# Causal Inference with Corrupted Data Measurement Error, Missing Values, Discretization, and Differential Privacy

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EEA ESEM 2023



# 1 Motivation

2 Model

3 Proposal

4 Case study

2020 Census will have differential privacy

■ (slowly) breaking news: April 22, 2022

# The New York Times

The 2020 Census Suggests That People Live Underwater. There's a Reason.

# 2020 Census will have differential privacy

#### differential privacy achieved by injecting synthetic noise

- "We are deploying differential privacy, the gold standard for privacy protection in computer science and cryptography, to preserve confidentiality in the 2020 Census and beyond"
- "There are many variants of differential privacy. The one selected for the 2020 Census introduces controlled noise into the data"

previously implemented in Apple iOS and Google Chrome



 painful trade-off between privacy and precision (Duchi et al. 2018, Abowd + Schmutte 2019, Hotz et al. 2022)

# Why will the Census have privacy?

#### a simulated attack on the 2010 Census



#### what did they find?

• "Our simulated attack demonstrated that, depending on the quality of the external data used,

between 52 and 179 million respondents to the 2010 Census can be correctly re-identified from the reconstructed microdata"

# Another recent announcement: discretization

to further protect privacy, the Bureau will discretize wage data

#### Atlanta Fed Wage Tracker data with and without rounded wages

Median annual log wage change, three-month moving average



after backlash, the policy was delayed

# What are experts saying?

#### Prof. Cynthia Dwork (computer science)

"Imagine a kind of weaponization, one where somebody decides to make a list of all the gay households across the country. I expect there will be people who would write the software to do that."

#### Prof. Charles Manski (econometrics)

"This is not a minor technical issue. It's an inescapable tension between enhancing privacy and enhancing data usability."

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# What does this mean for causal inference?

#### economists are worried about these "new" data corruptions

- differential privacy
- discretization

even before 2020, the Census had "old" data corruptions...

- missing values
- measurement error
- we propose a new end-to-end procedure
  - 1 data cleaning (slow rate)
  - **2** estimation (fast rate)
  - 3 inference (adjusted confidence interval)

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# Related work

semiparametric statistics

- asymptotic variance (Newey 1994, Robins et al. 1995, Hirano et al. 2003)
- targeted machine learning (van der Laan + Rubin 2006, Zheng + van der Laan 2011, Luedtke + van der Laan 2016)
- debiased machine learning (Chernozhukov et al. 2016, 2018, 2021)

#### error-in-variable regression

- auxiliary info: repeated measurement, instrument, negative control (Hausman et al. 1991, Schennach 2007, Maio et al. 2018, Deaner 2018)
- Lasso and Dantzig: covariance of measurement error must be known (Loh + Wainwright 2012, Rosenbaum + Tsybakov 2013, Belloni et al. 2017)
- principal component regression (Stock + Watson 2002, Agarwal et al. 2020)
- PCA for large factor models
  - identification, inference for latent factors (Bai 2003, Bai + Ng 2013)
- treatment effects with corrupted data
  - multiple imputation (Rubin 1976, Meng 1994)

# causal inference with the 2020 US Census?



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# Model: Causal parameter

- $Y_i \in \mathbb{R}$  outcome
- $D_i \in \{0, 1\}$  treatment
- $X_{i,\cdot} \in \mathbb{R}^p$  covariates
- for today, we focus on ATE with i.n.i.d. data

$$heta_0 = rac{1}{n}\sum_{i=1}^n heta_i, \hspace{1em} heta_i = \mathbb{E}[\,Y_i^{(1)} - \,Y_i^{(0)}]$$

■ the paper considers LATE, elasticity, CATE, etc

However, we observe  $(Y_i, D_i, Z_{i,\cdot})$  rather than  $(Y_i, D_i, X_{i,\cdot})$  $Y_i = \gamma_0(D_i, X_{i,\cdot}) + \varepsilon_i$  $Z_{i,\cdot} = [X_{i,\cdot} + H_{i,\cdot}] \odot \pi_{i,\cdot}$ 

This model encompasses all four types of corruption.



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# Model: Key assumption

#### Assumption: true covariates X are approximately low rank

Why? It holds in Census data (Autor et al. 2013)



Intuition: repeated measurement model

- average disability benefits
- average medical benefits
- average unemployment benefits

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# Census is $\sim low \ rank$ ; has $\sim$ repeated measurements



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We would like a procedure that

- estimates causal parameters as if data were uncorrupted
- adjusts for data cleaning in the confidence interval
- does not require knowledge of the corruption covariance structure
- preempts the looming trade-off of privacy versus precision

# Proposal: Algorithm

## Using the split sample





- 1 data cleaning: Â using "train"
- 2 regression:  $\hat{\gamma}$  using "train"
- 3 balancing weights:  $\hat{\alpha}$  using "train"
- 4 causal parameter:  $\hat{\theta}$  using "test"
  - implicit data cleaning of Z<sub>test</sub>!

# Proposal: Theory

#### Assume

- 1 each row of measurement error  $H_{i,\cdot}$  is mean zero and subexponential
- 2 each row of missingness  $\pi_{i,.}$  is subexponential
- 3  $r \approx rank(X)$  and the singular values are well-balanced

## Theorem (informal):

$$\hat{\mathrm{X}} \stackrel{p}{
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Interpretation

- from data cleaning to confidence interval
- $\hat{X} X$  converges at rate slower than  $n^{-1/2}$
- yet  $\hat{ heta} heta_0$  converges at rate  $n^{-1/2}$

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# *slow* data cleaning, yet *fast* causal inference



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# Case study: Import competition



what is the effect of import competition on the US labor market?

- Census data at commuting zone level (Autor et al. 2013)
- can we recover the same effects with synthetic corruption?
  - differential privacy calibrated to 2020 Census levels
- causal parameter: partially linear IV

# Case study: Synthetic corruption





(b) Missing values



(d) Differential privacy

#### (a) Measurement error



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# Case study: Calibration



Calibrated differential privacy

Results with formal differential privacy guarantee

- plausible deniability that any individual contributed data to a CZ
- parametrized by  $\varepsilon_{DP}$ , a measure of privacy loss
- calibrate Laplacian variance to  $\varepsilon_{DP}$  and variation within the CZ (Dwork et al. 2006)

Case study: Takeaway

# both privacy and precision

# hide your cake and eat it too

# Conclusion

■ goal: causal inference using 2020 Census

- abstractly: learn causal parameter from corrupted data
- concretely: overcome trade-off between privacy and precision

• we propose new data cleaning-adjusted confidence intervals

- bridge matrix completion  $(\hat{X} X)$  with semiparametrics  $(\hat{\theta} \theta_0)$
- future work: confounded noise, sample selection bias

I would love to talk more!

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