

# Distorted Unemployment Beliefs and Stock Market Participation

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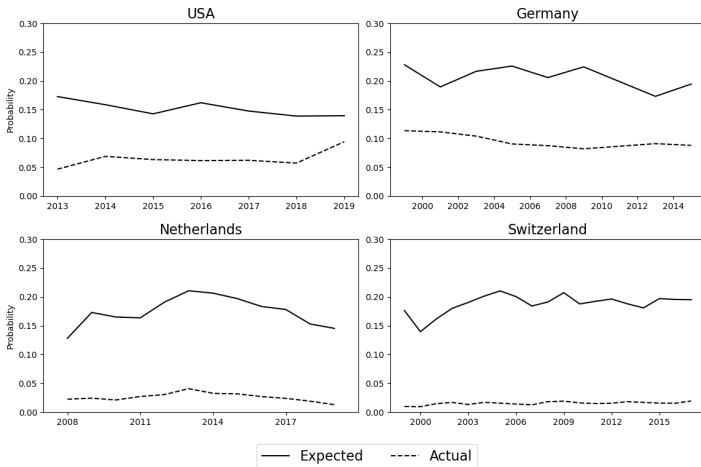
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# Motivation

- ▶ Important puzzle: Households hold very little stocks around the world.
- ▶ **Theory:** Traditional models have difficulties in explaining this fact.
- ▶ **Empirics:** 64.8% of respondents consider labor income risk important in their decision how/whether to allocate funds to the stock market (Choi & Robertson, 2020)

# An Empirical Fact



## What I find

- ▶ I find that individuals strongly overestimate the likelihood of losing their job.
- ▶ Empirically, increases in subjective unemployment expectations decrease the risky share.
- ▶ Incorporating distorted beliefs in a life-cycle model helps to match the evolution of wealth, equity share and participation rates with more plausible risk aversion estimates.

# Average Unemployment Beliefs

	USA		Germany		Netherlands		Switzerland	
	Exp.	Actual	Exp.	Actual	Exp.	Actual	Exp.	Actual
Total	0.155	0.067	0.195	0.098	0.176	0.026	0.189	0.015
Male	0.153	0.056	0.192	0.108	0.167	0.025	0.189	0.013
Female	0.156	0.080	0.198	0.087	0.186	0.027	0.189	0.019
< 35	0.136	0.078	0.235	0.165	0.158	0.030	0.189	0.028
35-50	0.152	0.061	0.193	0.105	0.180	0.024	0.202	0.014
> 50	0.173	0.067	0.157	0.055	0.182	0.025	0.173	0.009
No Degree	0.165	0.080	0.210	0.097	0.196	0.030	0.173	0.018
Voc. Training	0.155	0.092	0.202	0.100	0.187	0.028	0.199	0.016
University	0.149	0.055	0.173	0.089	0.155	0.021	0.186	0.014
Lowest Income	0.207	0.117	0.230	0.208	0.195	0.025	0.182	0.034
2	0.165	0.069	0.245	0.180	0.221	0.042	0.206	0.032
3	0.138	0.056	0.204	0.117	0.224	0.034	0.205	0.021
4	0.132	0.035	0.170	0.081	0.191	0.032	0.190	0.013
Highest Income	0.136	0.037	0.125	0.056	0.152	0.019	0.166	0.007

# Unemployment Expectations and Actual Unemployment

	USA	Germany		Switzerland		Netherlands	
	Actual	Actual	Actual	Actual	Actual	Actual	Actual
Unemployment Expectation	0.049*** (12.14)	0.080*** (54.93)	0.061*** (29.75)	0.015*** (17.67)	0.015*** (14.05)	0.041*** (19.42)	0.033*** (13.89)
Person FE	NO	NO	YES	NO	YES	NO	YES
Year FE	YES	YES	YES	YES	YES	YES	YES
Observations	8,867	87,301	73,980	72,181	69,577	26,182	24,312
Adjusted $R^2$	0.044	0.065	0.220	0.020	0.101	0.062	0.198

## Unemployment Expectations and the Risky Share

	Risky Share	Risky Share	Cond. Risky Share	Cond. Risky Share	Participation	Participation
Unemployment Expectation(t-1)	-0.006** (-2.10)	-0.006*** (-2.79)	-0.014** (-2.02)	-0.008* (-1.66)	-0.008 (-1.20)	-0.004 (-0.53)
Actual Unemployment	-0.005 (-0.33)	0.004 (0.34)	-0.060 (-1.39)	-0.024 (-0.73)	-0.040 (-1.04)	-0.020 (-0.50)
Person FE	NO	YES	NO	YES	NO	YES
Observations	6,888	5,997	1,748	1,324	4,235	3,164
Adjusted $R^2$	0.000	0.728	0.004	0.781	0.000	0.672

# Model

Agent optimizes lifetime utility:

$$E \sum_{t=1}^T \delta^{t-1} \left( \prod_{j=0}^{t-1} p_j \right) \left\{ \frac{C_{it}^{1-\gamma}}{1-\gamma} \right\}$$

Each period she decides how much to:

- ▶ consume ( $C_{it}$ )
- ▶ invest in risk-free asset ( $1 - \alpha_{it}$ )
- ▶ invest in risky asset ( $\alpha_{it}$ )



# Model

## Labor income process:

$$\log(Y_{it}) = f_{it} + \nu_{it} + \epsilon_{it}$$

### 1. Deterministic component:

$$f_{it} = \bar{f}_t + \alpha_i$$

### 2. Persistent component:

$$\nu_{it} = \nu_{i,t-1} + \zeta_{it}$$

where  $\zeta_{it} \sim \mathcal{N}(0, \sigma_\zeta^2)$  and  $\epsilon_{it} \sim \mathcal{N}(0, \sigma_\epsilon^2)$

# Model

## Unemployment:

$$\log(Y_{it+1}) = \begin{cases} \log(Y_{it+1})\kappa & \text{with probability } \omega_{t+1} \\ \log(Y_{it+1}) & \text{with probability } (1 - \omega_{t+1}) \end{cases}$$

## Subjective unemployment beliefs:

$$E_t^{subj}[\log(Y_{it+1})] = \begin{cases} \log(Y_{it+1})\kappa & \text{with probability } \omega_{t+1}^{subj.} \\ \log(Y_{it+1}) & \text{with probability } (1 - \omega_{t+1}^{subj.}) \end{cases}$$

where  $\omega_{t+1}^{subj.} \gg \omega_{t+1}$

# Model

## Bellman equation:

$$V_{it}(X_{it}) = \max_{C_{it} \geq 0, 0 \leq \alpha_{it} \leq 1} [U(C_{it}) + \delta p_t E_t V_{i,t+1}(X_{i,t+1})] \text{ for } t < T,$$

where:

$$X_{i,t+1} = Y_{i,t+1} + (X_{it} - C_{it})(\alpha_{it} R_{t+1} + (1 - \alpha_{it}) R_f) - 1^{\alpha_{it} > 0} \Phi$$

# Preset Parameters

Parameter		Value	Source
<i>Agent:</i>			
Age of first employment	$t_0$	23	
Age of retirement	$t_R$	65	
Maximum age	$T$	100	
<i>Assets:</i>			
Average return risky asset	$\mu_s$	0.082	S&P500 historical returns
Standard deviation risky asset	$\sigma_s$	0.159	S&P500 historical returns
Proportional management fee		0.01	Catherine (2021)
Return on risk-free asset	$R_f$	1.02	Catherine (2021)
<i>Income Process:</i>			
Effect of <i>age</i> on log wage	$f_1$	0.115	PSID
Effect of $age^2/10$ on log wage	$f_2$	-0.020	PSID
Effect of $age^3/100$ on log wage	$f_3$	0.001	PSID
Constant	$f_0$	-1.620	PSID
Std. of transitory income shocks	$\sigma_\epsilon$	0.290	PSID
Std. of permanent income shocks	$\sigma_\zeta$	0.117	PSID
Std. of initial income distribution	$\sigma_\alpha$	0.139	PSID
Unemployment probability	$\omega_t$		Choi et al. (2015)
Unemployment income	$\kappa$	0.065	PSID
Replacement ratio	$\lambda$	0.671	PSID

## Structural Estimation

**Parameters to be estimated:** discount factor, risk aversion, participation cost.

**Targeted moments:** mean of conditional/unconditional risky share, participation, and wealth averaged over *three* periods.

Minimize:

$$(\mathbf{m} - \hat{\mathbf{m}}(\gamma, \delta, \Phi))' \mathbf{W} (\mathbf{m} - \hat{\mathbf{m}}(\gamma, \delta, \Phi))$$

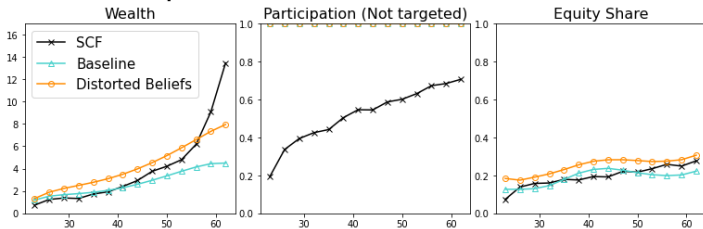
→ Simulated method of moments (SMM).

# Results

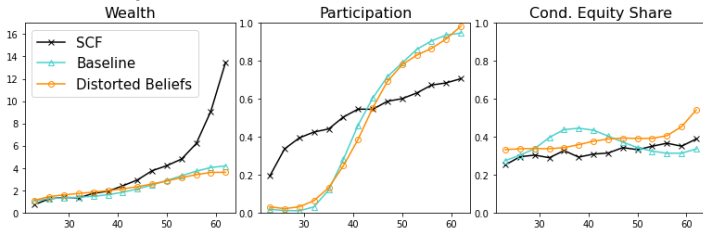
	Baseline		Distorted expectations	
	(1)	(2)	(3)	(4)
<i>Panel A: Estimated Parameters</i>				
Relative risk aversion	18.056	12.739	11.846	7.792
Discount factor	0.455	0.623	0.749	0.719
Fixed participation cost		0.0166		0.0147
<i>Panel B: Targeted life-cycle moments</i>				
Risky share	✓		✓	
Conditional risky share		✓		✓
Participation rate		✓		✓
Wealth	✓	✓	✓	✓

# Results

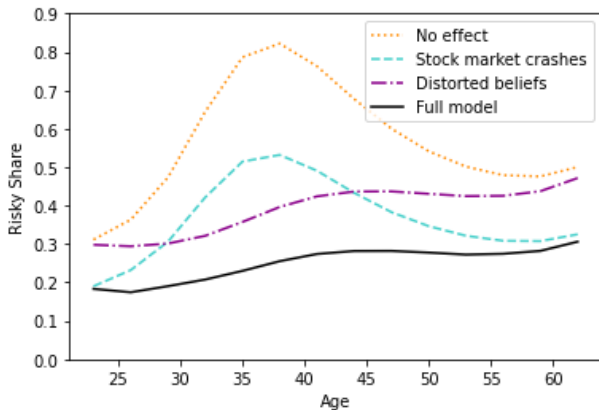
## Without Participation Cost



## With Participation Cost



# Effect Decomposition





# Conclusion

- ▶ Individuals strongly overestimate labor income disaster risk.
- ▶ Incorporating distorted beliefs into a life-cycle model improves model fit.
- ▶ Considering elicited beliefs helps to understand financial decision-making.

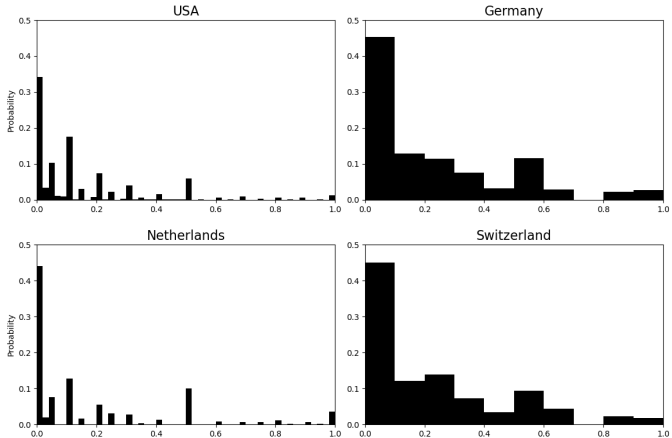
## Data

	USA		Germany		Netherlands		Switzerland	
	Mean	Std.	Mean	Std.	Mean	Std.	Mean	Std.
<i>Demographics</i>								
Female	0.49	0.50	0.52	0.50	0.51	0.50	0.52	0.50
Age	50.05	15.14	46.74	17.42	47.46	17.28	48.40	17.63
Net Income	.	.	1463	1252	1247	6096	4918	4942
<i>Education</i>								
No Degree	0.34	0.47	0.13	0.34	0.44	0.50	0.23	0.42
Vocational	0.13	0.34	0.57	0.50	0.24	0.43	0.40	0.49
University	0.53	0.50	0.19	0.40	0.32	0.47	0.37	0.48
<i>Employment</i>								
Employed	0.68	0.47	0.59	0.49	0.57	0.50	0.61	0.49
Unemployed	0.09	0.29	0.07	0.26	0.03	0.17	0.01	0.11
<i>Jobloss</i>								
Expectation	0.15	0.21	0.19	0.25	0.18	0.26	0.19	0.24
Actual	0.06	0.24	0.10	0.30	0.03	0.16	0.02	0.12

## Persistence of Unemployment Beliefs

	Germany		Netherlands		Switzerland	
	Unemployment Exp.		Unemployment Exp.		Unemployment Exp.	
Unemp. Exp.(t-2)	0.389*** (68.51)	0.391*** (68.49)				
Unemp. Exp.(t-1)			0.466*** (83.78)	0.466*** (83.61)	0.416*** (36.15)	0.415*** (35.93)
Year FE	NO	YES	NO	YES	NO	YES
Observations	50,353	50,353	76,147	76,147	18,199	18,199
Adjusted $R^2$	0.146	0.149	0.211	0.213	0.161	0.165

# Distributon of Unemployment Expectations

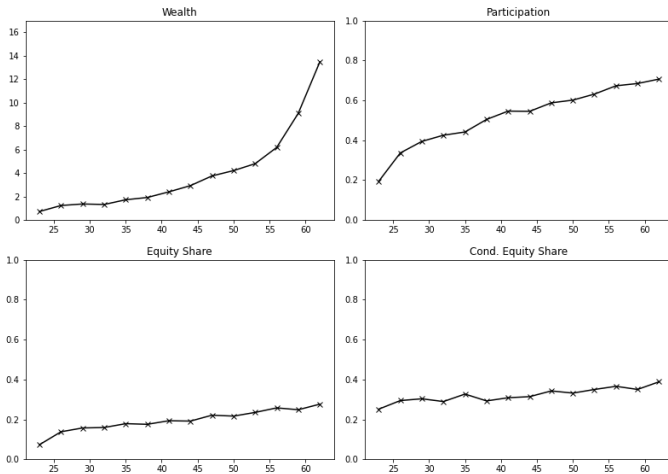


# SCF Summary Statistics

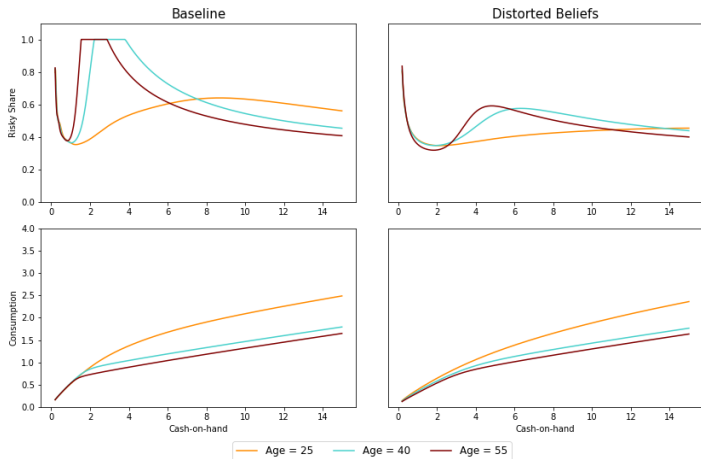
	Mean	Std. Deviation	Observations
Age	43.36	12.55	136,285
Wealth	285,847.79	1,145,659.09	136,285
Labor income	77,280.89	134,534.22	136,285
Stock market participation	0.49		136,285
Equity share	0.17	0.46	116,599
Cond. equity share	0.30	0.58	70,677

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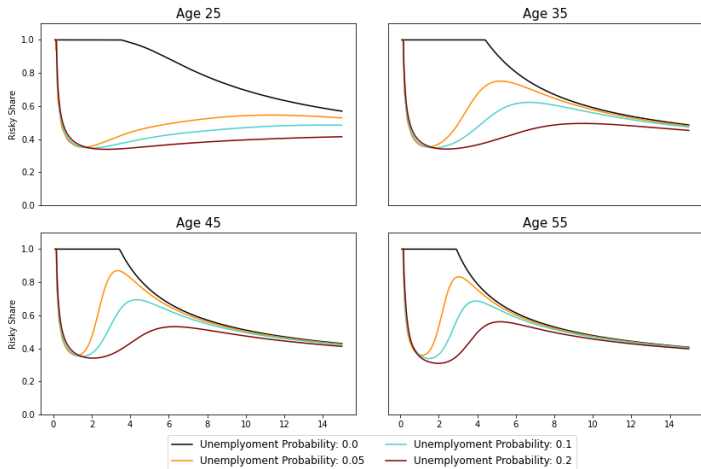
# Model Moments



# Discussion



# Discussion





# Effect Decomposition

