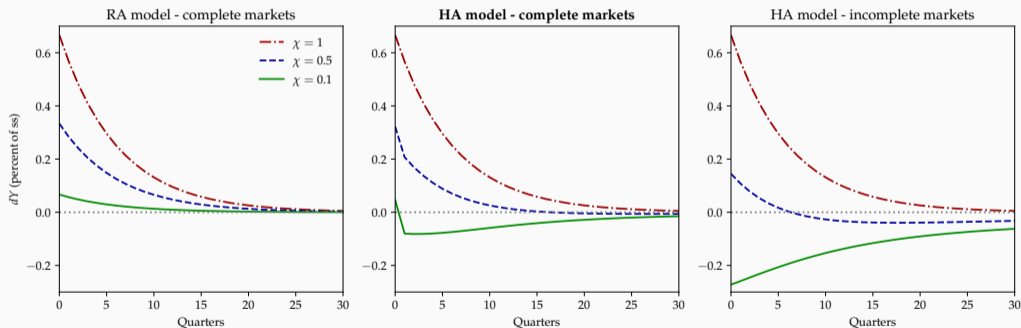
# Heterogeneity vs incomplete markets 1

- Middle panel shows  $dY$  in **RA model with incomplete markets**
  - Small contraction because of low MPCs: heterogeneity quantitatively critical



## Heterogeneity vs incomplete markets 2

- Middle panel shows  $dY$  in **HA model with complete markets**
  - Small contraction because of hedging: incomplete market also quant. critical



## Quantitative model with dynamic trade elasticity

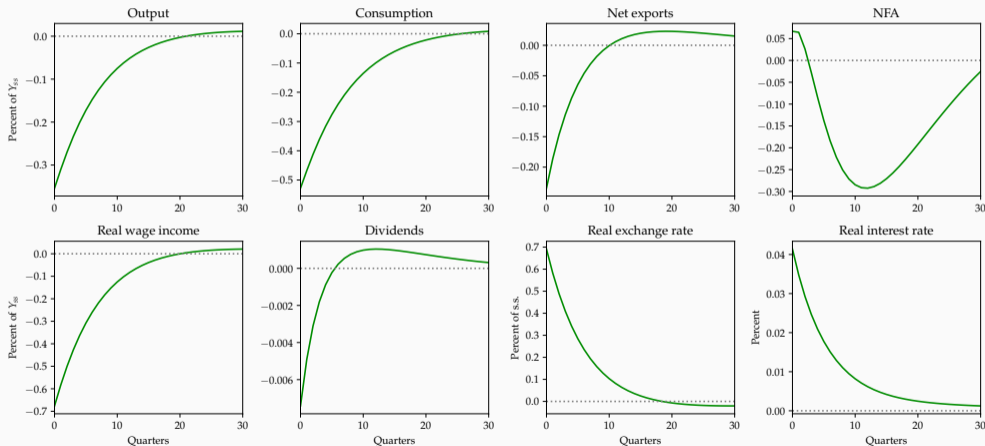
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- In simple model, trade elasticity  $\chi$  was critical. What is it?
  - Macro time-series literature  $\rightarrow \chi$  is low ( $< 1$ )
  - Trade literature (usually from cross-section)  $\rightarrow \chi$  is high ( $> 3$ )
- Build Calvo model of **delayed substitution** consistent with evidence [▶ Details](#)
  - $\chi$  is small in the short run, and large in the long run [Boehm-Levchenko-Pandalai-Nayar 20]

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  - $\chi$  is small in the short run, and large in the long run [Boehm-Levchenko-Pandalai-Nayar 20]
- Also add quantitative bells and whistles to model
  - Price rigidity in addition to wage rigidity + dollar currency pricing
  - Taylor rule for monetary policy
  - Nonhomotheticities in consumption, heterogeneous incidence of agg. shock



- Substitution delayed enough that capital outflow shocks are contractionary



## Conclusion

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**HA** + NK-SOE  $\Rightarrow$  real income channel

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- contractionary devaluations for plausibly delayed adjustment
- In paper: analytics + implications for monetary policy

- In baseline, consumption  $c_{it}$  aggregates  $H$  and  $F$  with elasticity  $\eta$ ,

$$c_{it} = \left[ (1 - \alpha)^{\frac{1}{\eta}} (c_{iHt})^{\frac{\eta-1}{\eta}} + \alpha^{\frac{1}{\eta}} (c_{iFt})^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

and preferences across goods  $j$  produced in countries  $k$  are

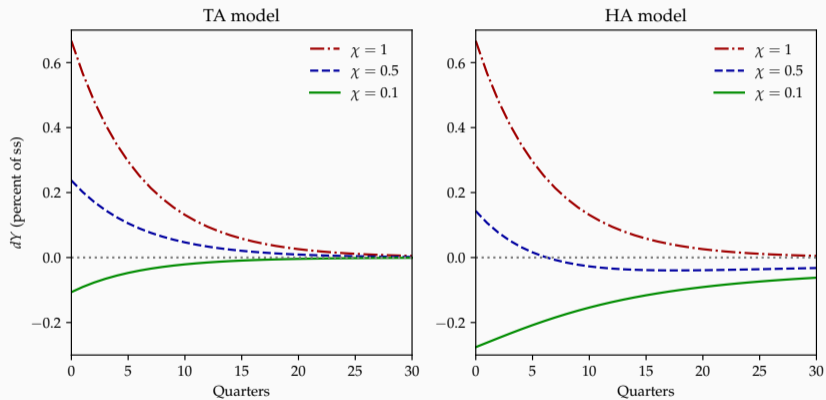
$$c_{iHt} = \left( \int_0^1 c_{iHt}(j)^{\frac{\epsilon-1}{\epsilon}} dj \right)^{\frac{\epsilon}{\epsilon-1}} \quad c_{iFt} = \left( \int_0^1 c_{ikt}^{\frac{\gamma-1}{\gamma}} dk \right)^{\frac{\gamma}{\gamma-1}} \quad c_{ikt} = \left( \int_0^1 c_{ikt}(j)^{\frac{\epsilon-1}{\epsilon}} dj \right)^{\frac{\epsilon}{\epsilon-1}}$$

with  $\epsilon > 1$ ,  $\gamma > 0$  and  $\eta > 0$ . Budget constraint:

$$\int_0^1 P_{Ht}(j) c_{iHt}(j) dj + \int_0^1 \int_0^1 P_{kt}(j) c_{ikt}(j) dj dk + a_{it+1} \leq (1 + r_t^p) a_{it} + e_{it} \frac{W_t}{P_t} N_t$$

- Demand for good  $j$  in country  $k$  by consumer  $i$ :

$$c_{ikt}(j) = \alpha \left( \frac{P_{kt}(j)}{P_{kt}} \right)^{-\epsilon} \left( \frac{P_{kt}}{P_{Ft}} \right)^{-\gamma} \left( \frac{P_{Ft}}{P_t} \right)^{-\eta} c_{it}$$



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- ... but one **big difference**: monetary easing here can have **negative NPV**

$$\text{Present value } (dY) < 0 \quad \Leftrightarrow \quad \chi < 1 - \alpha$$

1. Nonhomothetic Stone-Geary to capture heterogeneity in real income effect

$$C_t = \left( (1 - \alpha)^{\frac{1}{\eta}} C_{Ht}^{\frac{\eta-1}{\eta}} + \alpha^{\frac{1}{\eta}} (C_{Ft} - \underline{C}_F)^{\frac{\eta-1}{\eta}} \right)^{\frac{\eta}{\eta-1}}$$

2. Realistic passthrough of exch. rate to domestic & foreign consumer prices

- Add domestic price rigidities

$$\pi_{Ht} = \kappa_H \left( \frac{\mu_H W_t / Z_t}{P_{Ht}} - 1 \right) + \beta \pi_{Ht+1}$$

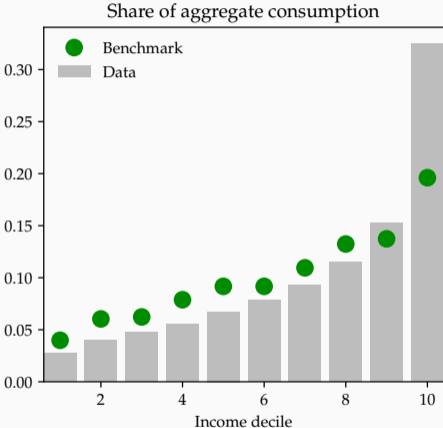
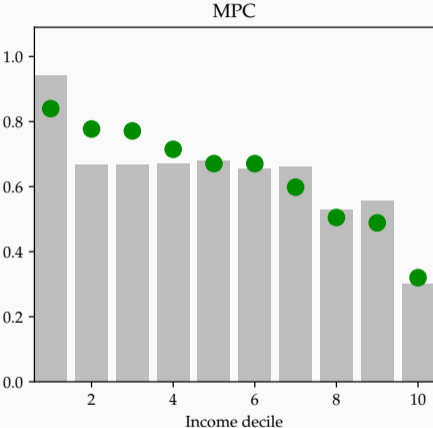
- Add flexibility of dollar export prices

$$\pi_{Ht}^* = \kappa_X \left( \frac{P_{Ht} / \mathcal{E}_t}{P_{Ht}^*} - 1 \right) + \beta \pi_{Ht+1}^*$$

- Allow foreign retailers to repatriate profits from dollar sales

3. Allow for currency mismatch in NFA ( $f_Y \equiv$  asset-liability mismatch/GDP)

- Debt held by households via mutual fund, or by government and then rebated

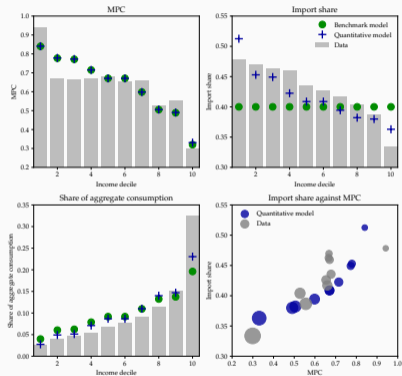


Parameter	Benchmark	Quantitative	Parameter	Benchmark	Quantitative
$\sigma$	1	1	$\mu$	1.03	1.028
$\psi$	2	2	s.s. nfa	0	0
$\eta$	$\frac{\{0.1, 0.5, 1, 2-\alpha\}}{2-\alpha}$	4	$\sigma_e$	0.6	0.6
$\gamma$	$= \eta$	$= \eta$	$\rho_e$	0.92	0.92
$\theta$	n.a.	0.987	$\theta_w$	0.95	0.95
$\beta$	0.954	0.953	$\theta_p$	0	0.75
$\Delta$	0.06	0.067	$\theta_x$	n.a.	0.66
$\alpha$	0.4	0.323	$\theta_l$	0	0
$\underline{c}$	0	0.114	$\phi$	n.a.	1.5

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Moment	Data	Benchmark model	Quantitative Model
Average MPC	0.632	0.636	0.637
Std of MPC	0.152	0.151	0.149
Average tradable share	0.400	0.400	0.400
Std of tradable share	0.042	n.a.	0.042

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## Delayed substitution model

- Ratio  $x = \frac{C_H}{C_F}$  is a state variable, updated a la Calvo with parameter  $\theta$
- Static outcome ( $\theta = 0$ )

$$x_t = \frac{\alpha}{1 - \alpha} \left( \frac{P_{Ht}}{P_{Ft}} \right)^{-\eta}$$

- Dynamic ( $\theta > 0$ ) outcome with log utility [general case in paper]

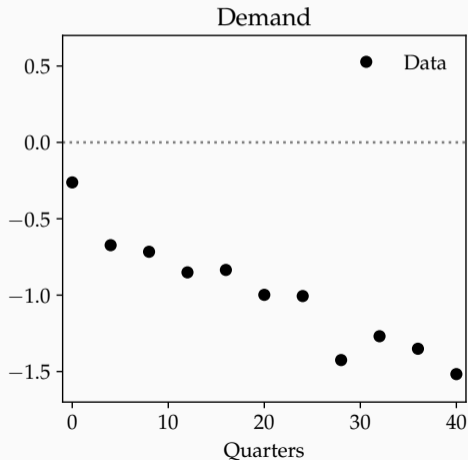
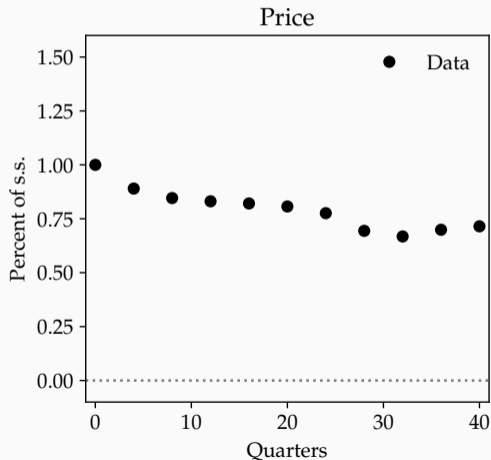
$$d \log x_t^* = -\eta(1 - \beta\theta) d \log \frac{P_{Ht}}{P_{Ft}} + \beta\theta d \log x_{t+1}^*$$

$$d \log x_t = (1 - \theta) d \log x_t^* + \theta d \log x_{t-1}$$

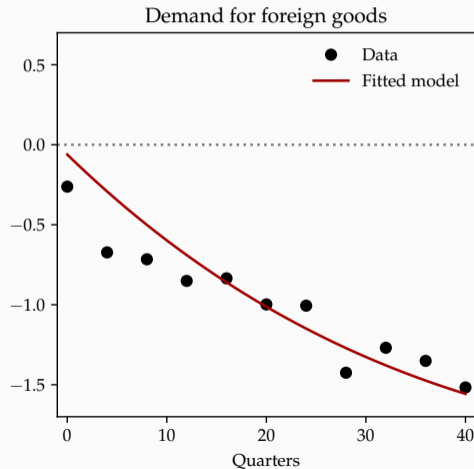
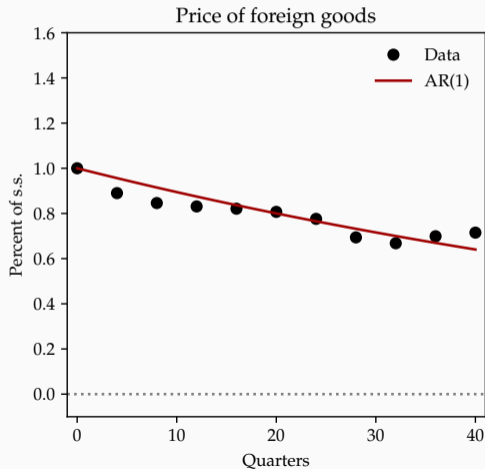
Long-run elasticity is  $\eta$ , short-run is  $< \eta$ , depends on shock duration

- Same assumption for  $\gamma$  (exports slow to adjust)

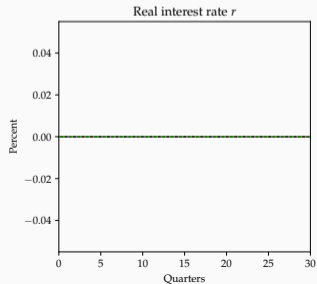
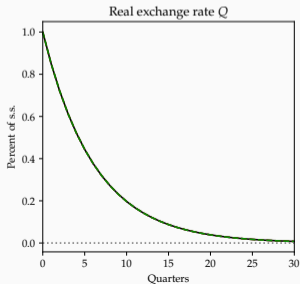
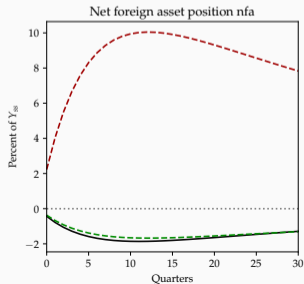
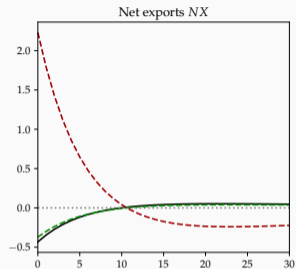
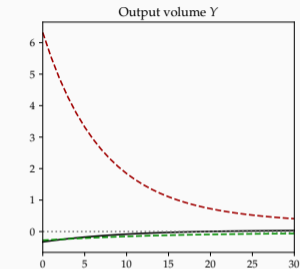
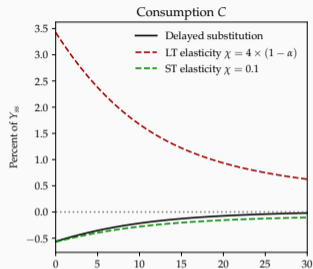
- Use tariff change evidence in Boehm, Levchenko, and Pandalai-Nayar



- Use tariff change evidence in Boehm, Levchenko, and Pandalai-Nayar



# Quantitative model behaves like a low-elasticity model



	Bench.	Low $\alpha$	High MPC	Full DCP	Low passthru	Homothetic	High ST elast.
$dY_0$	- 0.36	- 0.27	- 0.40	- 0.31	- 0.09	- 0.32	- 0.30
PDV of $dY$	- 2.03	- 2.38	- 1.15	- 1.25	- 1.01	- 1.51	- 0.25

(Response to  $i_t^*$  shock of quarterly persistence  $\rho = 0.8$  and impact effect of 1% on  $Q$ .)

Assuming a gross currency debt position in the NFA of 50% of annual GDP:

	Benchmark	Mutual fund	Government		
			lump-sum	prop tax	+ deficit-fin.
$dY_0$	- 0.36	- 0.41	- 0.71	- 0.63	- 0.46
PDV of $dY$	- 2.03	- 2.86	- 3.18	- 3.17	- 3.21

(Response to  $i_t^*$  shock of quarterly persistence  $\rho = 0.8$  and impact effect of 1% on  $Q$ .)

