

# The Option Value of Occupations

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Bank of Portugal & IZA

EEA–ESEM, Aug 2023



CNN Money Companies Markets Tech Media U.S. 2017

# 100 Best Jobs in America

CNNMoney/PayScale.com's top 100 careers with big growth, great pay and satisfying work

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CAREERS > SALARIES & COMPENSATION

## 25 Highest Paid Occupations in the US

+ *future jobs*  $\implies$  option value

# What I do & find

1. **Document** diverging occupational wage trajectories  
Hungarian linked administrative data across employers and occupations
2. **Model** job mobility within and across occupations  
Wage schedules, wage offers, labor market frictions, amenities, switching costs
3. **Estimate** substantial heterogeneity in the flow vs. option value of occupations  
Low-skill occs. have high flow value / high-skill occs. have high option value
4. **Simulate** counterfactual occupational wage trajectories  
Starting in bottom-wage high-skill occs.  $\gg$  top-wage low-skill occs.

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# Model in words

## Opportunities vs. choices

Individual works in a job (occupation  $a$ , wage  $i$ ), enjoys flow utility  $u_{ai}$

Their wage may increase/decrease from  $i$  to  $w$  at rate  $\chi_{ai}^{aw}$

They may separate from their job at rate  $\delta_a$

They may receive a job offer from occupation  $o$  at rate  $\lambda_a^o$

- Wage offer  $w \sim f^o$
- Stochastic switching cost  $\tilde{c}_a^o \implies$  accept offer if  $V_{ow} - \tilde{c}_a^o > V_{ai}$

# Model in math

Employed in occupation  $a$  earning wage  $i$ :

$$V_{ai} = \underbrace{\frac{u_{ai}}{\Gamma}}_{\text{flow value}} + \underbrace{\frac{\mathbb{E}_w [\chi_{ai}^{aw} V_{aw}]}{\Gamma} + \frac{\delta_a V_n}{\Gamma}}_{\text{continuation value}} + \underbrace{\frac{\mathbb{E}_{o,w,\tilde{c}} [\lambda_a^o \max\{V_{ow} - \tilde{c}_a^o, V_{ai}\}]}{\Gamma}}_{\text{option value}}$$

$$\Gamma = \sum_o \lambda_a^o + \sum_w \chi_{ai}^{aw} + \delta_a + \rho$$

## Model in terms of CCPs

$\tilde{c}_a^o \sim \text{Logistic}(c_a^o)$  (cf. Arcidiacono, Gyetvai, Maurel, and Jardim, 2022 NBER WP)

$$\rho V_{ai} = u_{ai} + \sum_w \chi_{ai}^{aw} (V_{aw} - V_{ai}) + \delta_a (V_n - V_{ai}) - \sum_{o,w} \lambda_a^o \log(1 - p_{ai}^{ow}) f^{ow}$$

where  $p_{ai}^{ow} = \frac{\exp(V_{ow} - V_{ai} - c_a^o)}{1 + \exp(V_{ow} - V_{ai} - c_a^o)}$

# Identification in a nutshell

$$\text{hazard} = \underbrace{\text{Pr}(\text{offer arrives})}_{\text{opportunities}} \times \underbrace{\text{Pr}(\text{offer is accepted})}_{\text{choices}}$$

## Separating opportunities from choices

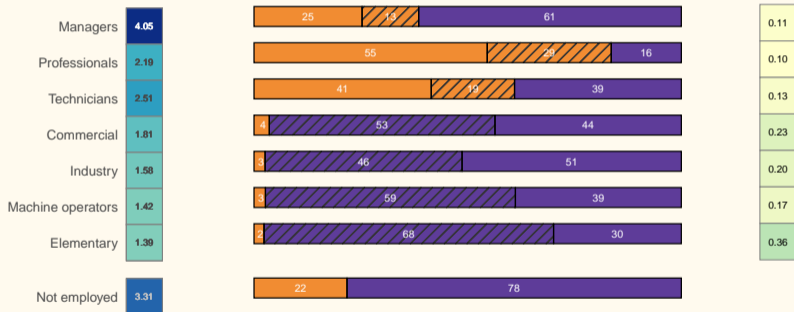
- **Frequent offers**  $\implies$  wait for a high-wage offer  $\implies$   $\uparrow$  transitions at high wages
- **Strong preferences**  $\implies$  accept any wage offer  $\implies$   $\uparrow$  transitions at all wages



## Offer arrivals

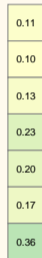
Total (annual rate)

Share of **high** / **own** / **low-skill** offers (%)



## Job separations

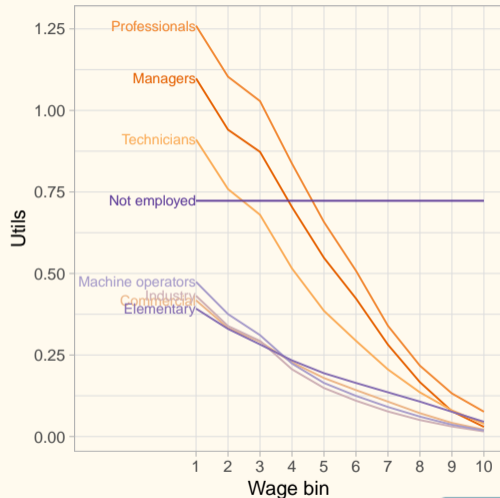
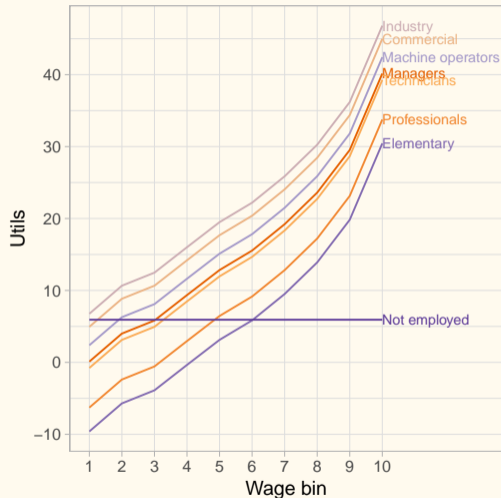
Total (annual rate)



[More results](#)

# The flow vs. option value of occupations

Estimates

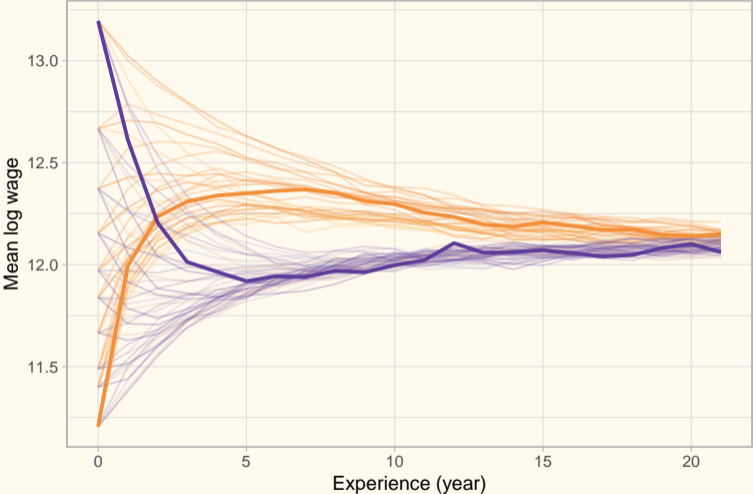


Formulas

Comp. diff'l's

# Simulating job trajectories

Estimates



Procedure

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Additional Slides

# Literature

## Career decisions

Keane and Wolpin (1997), Neal (1999), Sullivan and To (2014), ...

## Occupational choice

Miller (1984), McCall (1990), Antonovics and Golan (2012), ...

## Heterogeneity in job search

Postel-Vinay and Robin (2002), Cahuc, Postel-Vinay, and Robin (2006), Taber and Vejlin (2020), ...

## Option values

Rust (1987), Arcidiacono (2004), Stange (2012), ...

# References I

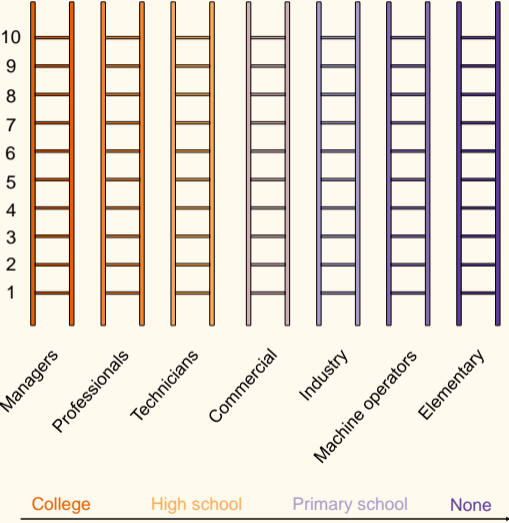
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# Occupational ladders and skill levels



2-digit occs.

◀ Back

# Skill levels and most frequent occupations

## 1-Managers College+HS

Managing directors  
Legislators

## 2-Professionals College

STEM  
Business, legal, and soc. sci.

## 3-Technicians High school

STEM  
Business

## 4-Commercial Primary

Catering  
Services

## 5-Industry Primary

Metal and electrical ind.  
Construction

## 6-Machine operators Primary

Drivers  
Assemblers

## 7-Elementary

Elementary

# Hungarian linked EE data with occupations

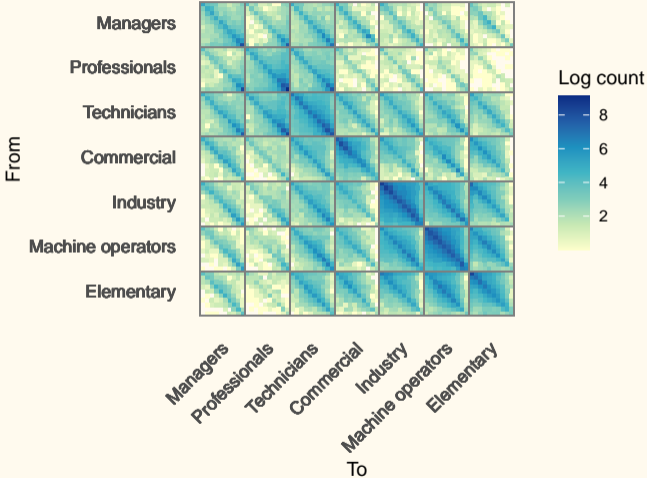
2003–2017, 50% sample

- 5 million individuals, 900 thousand firms per year
- Estimation sample: 22–50 males → 5 million job spells

1. (Virtually) continuous-time data
2. Reliable occupational classification → high vs. low-skill occupations

Various versions used in Koren and Tenreyro (2013 AER), Halpern, Koren, and Szeidl (2015 AER), DellaVigna, Lindner, Reizer, and Schmieder (2017 QJE), Harasztosi and Lindner (2019 AER), Verner and Gyöngyösi (2020 AER)

# Observed EE transitions



# Occupations capture diverging wage trajectories

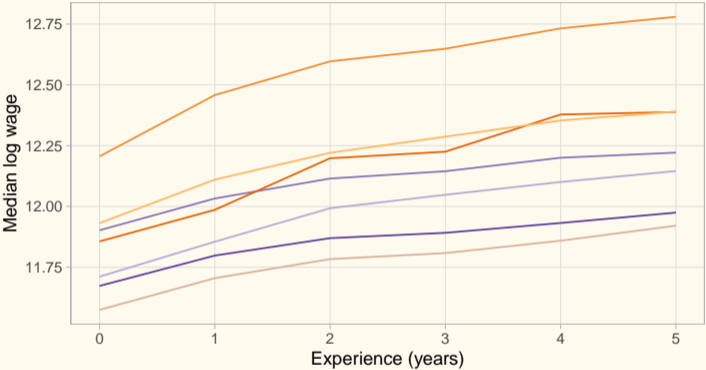


- By age
- By first occ.
- By current occ.
- Data
- Job ladders
- Transition matrix
- ◀ Back

# Occupations capture diverging wage trajectories

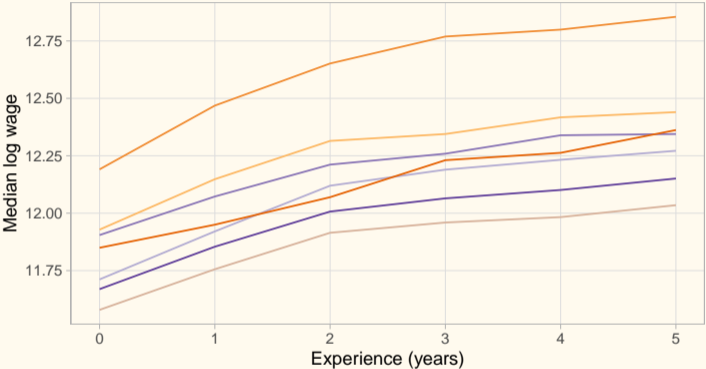


# Occupations capture diverging wage trajectories



Current occupation — Managers — Professionals — Technicians  
— Commercial — Industry — Machine operators — Elementary

# Occupations capture diverging wage trajectories



Starting occupation — Managers — Professionals — Technicians  
— Commercial — Industry — Machine operators — Elementary



## Flow vs. continuation value—formulas

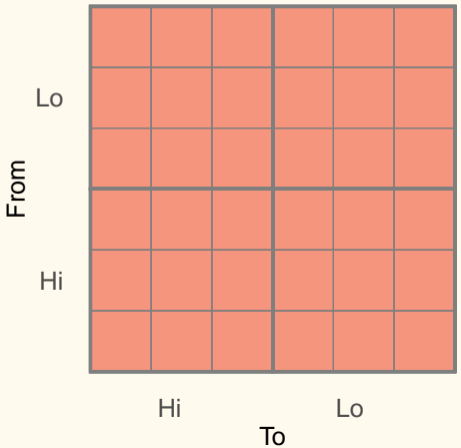
$$V_{ai} = \underbrace{\frac{u_{ai}}{\Gamma}}_{\text{flow value}} + \underbrace{\frac{\mathbb{E}_w [\chi_{ai}^{aw} V_{aw}]}{\Gamma} + \frac{\delta_a V_n}{\Gamma} + \frac{\mathbb{E}_{o,w,\tilde{c}} [\lambda_a^o \max\{V_{ow} - \tilde{c}_a^o, V_{ai}\}]}{\Gamma}}_{\text{continuation value}}$$

option value

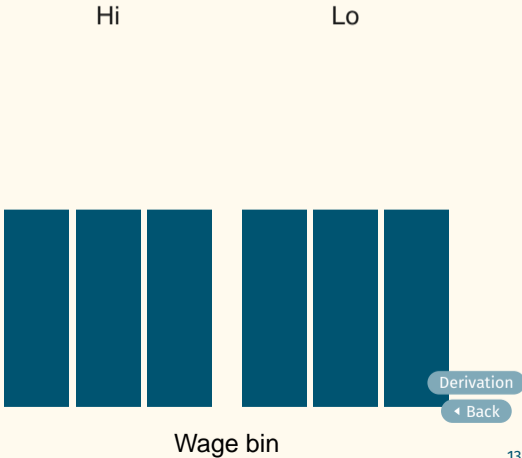
$$\Gamma = \sum_o \lambda_a^o + \sum_w \chi_{ai}^{aw} + \delta_a + \rho$$

Identifying variation  
Hazards across destination jobs

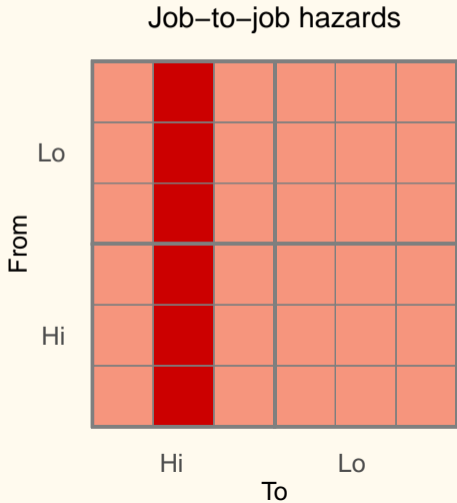
Job-to-job hazards



Offered wage distributions



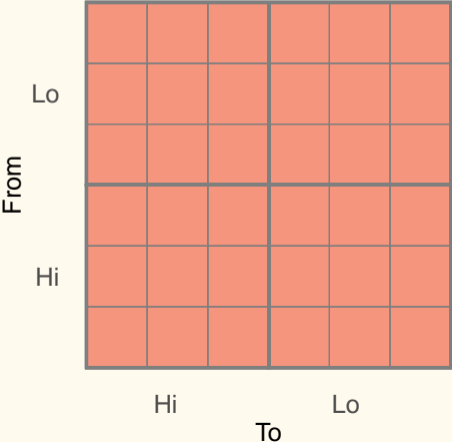
## Identifying variation Hazards across destination jobs



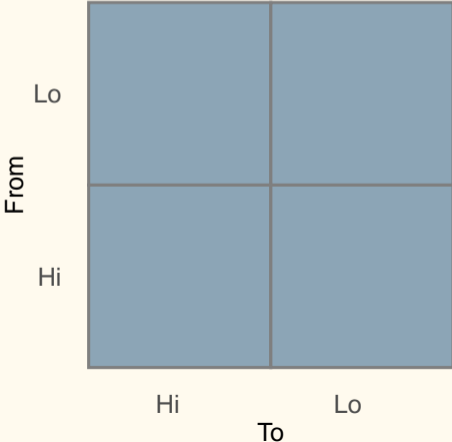
## Identifying variation

Hazards across origin and destination occupations at high wages

Job-to-job hazards



Offer arrival rates



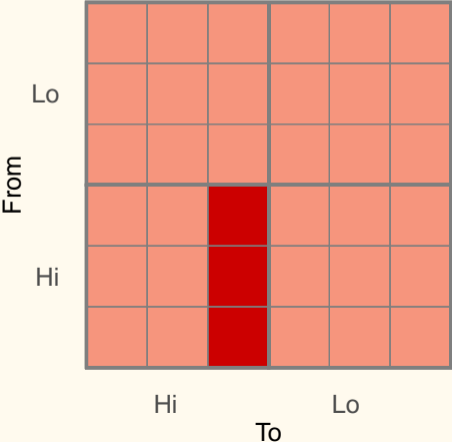
Derivation

◀ Back

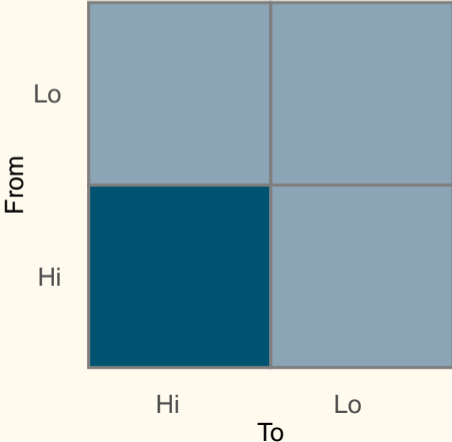
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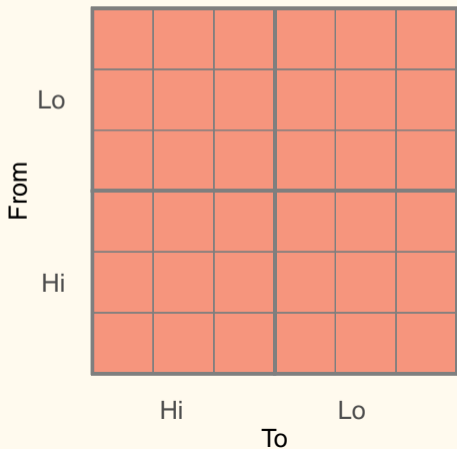
Derivation

◀ Back

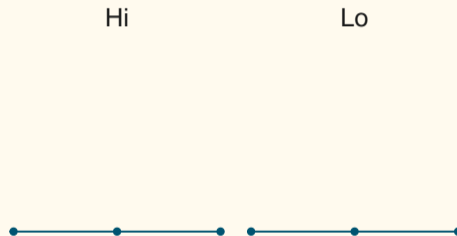
## Identifying variation

Hazards across origin and destination jobs

Job-to-job hazards



Flow utility



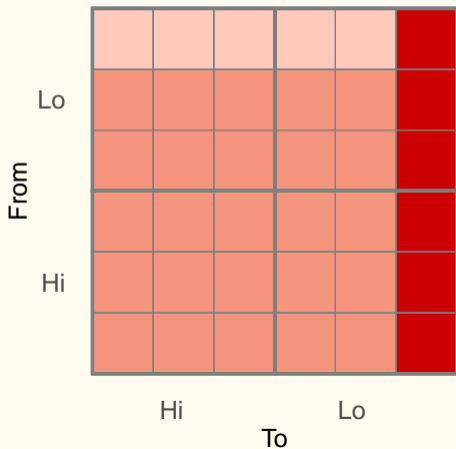
Derivation

◀ Back

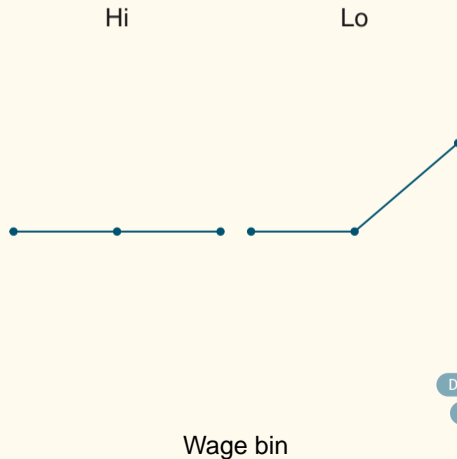
## Identifying variation

Hazards across origin and destination jobs

Job-to-job hazards



Flow utility



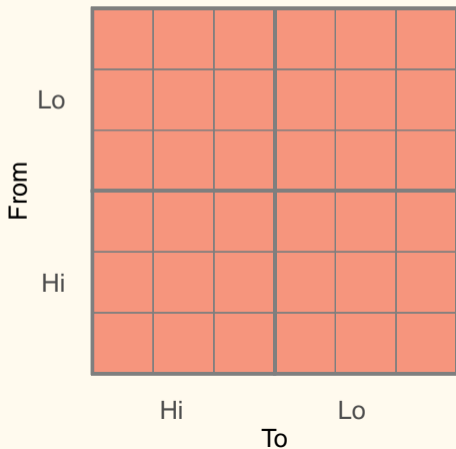
Derivation

◀ Back

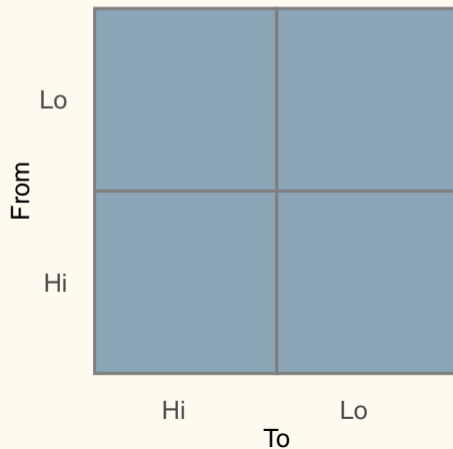
## Identifying variation

Hazards across origin and destination occupations at all wages

Job-to-job hazards



Switching costs



Structure

Derivation

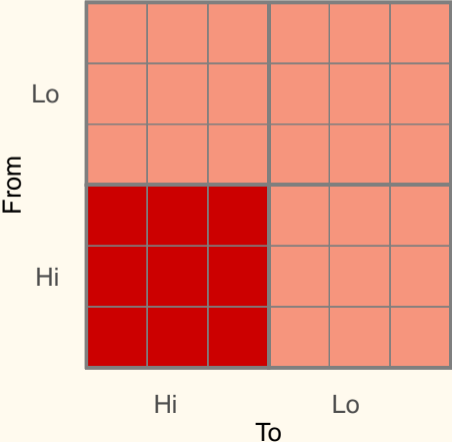
◀ Back



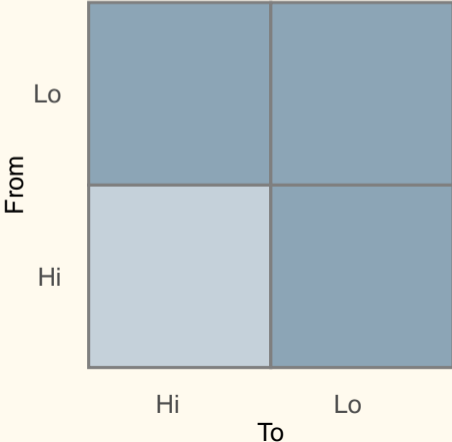
## Identifying variation

Hazards across origin and destination occupations at all wages

Job-to-job hazards



Switching costs



Structure

Derivation

◀ Back

*Idea: compare hazards of moving to the same job as the current one. Differential rates across wages are due to differences in offer propensity.*

Note that  $p_{ai}^{ai} = p_{aj}^{aj}$  for all  $a, i, j$

$$p_{ai}^{ai} = \frac{\exp(V_{ai} - V_{ai} - c_a^a)}{1 + \exp(V_{ai} - V_{ai} - c_a^a)} = \frac{\exp(-c_a^a)}{1 + \exp(-c_a^a)}$$

Therefore

$$\frac{h_{ai}^{ai}}{h_{aj}^{aj}} = \frac{\lambda_a^a p_{ai}^{ai} f^{ai}}{\lambda_a^a p_{aj}^{aj} f^{aj}} = \frac{f^{ai}}{f^{aj}}$$

$$\implies f^{ai} = \frac{h_{ai}^{ai}}{\sum_w h_{aw}^{aw}}$$

**Very** simple estimation is appealing to wider audience

*Idea: the odds of accepting an offer plus its reverse needs to be equal for all wages*

Log odds of accepting offers can be written in two ways:

1. Plugging in structural parameters for CCPs:

$$\varpi_{ai}^{bj} = \log \left( \frac{p_{ai}^{bj}}{1 - p_{ai}^{bj}} \right) = \log \left( \frac{h_{ai}^{bj}}{\lambda_a^b f^{bj} - h_{ai}^{bj}} \right)$$

Only unknown is  $\lambda_a^b \implies \varpi_{ai}^{bj} \equiv \varpi_{ai}^{bj}(\lambda_a^b)$

2. Plugging in value functions for CCPs:

$$\varpi_{ai}^{bj} = \log \left( \frac{p_{ai}^{bj}}{1 - p_{ai}^{bj}} \right) = V_{bj} - V_{ai} - c_a^b$$

First, offer arrives from same occupation:

$$\varpi_{ai}^{aj} = V_{aj} - V_{ai} - c_a^a$$
$$\implies \varpi_{ai}^{aj} + \varpi_{aj}^{ai} = \varpi_{ak}^{al} + \varpi_{al}^{ak} \implies \lambda_a^a \text{ from any } (i, j, k, \ell) \text{ 4-tuple}$$

Next, offer arrives from another occupation:

$$\varpi_{ai}^{bj} = V_{bj} - V_{ai} - c_a^b$$
$$\implies \varpi_{ai}^{bj} + \varpi_{bj}^{ai} = \varpi_{ak}^{bl} + \varpi_{bl}^{ak} \implies \lambda_a^b, \lambda_b^a \text{ from any two } (i, j, k, \ell), (i', j', k', \ell') \text{ 4-tuples}$$

*Idea: having identified the offered wages and arrival rates, CCPs map to hazards*

By the hazard definition,

$$h_{ai}^{bj} = \lambda_a^b p_{ai}^{bj} f^{bj}$$
$$\implies p_{ai}^{bj} = \frac{h_{ai}^{bj}}{\lambda_a^b f^{bj}}$$

*Idea: remaining parameters come from changes across wages vs. occupations*

Plug the structural parameters in the values in the log odds:

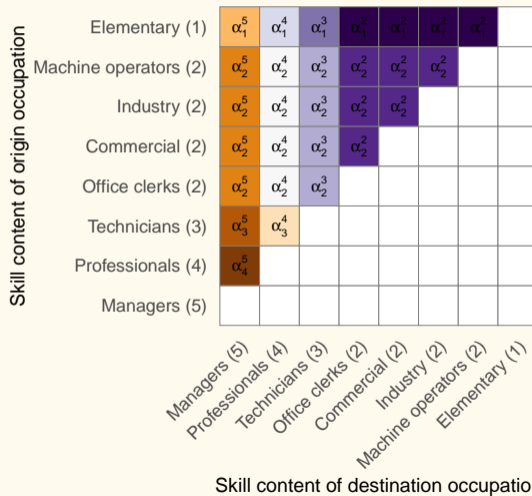
$$\begin{aligned} \varpi_{ai}^{bj} &= V_{bj} - V_{ai} - c_a^b \\ &= \frac{1}{\delta_b + \rho} \left( u_{bj} + \sum_w \chi_{bj}^{bw} (\varpi_{bj}^{bw} + c_b^b) - \sum_{o,w} \lambda_b^o \log(1 - p_{bj}^{ow}) f^{ow} \right) \\ &\quad - \frac{1}{\delta_a + \rho} \left( u_{ai} + \sum_w \chi_{ai}^{aw} (\varpi_{ai}^{aw} + c_a^a) - \sum_{o,w} \lambda_a^o \log(1 - p_{ai}^{ow}) f^{ow} \right) \\ &\quad + \frac{\delta_b - \delta_a}{(\delta_b + \rho)(\delta_a + \rho)} \left( u_n - \sum_{o,w} \lambda_n^o \log(1 - p_n^{ow}) f^{ow} \right) - c_a^b \end{aligned}$$

This expression is linear in  $u_{bj}$ ,  $u_{ai}$ ,  $u_n$ , and  $c_a^b$

We can write this in matrix form as

$$\kappa = A\theta \quad \implies \quad \theta = A^+ \kappa$$

Additional structure: relative symmetry along skill content



Two-stage MLE, competing risks with exponential hazards and two-sided censoring

1. Estimate wage change rates  $\chi$  and separation rates  $\delta$
2. Estimate hazards, imposing structure

Formulas

Likelihood

$$L(\mathbf{h}) = L \left( \underbrace{\lambda f}_{\text{Pr(offer arrives)}} \times \underbrace{p(\lambda, f, u, c, \hat{\chi}, \hat{\delta})}_{\text{Pr(offer is accepted)}} \right)$$

CCPs come from iterating the value function to a fixed point

VFI

Additional structure on offered wages, switching costs, flow utilities

$f$   $c$   $u$

I allow for two unobserved heterogeneity types

Reduced EM algorithm

Global optim

◀ Back



$$(\hat{\chi}_{ai}^{aw})_r = \frac{\sum_l q_{lr} \sum_s \mathbb{1}(a_s = a, i_s = i, d_s = WW, j_s = w)}{\sum_l q_{lr} \sum_s \mathbb{1}(a_s = a, i_s = i) t_s}$$

$$(\hat{\delta}_a)_r = \frac{\sum_l q_{lr} \sum_s \mathbb{1}(a_s = a, d_s = EN)}{\sum_l q_{lr} \sum_s \mathbb{1}(a_s = a) t_s}$$

Likelihood contribution of a single spell  $s$ :

$$L_s(h) = \prod_{a,i} \prod_{b,j} \left[ \left( h_{ai}^{bj} \right)^{\mathbb{1}(b_s=b, j_s=j)} \exp \left( -h_{ai}^{bj} t_s \right) \right]^{\mathbb{1}(a_s=a, i_s=i)}$$

Full likelihood:

$$L(h) = \sum_{\iota=1}^I \sum_{s=1}^{S_\iota} \log L_s(h)$$

Imposing structure:

$$L(\lambda, f, u, c) = \sum_{\iota=1}^I \sum_{s=1}^{S_\iota} \log L_s(\lambda f p(\lambda, f, u, c, \hat{\chi}, \hat{\delta}))$$

$m$ th iteration:

$$\left( \sum_o \lambda_a^o + \sum_w \chi_{ai}^{aw} + \delta_a + \rho \right) V_{ai}^{(m)} = u_{ai} + \sum_o \lambda_a^o V_{ai}^{(m-1)} + \sum_w \chi_{ai}^{aw} V_{aw}^{(m-1)} + \delta_a V_n^{(m-1)} + \sum_{o,w} \lambda_a^o \log \left( 1 + \exp \left( V_{ow}^{(m-1)} - V_{ai}^{(m-1)} - c_a^b \right) \right) f^{ow}$$

I calculate the CCPs as

$$p_{ai}^{bj} = \frac{\exp \left( V_{bj}^* - V_{ai}^* - c_a^b \right)}{1 + \exp \left( V_{bj}^* - V_{ai}^* - c_a^b \right)}$$

1. Estimate posterior type distribution using reduced-form full loglikelihood:

$$\max_{\mathbf{q}} \sum_{\ell} \log \left[ \sum_r \pi_r \left( L_{\ell r} \prod_s \tilde{L}_{sr} \right) \right] \rightsquigarrow \mathbf{q}_{\ell r}$$

2. Calculate wage change rates, job separation rates:

$$\left( \hat{\chi}_{ai}^{aw} \right)_r = \frac{\sum_{\ell} q_{\ell r} \sum_s \mathbb{1}(a_s = a, i_s = i, d_s = WW, j_s = w)}{\sum_{\ell} q_{\ell r} \sum_s \mathbb{1}(a_s = a, i_s = i) t_s}, \quad \left( \hat{\delta}_a \right)_r = \frac{\sum_{\ell} q_{\ell r} \sum_s \mathbb{1}(a_s = a, d_s = EN)}{\sum_{\ell} q_{\ell r} \sum_s \mathbb{1}(a_s = a) t_s}$$

3. Estimate remaining structural parameters using expected complete loglikelihood:

$$\max \sum_{\ell} \sum_r q_{\ell r} \sum_s \log L_{sr}(\lambda, f, u, c, \hat{\chi}, \hat{\delta})$$

Cutoffs:

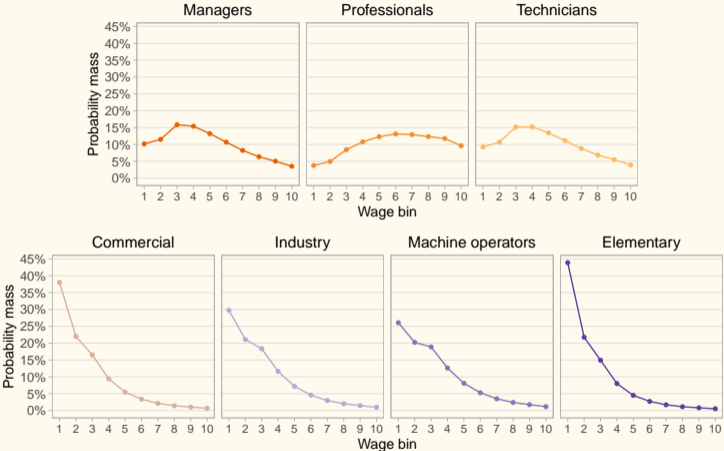
$$\phi_w = \begin{cases} \theta_1^\phi & \text{for } w = 1 \\ \phi_{w-1} + \exp(\theta_2^\phi + \theta_3^\phi \log w_w + \theta_4^\phi \log w_w^2) & \text{for } w > 1 \end{cases}$$

Logit structure:

$$f^{ow} = \begin{cases} \Lambda(\phi_w + \theta^o) & \text{for } w = 1 \\ \Lambda(\phi_w + \theta^o) - \Lambda(\phi_{w-1} + \theta^o) & \text{for } 1 < w < W \\ 1 - \Lambda(\phi_{W-1} + \theta^o) & \text{for } w = W \end{cases}$$

1. Optimize from “reasonable” starting values ( $R = 1$ )
2. Evaluate objective function in a Sobol sequence near local optimum
  - 1,000 points,  $\pm 50\%$  vicinity
3. If higher value found, optimize using corresponding arg max as starting values  
If not, global optimum found

Iterate steps 2-3 until convergence



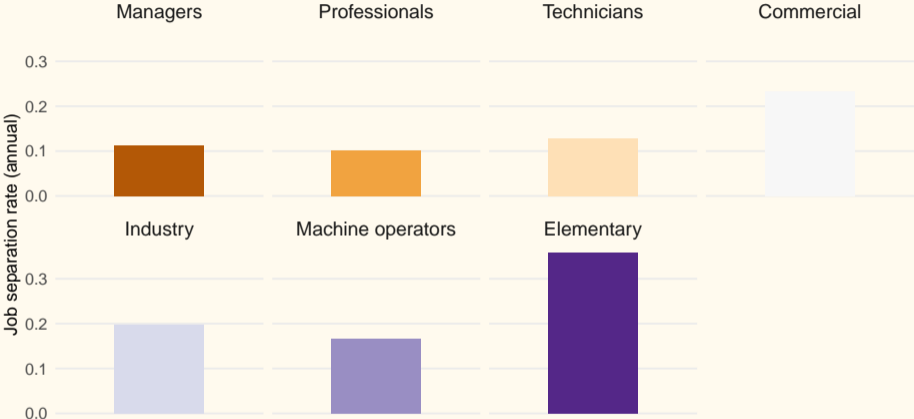
# Wage change rates

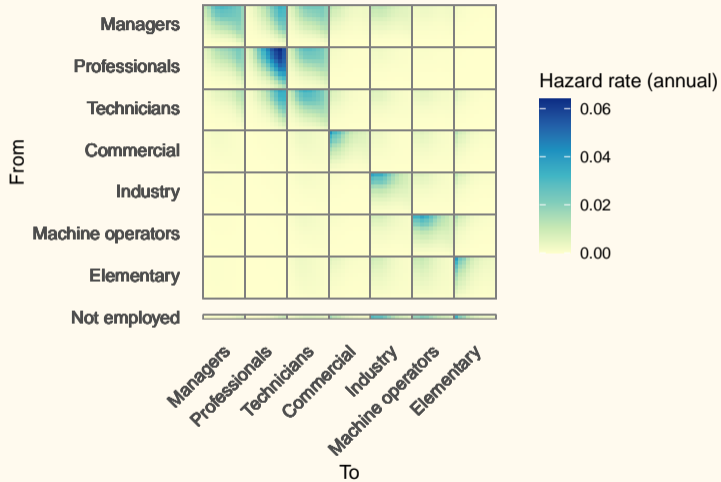




# Job separation rates

Estimates

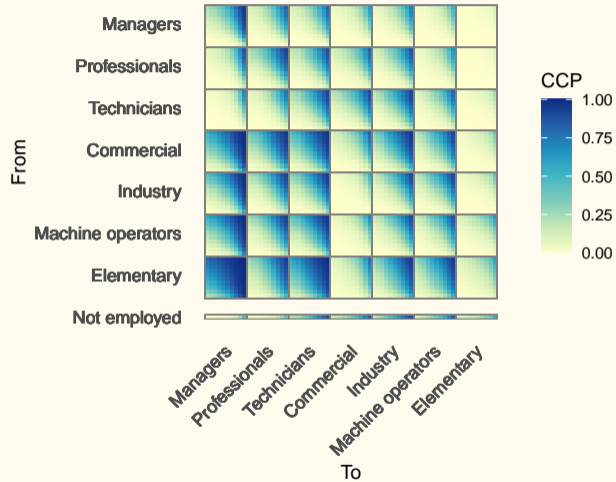




# Offer arrival rates

Estimates

From	Managers	0.54	0.40	0.62	0.72	0.71	0.44	0.62	4.05
	Professionals	0.66	0.63	0.53	0.06	0.08	0.08	0.13	2.19
	Technicians	0.57	0.47	0.49	0.12	0.11	0.18	0.57	2.51
	Commercial	0.02	0.01	0.04	0.96	0.04	0.10	0.65	1.81
	Industry	0.01	0.01	0.03	0.16	0.73	0.11	0.53	1.58
	Machine operators	0.00	0.00	0.03	0.09	0.17	0.83	0.29	1.42
	Elementary	0.00	0.00	0.03	0.18	0.10	0.14	0.94	1.39
	Not employed	0.36	0.24	0.12	0.31	0.57	0.70	1.01	3.31
		Managers	Professionals	Technicians	Commercial	Industry	Machine operators	Elementary	Total
	To								
	(annual rates)								



# Mean switching costs

Estimates

From

Managers	1.21	1.28	1.01	1.20	1.28	1.45	1.20
Professionals	3.18	1.16	1.24	1.01	1.26	1.64	2.06
Technicians	4.50	2.71	1.15	0.73	1.01	1.21	1.29
Commercial	1.60	1.46	0.83	2.05	1.00	1.01	1.43
Industry	1.71	1.82	1.15	3.05	1.56	0.75	1.01
Machine operators	1.94	2.36	1.38	3.07	2.28	1.73	0.80
Elementary	2.10	3.59	1.95	3.97	2.82	2.22	2.24
Not employed	5.42	4.21	1.33	1.01	1.01	1.01	0.00

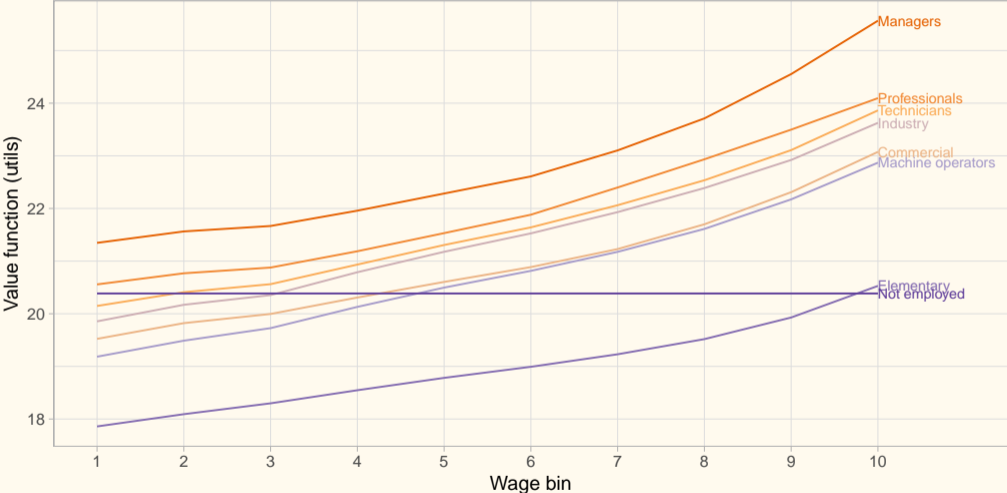
To

(utils)

◀ Back

# Value functions

Estimates



◀ Back

How much would a median-wage worker in occupation  $a$  have to be compensated to accept a machine operator job?

$$\psi_a + \beta \log \bar{w}_a = \psi_{MO} + \beta \log w_a^{MO}$$

Occupation	$\beta$	$\psi_a$	Comp. diff.
Managers	1.01	-0.20	0.89
Professionals		-0.52	0.65
Technicians		-0.24	0.85
Commercial		0.04	1.14
Industry		0.13	1.24
Machine operators		-0.09	-
Elementary		-0.69	0.55

- 0. Initialize  $G$  number of individuals in each occupation and wage bin  $G = 1,000$
- 1. Draw exponential durations using hazards  $h$ , wage change rates  $\chi$ , and job separation rates  $\delta$
- 2. Take minimum duration (competing hazards), record new job

Repeat steps 1-2 until sufficient years of cumulative durations are drawn (45 years)