

# Same Sex Marriage, The Great Equalizer

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- Q:** Why would someone lose from allowing same sex marriage?
- A:** Because same sex marriage changes the *expectations* of marriage market participants, changing the outcomes of everyone, **making genders equal**

## Baseline Model

- Continuum of *types*, generically denoted  $x, y \in [0, 1]$ , total mass 1, cdf  $G(\cdot)$
- Family production function  $f(x, y)$ , increasing in both arguments, symmetric, continuous
- If married, output is shared by Nash bargaining:

$$v(x) + \overbrace{\frac{f(x, y) - v(x) - v(y)}{2}}^{s(x, y)}$$

- If not married, pay search costs  $c > 0$ . No time discount

$$v(x) = -c + \int_0^1 \max \left[ v(x) + \frac{f(x, y) - v(x) - v(y)}{2}, v(x) \right] dG(y)$$

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$$v(x) = -c + \int_0^1 \max \left[ v(x) + \frac{f(x, y) - v(x) - v(y)}{2}, v(x) \right] dG(y) \Rightarrow$$

$$2c = \int_0^1 \max [s(x, y), 0] dG(y) = \int_{\{y: s(x, y) \geq 0\}} s(x, y) dG(y)$$

## Results of Atakan (2006)

$$2c = \int_0^1 \max [s(x, y), 0] dG(y) = \int_{y:s(x,y) \geq 0} s(x, y) dG(y)$$

- Under regularity conditions, equilibrium  $v(x) : [0, 1] \rightarrow R$  exists, generically not unique;  $v(x)$  is continuous
- Under supermodularity of  $f(x, y)$ :
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  - Positive assortative matching

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  - Positive assortative matching
- However, total disregard for gender.

## With Different Genders

- With two genders,  $\{m, f\}$ , eqm conditions are

$$2c = \int_0^1 [f(x, y) - v_m(x) - v_f(y)]^+ dG(y)$$

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- (Conditional) asymmetry:  $v_m(x) \neq v_f(x)$ .

## Equilibrium

We generalize over sexual orientations  $t \in T$ :

$$a(t_1, t_2) = 0 \Leftrightarrow t_1 \text{ can't marry } t_2.$$

$$a(t_1, t_2) = 1 \Leftrightarrow t_1 \text{ can marry } t_2.$$

Under Lipschitz continuity, equilibrium exists and satisfies the constant surplus condition:

$$2c = \sum_j a(t, j) q_j \int_y [f(x, y) - v_t(x) - v_j(y)]^+ dG_j(y).$$

## Easiest Way

Everyone can marry everyone:

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### Proposition

*In every equilibrium,  $v_m(x) = v_f(x)$ .*

## Proof

If there is  $x_0$  where  $v_m(x_0) > v_f(x_0)$ :

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- and therefore

$$\mathbf{E} [f(x, y) - v_m(x) - v_f(y)]^+ < \mathbf{E} [f(x, y) - v_f(x) - v_f(y)]^+$$

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- for the same reason

$$\mathbf{E} [f(x, y) - v_m(x) - v_m(y)]^+ < \mathbf{E} [f(x, y) - v_f(x) - v_m(y)]^+$$

If the total expected surplus of  $m$  gender is  $2c$ , the total expected surplus of  $f$  must be above  $2c$ !

## A Bit Harder Way

Everyone can marry opposite gender

$$2c = \int_0^1 [f(x, y) - v_m(x) - v_f(y)]^+ dG(y)$$

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## A Bit Harder Way

Everyone can marry opposite gender and there is a *chance* you can marry same gender

$$2c = \int_0^1 [f(x, y) - v_m(x) - v_f(y)]^+ dG(y) +$$

$$+ p \int_0^1 [f(x, y) - v_m(x) - v_m(y)]^+ dG(y)$$

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In every equilibrium with  $p > 0$ ,  $v_m(x) = v_f(x)$ .

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Take  $\Delta_0 = \max_x \underbrace{v_m(x) - v_f(x)}_{\Delta(x)}$ , and  $x_0$  is the maximand. Assume

$\Delta_0 \geq \max_x (v_f(x) - v_m(x))$ ; rename genders otherwise.

## Proof

$$\begin{aligned} \int [f(x, y) - v_f(x_0) - v_f(y) - \Delta(y)]^+ dG(y) &\geq \\ &\geq \int [f(x, y) - v_f(x_0) - v_f(y) - \Delta_0]^+ dGy. \\ p \int [f(x, y) - v_f(x_0) - v_f(y)]^+ dG(y) &\geq \\ \geq p \int [f(x, y) - v_f(x_0) - v_f(y) - \Delta_0 - \Delta(y)]^+ dGy. \end{aligned}$$

Can there be =?

Not =

$$\begin{aligned} \int [f(x, y) - v_f(x_0) - v_f(y) - \Delta(y)]^+ dG(y) &= \\ &= \int [f(x, y) - v_f(x_0) - v_f(y) - \Delta_0]^+ dGy \end{aligned}$$

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$$\Rightarrow \Delta(y) = -\Delta_0.$$

## Even Harder Way

All can marry opposite gender

$$2c = \int_0^1 [f(x, y) - v_{mh}(x) - v_{fh}(y)]^+ dG(y)$$

$$2c = \int_0^1 [f(x, y) - v_{mb}(x) - v_{fh}(y)]^+ dG(y)$$

## Even Harder Way

All can marry opposite gender, *some* can marry same gender

$$2c = \int_0^1 [f(x, y) - v_{mh}(x) - v_{fh}(y)]^+ dG(y) +$$

$$+ q \int_0^1 [f(x, y) - v_{mh}(x) - v_{fb}(y)]^+ dG(y)$$

$$2c = \int_0^1 [f(x, y) - v_{mb}(x) - v_{fh}(y)]^+ dG(y) +$$

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 \end{aligned}$$

### Proposition

In equilibrium with  $q > 0$ ,  $v_{mh}(x) = v_{fh}(x) \leq v_{mb}(x) = v_{fb}(x)$ .

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  - Somewhat harder to achieve if it is *harder* to partake in same sex marriage
  - Even harder if some people *cannot* partake in same sex marriage
- Mathematically, requires symmetry across distributions
  - Hard to hope for equality without symmetry