

THE SOCIAL COST OF CARBON UNDER CLIMATE VOLATILITY RISKS

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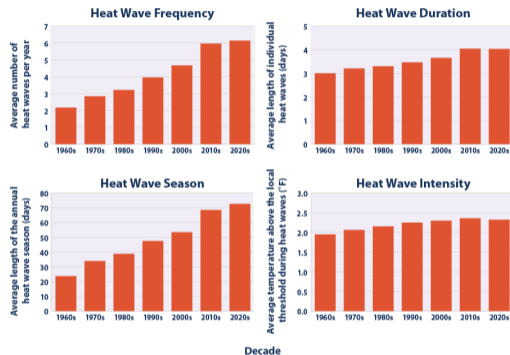
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MOTIVATION

- Extreme weather events will become more frequent and more intense (i.e. **more volatile**) with human-induced climate change (The National Climate Assessment (2018), IPCC (2021))
- But the timing and size of rising frequency and/or intensity is uncertain.
- Such uncertainty about climate volatility has not been studied by climate economists (**climate volatility risk**)

Heat Wave Characteristics in the United States by Decade, 1961–2021



Data source: NOAA (National Oceanic and Atmospheric Administration), 2022. Heat stress datasets and documentation. Provided to EPA by NOAA in February 2022.

For more information, visit U.S. EPA's "Climate Change Indicators in the United States" at www.epa.gov/climate-indicators.

CLIMATE VOLATILITY AND CLIMATE VOLATILITY RISK

Climate volatility

- Uncertainty about climate damage
 - The arrival of heatwaves is stochastic.
 - The damage from heatwave is a random variable.

Climate volatility risk

- Uncertainty about climate volatility itself (higher-order uncertainty)
 - How much more frequent will heatwaves be by the end of this century? (Uncertainty about how the frequency changes over time)
 - Will the distribution of damage size from an individual heatwave change by 2050? (Uncertainty about how the distribution shifts over time)

IN THIS PAPER

Goal: The impact of climate volatility risk on the Social Cost of Carbon (SCC)

- SCC: a monetary metric for the damage caused by an additional ton of carbon emission
- A guideline for climate policy in regulatory impact assessments (Greenstone et al. 2013, Watkiss and Hope 2011)
- Determined by climate-economic integrated assessment models (IAMs)

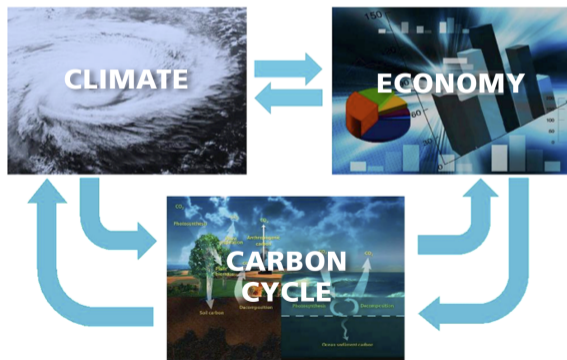


FIGURE: The interdependence of a climate-economic IAM (Krusell and Hassler (2013))

Model: Stochastic dynamic climate-economic IAM

(Extension to S-DICE (Cai and Lontzek (2019))); with richer risk structure of the climate volatility)

- Calculate SCC using ideas from consumption CAPM
- Two policy scenarios: Business As Usual (BAU), Optimal Abatement (OA)

Main results:

- Climate volatility risk substantially increases the SCC (as important as the climate volatility itself).
- Two types of volatility risk (frequency vs. size): Given the same expected climate damage, more severe disasters (size) leads to higher SCC than more frequent disasters.
- SCC is larger in the OA scenarios than the BAU scenarios (all else being equal).

STOCHASTIC IAM: CLIMATE MODEL

Mechanism: Carbon emission \rightarrow Mean global surface temperature \rightarrow More climate-related disasters

Emissions: two alternative specifications

- Exogenous: baseline scenario from Nordhaus (2017)
- Endogenous: proportional to aggregate output
- Here: focus on the **exogenous** setup
 - ▶ Analytical results
 - ▶ Endogenizing emissions does not qualitatively change the results

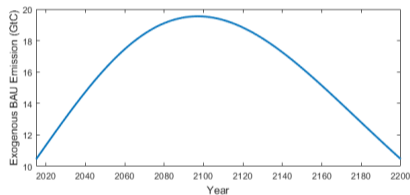


FIGURE: Exogenous carbon emissions (GtC) in the business-as-usual scenario

STOCHASTIC IAM: CLIMATE MODEL

Temperature increases linearly in actual emissions

$$dT_t = \underbrace{\chi}_{\text{Sensitivity}} \underbrace{(1 - u_t)E_t}_{\text{Actual Emission}} dt, \quad \text{where } u_t \in [0, 1] \text{ is the abatement control rate}$$

Climate disasters: a compound Poisson process causing economic losses

- **Climate volatility** measured by
 - ▶ Frequency: arrival rate $\lambda_{2,t}$ which increases in T_t
 - ▶ Size (disaster intensity): random variable J_2
- **Climate volatility risk:** stochastic shock to the climate volatility
 - ▶ One-off, irreversible, positive Poisson shocks
 - ▶ Two types of shocks: on the frequency or (the distribution of) the disaster size

STOCHASTIC IAM: STOCHASTIC PURE EXCHANGE ECONOMY

- Endowment Y_t

$$dY_t = \underbrace{\mu Y_t dt}_{\text{econ. growth}} + \underbrace{\sigma Y_t dZ_t}_{\text{econ. volatility}} - \underbrace{J_1 Y_{t-} dN_{1,t}}_{\text{econ. disasters}} - \underbrace{J_2 Y_{t-} dN_{2,t}}_{\text{climate disasters}}$$

- ▶ Disasters follows Poisson processes (Barro-type rare disasters as in Barro (2009), Barro (2009))

	Arrival rate	Size
Economic disasters N_1	λ_1	J_1
Climate disasters N_2	$\lambda_{2,t}$	J_2

- Endowment $Y_t = \text{Consumption } C_t + \text{Abatement } A_t$

- ▶ Abatement cost A_t increases in the emission control rate u_t

PREFERENCES

- Representative agents with Duffie-Epstein preferences (Duffie and Epstein (1992))
- In the Optimal Abatement scenario, agents choose emission control rate u_t to maximize the welfare:

$$V_0 = \max_{u_t} \mathbb{E}_0 \int_0^{\infty} f(C_t, V_t) dt$$

where the utility flow $f(C, V) = \frac{\beta}{1-\frac{1}{\epsilon}} \frac{C^{1-\frac{1}{\epsilon}} - [(1-\gamma)V]^{\frac{1}{\zeta}}}{[(1-\gamma)V]^{\frac{1}{\zeta}-1}}$ with

- ▶ risk aversion γ
 - ▶ elasticity of intertemporal substitution (EIS) $\epsilon \neq 1$
 - ▶ $\zeta = \frac{1-\gamma}{1-\frac{1}{\epsilon}}$
 - ▶ time discount rate β
- In the BAU scenario, set $u_t = 0$

SOCIAL COST OF CARBON (SCC)

- SCC: The marginal damage of carbon emissions (scaled by marginal utility of consumption)

$$SCC_0 = -\chi \frac{\partial V_0 / \partial T_0}{f_C(C_0, V_0)}$$

- An explicit expression to identify the impact of climate volatility risk on the SCC

$$SCC_0 \approx \int_0^\infty \underbrace{\left(\int_0^t \chi \frac{\partial \lambda_{2,s}}{\partial T_0} \frac{1}{\alpha_{2,s} + 1 - \gamma} ds \right) \mathbb{E}_0 C_t}_{\text{Certainty Equivalent (CE) of damage from marginal emission}} \cdot \underbrace{\exp \left(- \int_0^t r_s^{(CDR)} ds \right)}_{\text{Stochastic Discount Factor (SDF)}} dt$$

where $r^{(CDR)}$ is the growth-adjusted consumption discount rate.

SCC AT $t = 0$

$$SCC_0 \approx \int_0^{\infty} CE_t \cdot SDF_t dt$$

The impact of climate volatility risk

- on **Certainty Equivalent (CE)** : positive (Disasters are getting worse in the future.)
- on **Stochastic Discount Factor (SDF)**: unclear ex ante
 - ▶ SDF is negatively correlated with the growth-adjusted consumption discount rate $r^{(CDR)}$

$$r_t^{(CDR)} \approx \underbrace{r_t^f}_{\text{Risk free rate}} + \underbrace{r_{p,t}}_{\text{Risk premium}}$$

- ▶ Numerically solve each term

NUMERICAL SOLUTIONS

- Calibration:

- ▶ Endowment: $\mu = 3\%$ (growth), $\sigma = 2.5\%$ (volatility), $\lambda_1 = 3.5\%$ (arrival rate of economic disasters), $\alpha_1 = 6.5$ (\rightarrow mean economic disaster size $\mathbb{E}J_1 = 13.3\%$)
- ▶ Preference: $\epsilon = 1.5, \gamma = 4.3, \beta = 0.026$
- ▶ Climate disaster: $\bar{\lambda}^{(L)} = 6\%$, $\alpha_{2,t=0} = 6.5$ (\rightarrow mean climate disaster size $\mathbb{E}J_2 = 1.5\%$)
- ▶ Abatement costs: $A_t = 0.0741e^{-0.019t}u_t^{2.8}$ (Nordhaus-type abatement cost function)
- ▶ Temperature: $\chi = 1.8^\circ\text{C}/Tt\text{C}$ (transient climate response to cumulative emissions)

- Climate Volatility Risk: Calibration is difficult for lack of time series data and volatility models

\implies Therefore we experiment with

- ▶ different sizes of Poisson shocks on either the disaster frequency or the (average) disaster size (e.g. $\times 2, \times 4$)
- ▶ different arrival rate of such Poisson shocks to volatility

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HOW CLIMATE VOLATILITY RISK AFFECTS SCC

- $SCC_0 \approx \int_0^\infty CE_t \cdot SDF_t dt$
- where SDF_t is negatively correlated with growth-adjusted consumption discount rate

$$r_t^{(CDR)} \approx \underbrace{r_t^f}_{\text{Risk free rate}} + \underbrace{r_{p,t}}_{\text{Risk premium}}$$

We find numerically that under climate volatility risk

- Risk-free rate \downarrow , risk premium \uparrow ▶ Analytical decomposition of r^f and r_p
- $CE \uparrow$, discount rate $r^{(CDR)} \downarrow$ (i.e. $SDF \uparrow$) \implies Larger SCC
- Given the same expected climate damage, a positive shock on the size of a single disaster leads to larger CE (and thus larger SCC) than a shock on the disaster frequency.
Intuitively, under risk aversion, utility is concave. Therefore an increase in disaster size leads to larger loss of marginal utility than an increase in disaster frequency.

BAU: SHOCK TO FREQUENCY VS. SIZE

TABLE: SCC (\$/tC) in 2025, 2050 and 2100 in the BAU scenario. Disaster frequency/size is doubled (Multiplier=2) or quadrupled (Multiplier=4) after the shock arriving at rate 0.01.

Multiplier	Year	(a) Frequency	(b) Size
2	2025	505	522
	2050	955	998
	2100	2911	3044
4	2025	771	902
	2050	1476	1707
	2100	3976	4543

Given the same expected climate damage ("Multiplier"), a positive shock to the size of climate disasters leads to a higher SCC

BAU: HOW MUCH CLIMATE VOLATILITY RISK AFFECTS THE SCC

TABLE: SCC (\$/tC) under BAU in Year 2025. The disaster *frequency* is doubled after the shock with arrival rate 0.01.

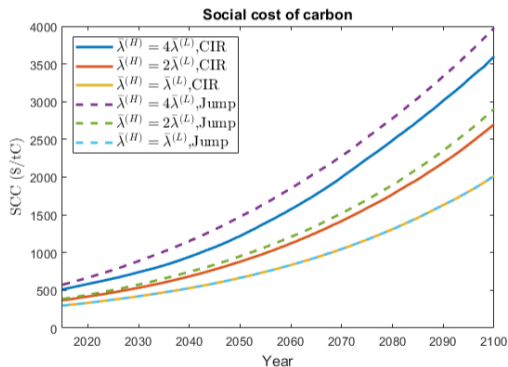
Risk aversion γ	EIS ϵ	(a) Stochastic shock	(b) Deterministic shock
4.3	1.5	505	377
6	1.5	359	268
4.3	0.75	243	173
6	0.75	360	242

Column (a): shock is stochastic (with climate volatility risk);(b) shock is deterministic (without climate volatility)

- Under the same shock size, SCC is substantially larger if the shock arrives stochastically.
- **The stochasticity** of climate volatility substantially increases SCC
- Qualitative implications robust under different preference parameters (γ and ϵ)

ALTERNATIVE VOLATILITY RISK MODEL

- What looks like an instantaneous jump on a geographical time scale unfolds more gradually on a regular timescale (Dietz et al. (2021))



- **Model:** Gradual unfold tipping on disaster frequency (CIR process), instead of a Poisson jump.
- **Figure:** SCC in the BAU scenario under different volatility models
 - ▶ Solid lines: gradual
 - ▶ Dashed lines: jump
- **Result:** A more gradual increase in volatility (*solid*) leads to a lower SCC than an abrupt increase (*dashed*)

CONCLUSION

- The stochasticity of climate volatility substantially increases the SCC (**as important as the climate volatility itself**)
- Given the same expected climate damage, an increase in the size of climate disasters leads to a higher SCC than an increase in the disaster frequency.
- All else being equal, the SCC is larger in the OA scenario than the BAU scenario.
- Smoothing the increase in climate volatility leads to lower SCCs.
- Endogenizing carbon emissions does not qualitatively change the results obtained under exogenous emissions.

Thank you!

RISK-FREE RATE AND RISK PREMIUM

Both the risk-free rate and the risk premium are affected by climate volatility risk (**directly** and **indirectly**)

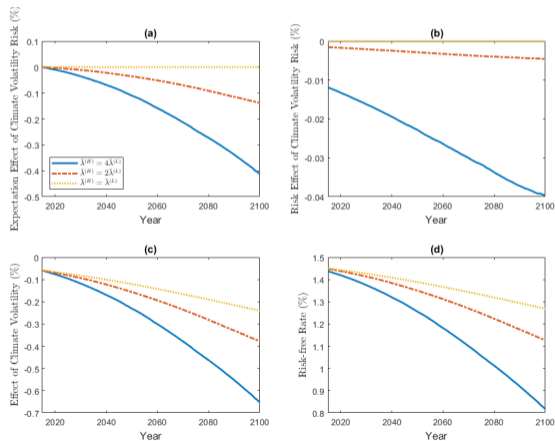
$$r_t^f = \underbrace{\beta + \frac{\mu_{C,t}}{\epsilon} - \frac{\gamma}{2} \left(1 + \frac{1}{\epsilon}\right) \sigma^2}_{\text{Standard}} + \underbrace{\lambda_1 \left(\frac{\gamma - 1/\epsilon}{\alpha_1 + 1 - \gamma} - \frac{\gamma}{\alpha_1 - \gamma} \right)}_{\text{Econ. disasters}(<0)} + \underbrace{\lambda_{2,t} \left(\frac{\gamma - 1/\epsilon}{\alpha_{2,t} + 1 - \gamma} - \frac{\gamma}{\alpha_{2,t} - \gamma} \right)}_{\text{Clim. disasters}(<0)} + \underbrace{\lambda_{0,t} \mathcal{J}_{f,t}}_{\text{Regime shift risk}(\leq 0)}$$

$$r_{p,t} = \underbrace{\gamma \sigma^2}_{\text{Standard}} + \underbrace{\lambda_1 \left[\frac{-1}{\alpha_1 + 1} + \frac{\gamma}{\alpha_1 - \gamma} + \frac{1 - \gamma}{\alpha_1 + 1 - \gamma} \right]}_{\text{Econ. disasters}(>0)} + \underbrace{\lambda_{2,t} \left[\frac{-1}{\alpha_{2,t} + 1} + \frac{\gamma}{\alpha_{2,t} - \gamma} + \frac{1 - \gamma}{\alpha_{2,t} + 1 - \gamma} \right]}_{\text{Clim. disasters}(>0)} + \underbrace{\lambda_{0,t} \mathcal{J}_{rp,t}}_{\text{Regime shift risk}(>0)}$$

▶ back

RISK-FREE RATES UNDER BAU

FIGURE: Risk-free rates under BAU and exogenous emissions: (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d) Risk-free rate

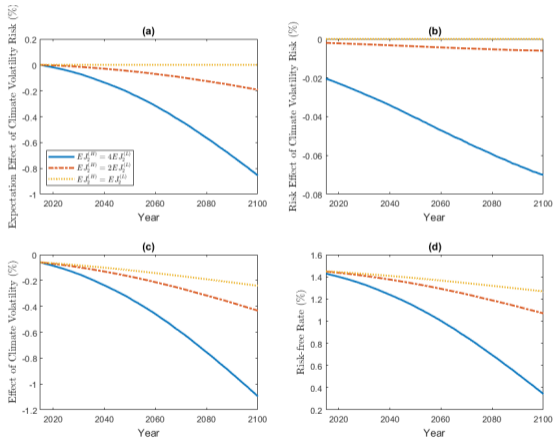


Higher frequency
 $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}, 2\bar{\lambda}^{(L)}, \bar{\lambda}^{(L)}$:

- All risks: negative
- Magnitude increases in $\bar{\lambda}^{(H)}$
- 1st-order risk \sim Expectation channel $>$ Risk channel

— $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}$
 - - - $\bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)}$
 ···· $\bar{\lambda}^{(H)} = \bar{\lambda}^{(L)}$

FIGURE: Risk-free rates under BAU and exogenous emissions: (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d) Risk-free rate



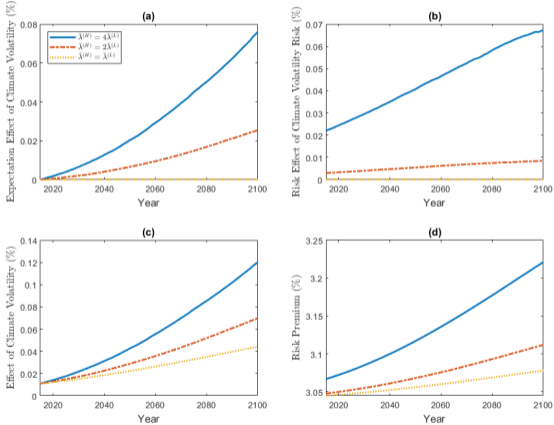
Higher intensity

$$EJ_2^{(H)} = 4EJ_2^{(L)}, 2EJ_2^{(L)}, EJ_2^{(L)}:$$

- Magnitudes in (a), (b) and (c) slightly larger than switching to a regime with higher frequency
- Slightly lower risk-free rate

$$\begin{aligned} & \text{—} EJ_2^{(H)} = 4EJ_2^{(L)} \\ & \text{- - -} EJ_2^{(H)} = 2EJ_2^{(L)} \\ & \text{⋯} EJ_2^{(H)} = EJ_2^{(L)} \end{aligned}$$

FIGURE: Risk premia under BAU and exogenous emissions: (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d) Risk premia



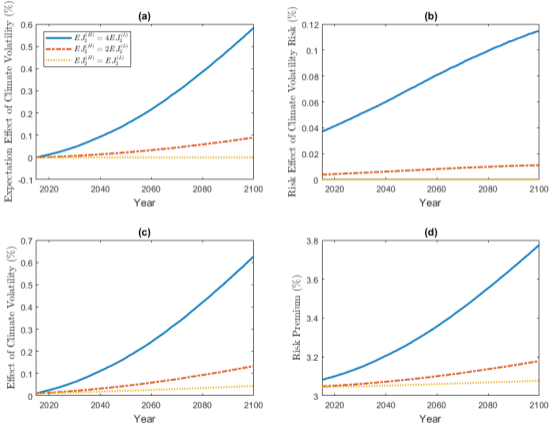
Higher frequency in the new regime:

- Positive and increasing in $\bar{\lambda}^{(H)}$
- Climate volatility risk ((a)+(b)) as important as climate volatility itself (c)

$$\begin{aligned} & \text{— } \bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)} \\ & \text{- - } \bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)} \\ & \cdots \bar{\lambda}^{(H)} = \bar{\lambda}^{(L)} \end{aligned}$$

▶ Exogenous Emission under BAU

FIGURE: Risk premia under BAU and exogenous emissions: (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d) Risk premia



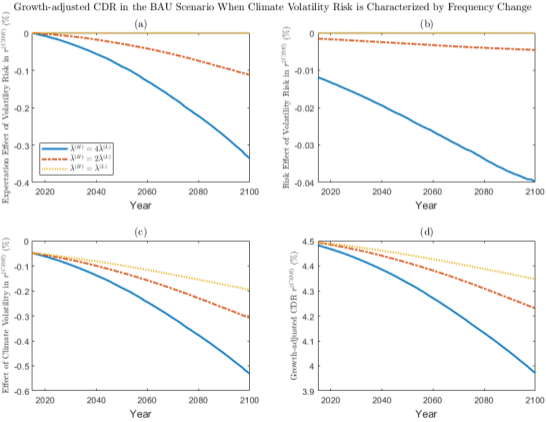
Higher intensity:

- Positive and increasing in $\mathbb{E}J_2^{(H)}$
- Climate volatility risk ((a)+(b)) as important as climate volatility itself (c)
- (a) and (c) substantially larger than switching to a high-frequency regime
- ⇒ Higher risk premium

$$\begin{aligned}
 & \text{— } EJ_2^{(H)} = 4EJ_2^{(L)} \\
 & \text{- - } EJ_2^{(H)} = 2EJ_2^{(L)} \\
 & \cdots EJ_2^{(H)} = EJ_2^{(L)}
 \end{aligned}$$

▶ Exogenous Emission under BAU

FIGURE: Growth-adjusted consumption discount rate under BAU and exogenous emissions: (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d) Growth-adjusted consumption discount rate



Higher frequency
 $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}, 2\bar{\lambda}^{(L)}, \bar{\lambda}^{(L)}$:

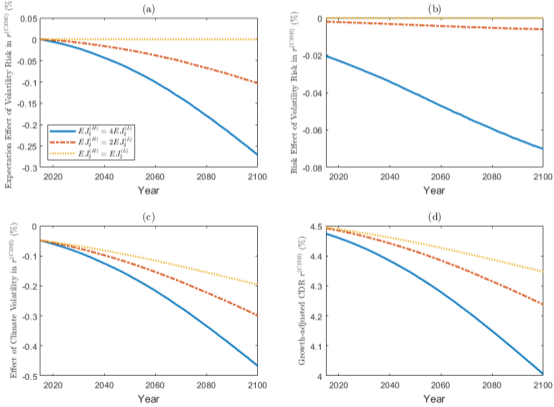
- All risks: negative
- Magnitude increases in $\bar{\lambda}^{(H)}$
- $r^{(CDR)}$ decreases in $\bar{\lambda}^{(H)}$

— $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}$
 - - - $\bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)}$
 $\bar{\lambda}^{(H)} = \bar{\lambda}^{(L)}$

▶ Exogenous Emission under BAU

FIGURE: Growth-adjusted consumption discount rate under BAU and exogenous emissions: (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d) Growth-adjusted consumption discount rate

Growth-adjusted CDR in the BAU Scenario When Climate Volatility Risk is Characterized by Intensity Change



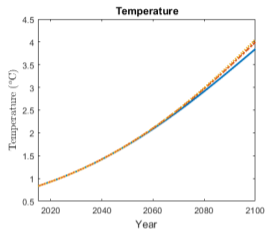
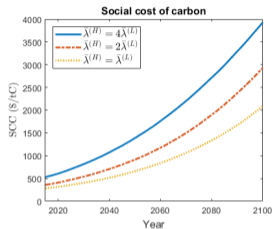
Higher intensity
 $EJ_2^{(H)} = 4EJ_2^{(L)}, 2EJ_2^{(L)}, EJ_2^{(L)}$:

● $r^{(CDR)}$ does not differ much from the case when the new regime has higher disaster frequency

- $EJ_2^{(H)} = 4EJ_2^{(L)}$
- $EJ_2^{(H)} = 2EJ_2^{(L)}$
- $EJ_2^{(H)} = EJ_2^{(L)}$

▶ Exogenous Emission under BAU

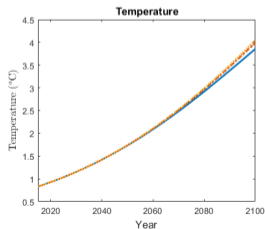
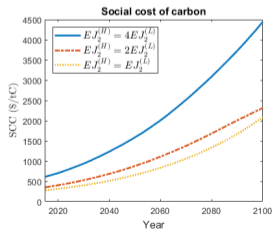
ENDOGENOUS EMISSION AND BAU



Legend in (A)

- $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}$
- $\bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)}$
- $\bar{\lambda}^{(H)} = \bar{\lambda}^{(L)}$

(A) Higher frequency ($\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}, 2\bar{\lambda}^{(L)}$ and $\bar{\lambda}^{(L)}$)



Legend in (B)

- $EJ_2^{(H)} = 4EJ_2^{(L)}$
- $EJ_2^{(H)} = 2EJ_2^{(L)}$
- $EJ_2^{(H)} = EJ_2^{(L)}$

▶ back

(B) Higher intensity ($EJ_2^{(H)} = 4EJ_2^{(L)}, 2EJ_2^{(L)}$ and $EJ_2^{(L)}$)

OPTIMAL ABATEMENT: TIME PATHS OF SCC IF SHOCK ON SIZE

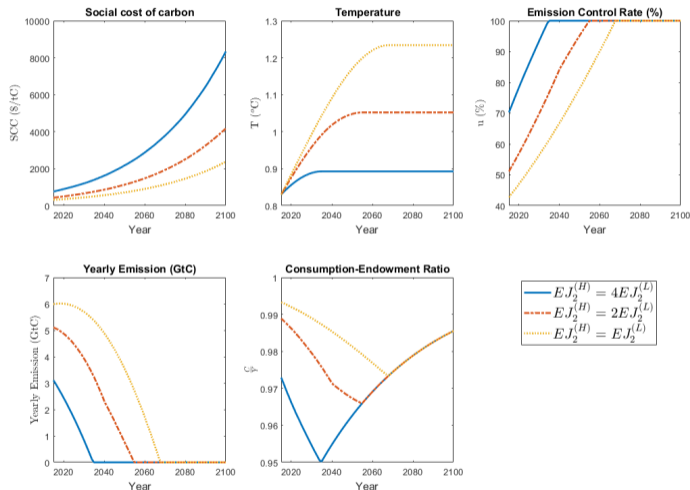
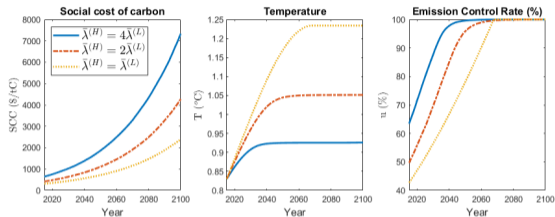


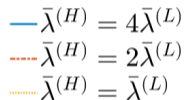
FIGURE: SCC under optimal abatement, exogenous E and increasing intensity

- SCC higher than BAU
- Emission control rate increases in disaster intensity

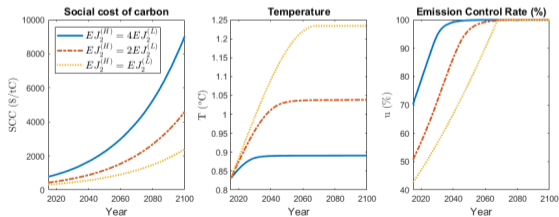
ENDOGENOUS EMISSION AND OPTIMAL ABATEMENT



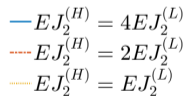
Legend in (A)



(A) Higher frequency ($\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}$, $2\bar{\lambda}^{(L)}$ and $\bar{\lambda}^{(L)}$)



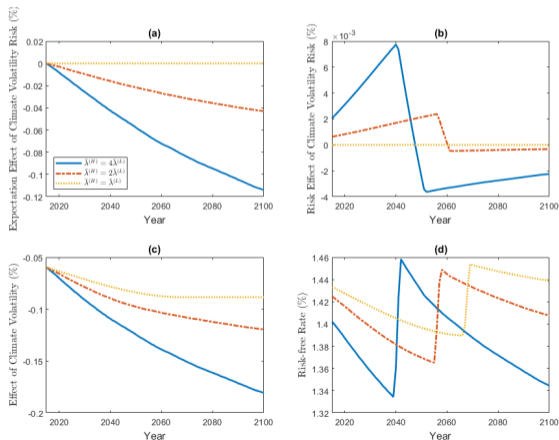
Legend in (B)



(B) Higher intensity ($EJ_2^{(H)} = 4EJ_2^{(L)}$, $2EJ_2^{(L)}$ and $EJ_2^{(L)}$)

RISK-FREE RATE UNDER OPTIMAL ABATEMENT

FIGURE: Risk-free rates under optimal abatement and exogenous emissions:
 (a) Expectation channel (b) Risk channel (c) 1st-order climate risk (d)
 Risk-free rate

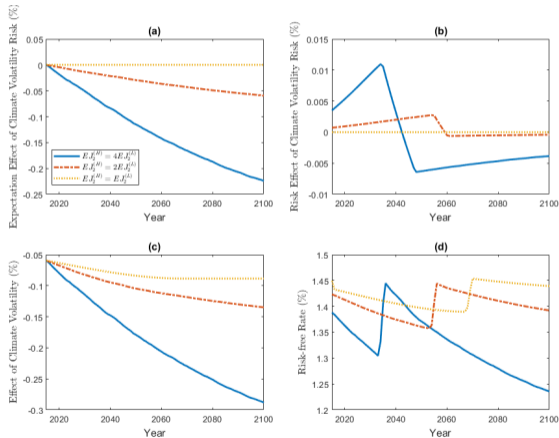


Higher frequency
 $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}, 2\bar{\lambda}^{(L)}, \bar{\lambda}^{(L)}$:

- Magnitude increases in $\bar{\lambda}^{(H)}$ but much smaller than BAU
- Higher risk-free rate than BAU
- Jump in (b): stronger precautionary saving effect after emission control rate reaches 100%,
- Jump in (d): μ_C higher after emission control rate reaches 100%

$$\begin{aligned} &\text{— } \bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)} \\ &\text{- - } \bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)} \\ &\text{... } \bar{\lambda}^{(H)} = \bar{\lambda}^{(L)} \end{aligned}$$

FIGURE: Risk-free rates under optimal abatement and exogenous emissions:
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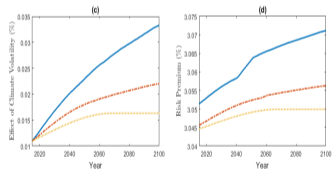
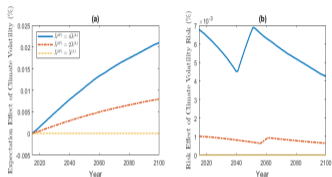
Higher intensity

$$\mathbb{E}J_2^{(H)} = 4\mathbb{E}J_2^{(L)}, 2\mathbb{E}J_2^{(L)}, \mathbb{E}J_2^{(L)}:$$

- Larger risk effects than the high-frequency case but still small relative to BAU
- Jump in (b): precautionary saving effect stronger when emission control rate reaches 100%,
- Jump in (d): μ_C higher after emission control rate reaches 100%

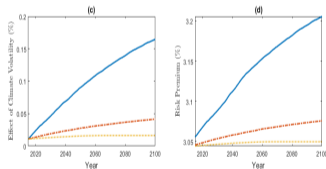
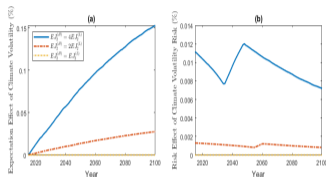
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FIGURE: Risk premia under optimal abatement and exogenous emissions



(A) Higher frequency
 $(\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}, 2\bar{\lambda}^{(L)} \text{ and } \bar{\lambda}^{(L)})$

▶ Exogenous Emission under Optimal Abatement



(B) Higher intensity
 $(\mathbb{E}J_2^{(H)} = 4\mathbb{E}J_2^{(L)}, 2\mathbb{E}J_2^{(L)} \text{ and } \mathbb{E}J_2^{(L)})$

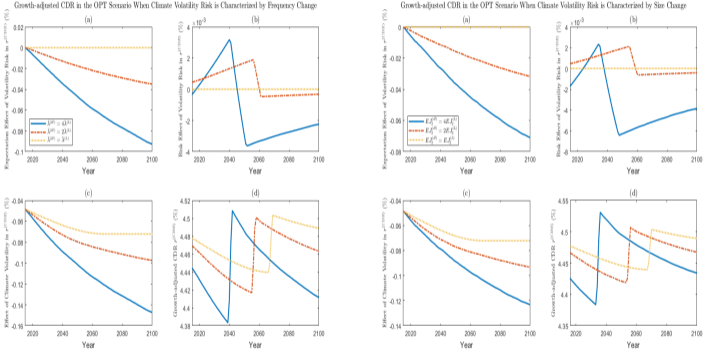
Legend in (A)

$\text{—} \bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}$
 $\text{- - -} \bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)}$
 $\text{...} \bar{\lambda}^{(H)} = \bar{\lambda}^{(L)}$

Legend in (B)

$\text{—} EJ_2^{(H)} = 4EJ_2^{(L)}$
 $\text{- - -} EJ_2^{(H)} = 2EJ_2^{(L)}$
 $\text{...} EJ_2^{(H)} = EJ_2^{(L)}$

FIGURE: Growth-adjusted consumption discount rate under OPT and exogenous carbon emissions



Legend in (A)

- $\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}$
- - - $\bar{\lambda}^{(H)} = 2\bar{\lambda}^{(L)}$
- ⋯ $\bar{\lambda}^{(H)} = \bar{\lambda}^{(L)}$

Legend in (B)

- $EJ_2^{(H)} = 4EJ_2^{(L)}$
- - - $EJ_2^{(H)} = 2EJ_2^{(L)}$
- ⋯ $EJ_2^{(H)} = EJ_2^{(L)}$

(A) Higher frequency
 $(\bar{\lambda}^{(H)} = 4\bar{\lambda}^{(L)}, 2\bar{\lambda}^{(L)} \text{ and } \bar{\lambda}^{(L)})$

(B) Higher intensity
 $(EJ_2^{(H)} = 4EJ_2^{(L)}, 2EJ_2^{(L)} \text{ and } EJ_2^{(L)})$

▶ Exogenous Emission under Optimal Abatement

Barro, R. J. (2009). Rare disasters, asset prices, and welfare costs. American Economic Review, 99(1):243–264.

Cai, Y. and Lontzek, T. S. (2019). The social cost of carbon with economic and climate risks. Journal of Political Economy, 127(6):2684–2734.

Dietz, S., Rising, J., Stoerk, T., and Wagner, G. (2021). Economic impacts of tipping points in the climate system. Proceedings of the National Academy of Sciences, 118(34):e2103081118.

Duffie, D. and Epstein, L. G. (1992). Stochastic differential utility. Econometrica: Journal of the Econometric Society, pages 353–394.

IPCC (2021). Climate Change 2021: The Physical Science Basis. Contribution of Working Group I to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change, volume In Press. Cambridge University Press, Cambridge, United Kingdom and New York, NY, USA.

Nordhaus, W. D. (2017). Revisiting the social cost of carbon. Proceedings of the National Academy of Sciences, 114(7):1518–1523.

The National Climate Assessment (2018). Fourth national climate assessment.