

Efficient Sovereign Debt Management in Emerging Economies

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- Argentina and Brazil experienced an **economic crisis** at the end of 1990s.
- **Maturity** shortened in both countries during that period.
- Argentina **defaulted** in 2001 and got excluded from markets until 2006.
- Brazil did not default and conducted **costly buybacks** since 2006.

Research Questions

- What can **explain** these opposite debt management?
- Which of these two debt management is more **efficient**?
- What are the specific roles of **default**, **buyback** and **maturity**?

This Paper

- Incomplete market economy with:
 - Impatient borrower with limited commitment.
 - Large number of foreign lenders.
- Pareto efficiency in market economy:
 - Assessment of [Second](#) Welfare Theorem.
 - Risk-sharing properties of default, buyback and maturity.
- Multiplicity of equilibria in market economy:
 - Assessment of [First](#) Welfare Theorem.
 - Role of lenders' beliefs.

- Second Welfare Theorem holds:
 - No defaults on equilibrium path, costly buybacks instead.
 - Costly buybacks provide risk sharing and avoid dead weight loss of markets exclusion.
- First Welfare Theorem fails even under Markov equilibrium:
 - Link Markov equilibrium to emerging economies (not today).
 - Multiple equilibria due to lenders' beliefs on buybacks and risky lending.
- Difference between Argentina and Brazil is about coordination of lenders.
 - Brazil gets closer to constrained efficiency than Argentina.

Outline

- 1** Environment
- 2 Market Economy
- 3 Constrained Efficient Debt Management
- 4 Emerging Economies Debt Management
- 5 Quantitative Analysis

- Small open economy in infinite discrete time populated by:
 - A large number of risk **neutral** lenders with discounting $\frac{1}{1+r}$.
 - A risk **averse** borrower with discounting $\beta < \frac{1}{1+r}$ and $\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t u(c_t)$.
- Production function $F(k, \ell)$ with $F(0, 1) > 0$.
 - Foreign lenders **supply** k and $\delta = 1$.
 - **Shock** $g \in \{g_H, g_L\}$ with $g_H > g_L > 0$ and $\pi(g'|g)$.
- Two types of bond contract: one-period, b_{st} , and perpetual, $b_{lt} \leq 0$.

Bond Contract

- A **default** corresponds to a missed coupon payment.
 - Markets exclusion with re-access with probability $\lambda \geq 0$.
- A **buyback** corresponds to $b'_{lt} \geq b_{lt}$:
 - Official buyback at $q_{lt}^{bb} = q_{lt} + \chi$ with $\chi > 0$.
 - Unofficial buyback at q_{lt} .
- Long-term bonds have to be **re-issued** anew every period.
 - Lenders need to form beliefs on official buybacks \rightarrow Sunspot v .

Timing of Actions

- 1 Shock $s \equiv (g, v)$ realizes, outstanding debt b_{st} and b_{lt} .
- 2 Lender supplies k and production takes place.
- 3 Borrower decides whether to repay and whether to pay χ .
- 4 Conditional on repayment, b'_{st} and b'_{lt} are issued.

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Choice and history:

- Choice set at t : $\mathcal{C}_{b,t} \equiv \{ \overbrace{D_t}^{\text{Default}}, \overbrace{M_t}^{\text{Official buyback}}, \overbrace{b_{st,t+1}, b_{lt,t+1}}^{\text{New debt portfolio}} \}$.
- History up to t : $h_b^t = (h^{t-1}, s_t, \underbrace{\mathbb{I}_{D,t}}_{\text{Default status}}, k_t)$ with $h^{t-1} = (h^{t-2}, s_{t-1}, \mathbb{I}_{D,t-1}, k_{t-1}, \mathcal{C}_{b,t-1})$.

Maximization problem:

$$W^b(h_b^t) = \max_{\{\mathcal{C}_{b,t}\}_{t=0}^{\infty}} u(c_t) + \beta \mathbb{E} \left[W^b(h_b^{t+1}) \mid h_b^t, \mathcal{C}_{b,t} \right]$$

$$\text{s.t.} \begin{cases} c_t + \overbrace{q_{st} b_{st,t+1}}^{\text{New short-term debt}} + \overbrace{q_{lt} (b_{lt,t+1} - b_{lt,t})}^{\text{New long-term debt}} = g_t F(k_t, 1) - k_t + b_{st,t} + b_{lt,t} & \text{if } D_t = 0 \wedge M_t = 0. \\ c_t + q_{st} b_{st,t+1} + q_{lt} b_{lt,t+1} = g_t F(k_t, 1) - k_t + b_{st,t} + \underbrace{b_{lt,t}(1 + q_{lt}^{bb})}_{\text{Official debt buyback}} \wedge \underbrace{b_{lt,t+1} \geq b_{lt,t}}_{\text{Buyback restriction}} & \text{if } D_t = 0 \wedge M_t = 1. \\ c_t = g_t F(0, 1) & \text{if } D_t = 1. \end{cases}$$

Sustainable Equilibrium

- A **sustainable equilibrium**: subgame perfection for all histories.
 - **Multiple** equilibrium outcomes:
 - Trigger strategies: reversion to permanent autarky.
- ⇒ Second Welfare Theorem holds.
- ⇒ First Welfare Theorem fails even if restrict to Markov equilibria.

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- Perspective of a central **Planner** who:
 - Allocates c and k .
 - Accounts for limited commitment.
- Constrained efficient allocation features:
 - Risk sharing between borrower and lender.
 - Strictly positive capital, $k > 0 \rightarrow$ Inada conditions.

Decentralization

- Official buybacks on equilibrium path:

- Buyback premium generates **state contingency** in bonds.
- Official buybacks in good times.

- No default on equilibrium path:

- Default triggers **markets exclusion** and $k = 0$.

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- Markov equilibria rely on payoff-relevant space $\Omega \equiv (s, \mathbb{I}_D, b_{st}, b_{lt})$.
- Foundation of Markov equilibria:
 - ⇒ Emerging economies are characterized by **political instability** and **hazy fundamentals**.
 - 1 Borrower's memory goes back to $\mathcal{T} = \frac{1-\psi}{\psi}$ with $\psi \in [0, 1]$.
 - 2 Privately-observed and i.i.d. utility shock: $\epsilon_{\theta b,t}$ and $\epsilon_{\theta l,t}$.
 - ⇒ All sustainable equilibria are Markov for $(\epsilon, \psi) > 0$ arbitrarily close to zero.

- Borrower cannot commit to pay the buyback premium χ .
- Lenders cannot detect a buyback before debt auction.
- Lenders can **threaten** not to buy new debt if χ not paid.
- State space Ω can be separated in two zones:
 - 1 **Enforcement** zone: if lenders believe official buyback happens, it does. Otherwise, it does not.
 - 2 **Impunity** zone: official buyback is not enforceable. Sunspot v is irrelevant.

Strategic Complementarity

- Markets exclusion is detrimental to both borrower and lenders.
- Lenders would like to avoid default → Limit lending.
- Strategic complementarity in lenders' action:
 - Beliefs about behavior of other lenders.
 - Coordination on whether lending is risky.
- Markov equilibrium with or without default.

- Four different outcomes: whether lending is risky and whether official buybacks occur.
- Rule out possibility of having official buybacks and risky lending.
- Two Markov equilibria:
 - 1 Markov equilibrium **with** default (MA) where official buybacks never occur → Argentina.
 - 2 Markov equilibrium **without** default (MAND) where official buybacks can occur → Brazil.
- Is the MAND constrained efficient? This depends on v and enforcement zone.

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- My view is that Argentina and Brazil are **alike** in terms of economic fundamentals.
- The **difference** lies in the lenders' coordination of beliefs.
- Calibration strategy:
 - Calibrate MA to Argentina for the period 1995-2019.
 - Use the same calibration to solve the other equilibria.
 - Only difference is the specification of v .

Calibration Outcome

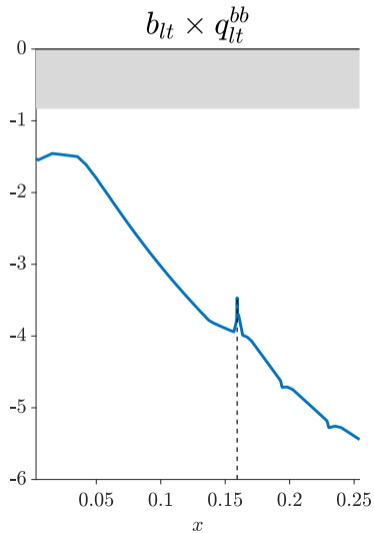
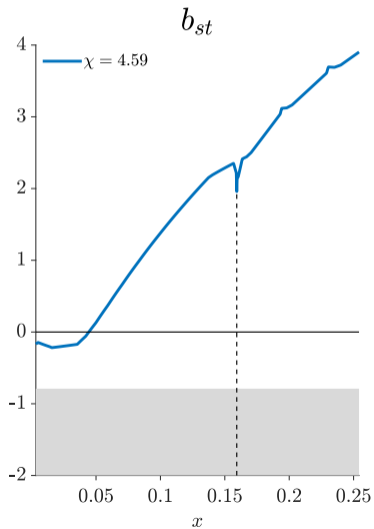
A. Targeted Moments					
Variable	Argentina	MA	Brazil	MAND	CEA
i/y	14.26	14.22	17.98	16.22	14.61
$-b/y$	28.71	28.15	10.12	7.18	-353.20
Spread	14.17	12.88	4.97	3.85	3.95
$\text{corr}(c, y)$	0.96	0.94	0.88	0.95	0.68

B. Non-Targeted Moments					
Variable	Argentina	MA	Brazil	MAND	CEA
b/y in default	65.7	216.4	-	-	-
b/y in restructuring	29.9	17.5	-	-	-
b_{st}/b	9.7	44.0	12.6	21.7	112.5
b_{st}/b in default	11.7	84.1	-	-	-
b_{st}/b in restructuring	9.0	64.5	-	-	-

Non-Markov Implementation

Details

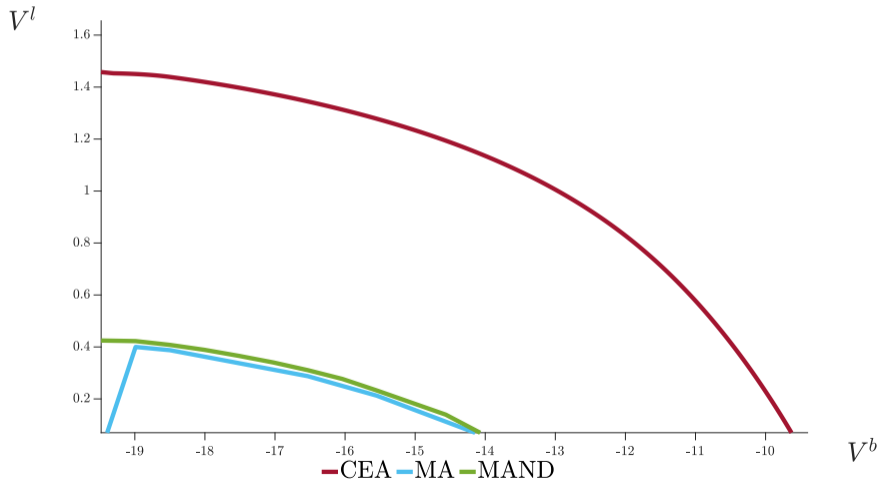
χ



- Welfare gains in consumption equivalent with respect to MA.
- Distance to Pareto frontier.

State	Borrower welfare gains (percent)		Lenders welfare gains (percent)		MA	$\mathcal{F}(g)$ (percent)	
	MAND	CEA	MAND	CEA		MAND	CEA
g_H	0.01	0.07	0.5	1.7	23.6	26.3	100.0
g_L	0.84	0.85	1.9	3.4	18.7	21.2	100.0
average	0.17	0.22	0.8	2.0	22.6	25.3	100.0

Distance to Pareto Frontier



Conclusion

- Assessment of sovereign debt management in emerging economies:
 - Markov equilibrium is the relevant equilibrium concept for emerging economies.
 - Markov equilibria generally fail constrained efficiency + far from Pareto frontier.
- Defaults are an inefficient source of risk sharing, use buybacks instead → lenders' beliefs.
- Relate to the experience of Argentina and Brazil since 1995.

Thanks for your attention!

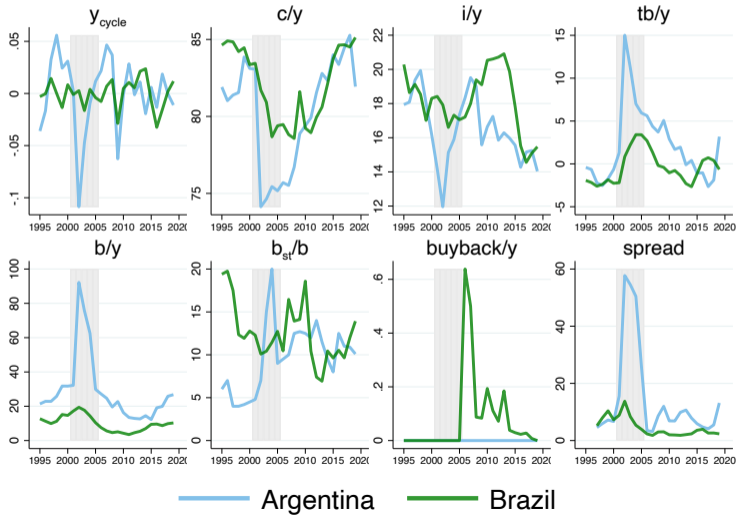
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Appendix

Argentina vs. Brazil

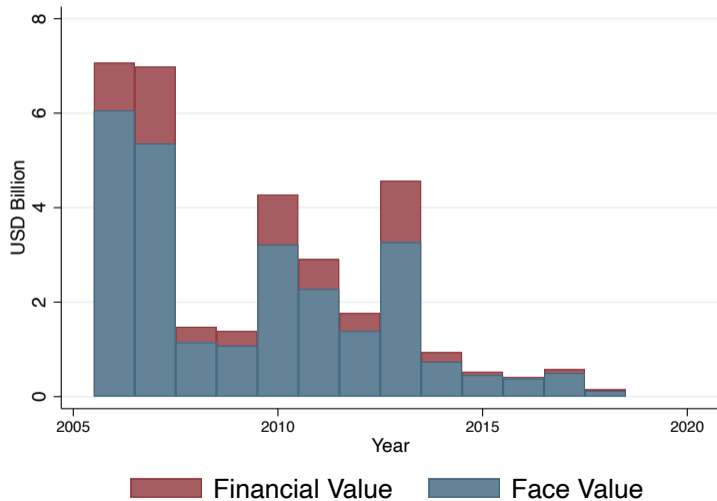
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Appendix

Brazilian buyback program

[Go back](#)



■ Sovereign debt defaults:

- Eaton and Gersovitz (1981), Aguiar and Gopinath (2006), Arellano (2008), **Mendoza and Yue (2012)**, **Arellano and Ramanarayanan (2012)**, Niepelt (2014), **Dovis (2019)** and Müller et al. (2019).
- ⇒ [Foundation of Markov equilibria + inefficiency of defaults + lenders' belief.](#)

■ Sovereign debt buybacks:

- **Bulow and Rogoff (1988, 1991)**, Rotemberg (1991), Acharya and Diwan (1993), Cohen and Verdier (1995), Aguiar et al. (2019) and Aguiar et al. (2022).
- ⇒ [Efficiency of buybacks + self-fulfilling equilibrium.](#)

■ Sovereign debt maturity:

- **Angeletos (2002)**, Buera and Nicolini (2004), Faraglia et al. (2010), Debortoli et al. (2017), Aguiar et al. (2019), Faraglia et al. (2019) and Kiiashko (2022).
- ⇒ [Approximation of constrained efficiency through Markov strategies.](#)

- Lender provides k at price p which is taxed at fixed rate τ .
- The **level of capital** is such that

$$gf_k(k) = p.$$

- The **price of capital** is consistent with

$$\max_k p(1 - \tau)k - k.$$

- With $\tau = 1 - \frac{1}{p}$, p is used to decentralize the distortion of k the Planner chooses.

The price of one unit of bond is given by

$$q_{lt}(h^t) = \frac{1}{1+r} \mathbb{E} \left[(1 - D(h^{t+1})) \left\{ 1 + (1 - M(h^{t+1})) q_{lt}(h^{t+1}) + M(h^{t+1}) q_{lt}^{bb} \right\} \middle| h^t \right],$$

$$q_{st}(h^t) = \frac{1}{1+r} \mathbb{E} \left[(1 - D(h^{t+1})) \middle| h^t \right].$$

Appendix

Optimal Contract

Go back

$$\begin{aligned} & \max_{\{k(g^t), c(g^t)\}_{t=0}^{\infty}} \overbrace{\mu_{b,0} \sum_{t=0}^{\infty} \beta^t \sum_{g^t} \pi(g^t | g_0) u(c(g^t))}^{\text{Value of borrower}} + \overbrace{\mu_{l,0} \sum_{t=0}^{\infty} \left(\frac{1}{1+r}\right)^t \sum_{g^t} \pi(g^t | g_0) T(g^t)}^{\text{Value of lender}} \\ \text{s.t. } & \sum_{j=t}^{\infty} \beta^{j-t} \sum_{g^j} \pi(g^j | g_t) u(c(g^j)) \geq \underbrace{V^D(g_t, k(g_t))}_{\text{Autarky value in Markov equilibrium with default}}, \end{aligned} \quad (\text{PC})$$

$$T(g^t) = g_t f(k(g^t)) - c(g^t) - k(g^t), \quad \forall g_t, g^t, t$$

with $\mu_{b,0}$ and $\mu_{l,0}$ given.

- Following Marcet and Marimon (2019),

$$FV(g, x) = \mathcal{SP} \min_{\{\nu(g)\}} \max_{\{k(g), c(g)\}} x \left[(1 + \nu(g))u(c(g)) - \nu(g)V^D(g, k) \right] \\ + T(g) + \frac{1}{1+r} \sum_{g'} \pi(g'|g) FV(g', x')$$

s.t. $T(g) = gf(k(g)) - c(g) - k,$
 $x'(g) = (1 + \nu(g))\eta x \quad \forall g.$

- Value functions take the following form,

$$FV(g, x) = xV^b(g, x) + V^l(g, x) \quad \text{with} \\ V^b(g, x) = u(c(g)) + \beta \mathbb{E}_{g'|g} \left[V^b(g', x') \right] \quad \text{and} \quad V^l(g, x) = T(g) + \frac{1}{1+r} \mathbb{E}_{g'|g} \left[V^l(g', x') \right].$$

The allocation is such that:

- I (Production). There exists a level of relative Pareto weight $x^*(g)$ such that $k(g, x) = k^*(g)$ for $x \geq x^*(g)$ and $x^*(g_H) > x^*(g_L)$. Conversely, for all $x, \tilde{x} \in X$ with $x^*(g) > x > \tilde{x}$, $0 < k(g, \tilde{x}) < k(g, x) < k^*(g)$.

- II (Risk-Sharing). $c(g_L, x) \leq c(g_H, x)$ and $x'(g_L, x) \leq x'(g_H, x)$ for all x with equality when $x \geq x^*(g_H)$.

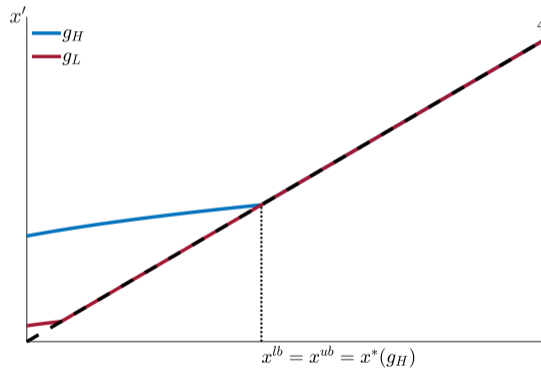
- III (Liabilities). $V^l(g_L, x) < V^l(g_H, x)$ for all x .

- The utility possibility frontier is strictly increasing.
 - $V^b(g, x)$ is strictly **increasing** in x .
 - $V^l(g, x)$ is strictly **decreasing** in x .
- The autarkic allocation is **not** optimal.
 - Inada conditions on production function.
 - Region of *ex post* inefficiencies around $k = 0$.

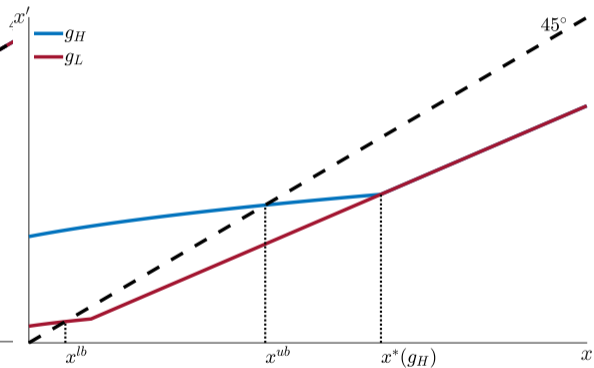
Appendix

Steady state

Go back



(a) $\beta(1+r) = 1$



(b) $\beta(1+r) < 1$

- **No** default \Rightarrow neither x^{lb} nor x^{up} can be interpreted as default.
- **Costly** buybacks $\Rightarrow r^{bb} < r$ necessary to generate some (**negative**) spread.
- Holdings at buybacks:

$$b_{st}(x) = \frac{V'(g_H, x)[1 + q_{lt}] - V'(g_L, x)[1 + q_{lt}^{bb}]}{q_{lt}^{bb} - q_{lt}} \leq 0$$

$$b_{lt}(x) = -\frac{V'(g_H, x) - V'(g_L, x)}{q_{lt}^{bb} - q_{lt}} < 0.$$

- Recall: buyback enforceable with **Markov strategies** if $b'_{st} < 0$ and low χ .

- A sustainable equilibrium is **Markov** if for any $(h_b^t, \overbrace{h_l^t}^{(h^{t-1}, s_t, \mathbb{I}_{D,t})}) \neq (\tilde{h}_b^t, \tilde{h}_l^t)$ ending with the same $\Omega_t \equiv (g_t, \mathbb{I}_{D,t}, b_{st,t}, b_{lt,t})$, strategies are the same such that

$$W^b(h_b^t) = W^b(\tilde{h}_b^t) \wedge \underbrace{W^l(h_l^t)}_{\text{Value of lender}} = W^l(\tilde{h}_l^t).$$

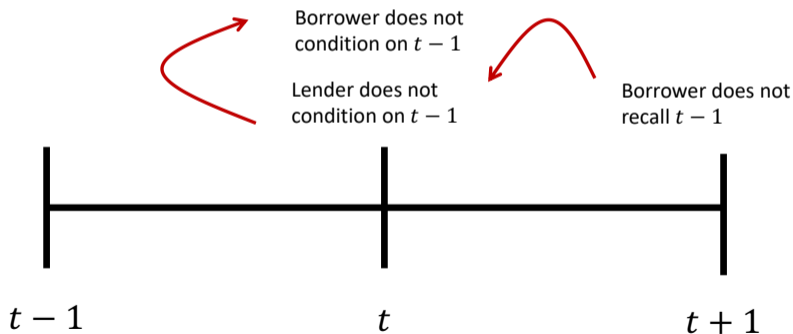
- **Bounded memory** rules out sequential conditioning on past history.
- **Utility shocks** rule out weak-Markov equilibrium.

Appendix

Markov equilibrium

Go back

- Suppose borrower's memory goes back $\mathcal{T} = 1$ period.
- Sequential moves: first borrower then lender.



- Value of debt contract:

$$W^b(s, 0, b_{st}, b_{lt}) = \max_{D \in \{0,1\}} \left\{ (1 - D) \overbrace{V^P(s, 0, b_{st}, b_{lt})}^{\text{Value under repayment}} + D \underbrace{V^D(s, 0, k)}_{\text{Value under default}} \right\}.$$

- Value under default:

$$V^D(s, 0, k) = u(gF(k, 1)) + \beta \mathbb{E}_{s'|s} \left[(1 - \lambda) V^D(s', 1, 0) + \underbrace{\lambda}_{\text{Probability of market re-access}} W^b(s', 0, w_{st}, w_{lt}) \right].$$

- Value under repayment:

$$V^P(s, 0, b_{st}, b_{lt}) = \max_{b'_{st}, b'_{lt}, M} u(c) + \beta \mathbb{E}_{s'|s} W^b(s', 0, b'_{st}, b'_{lt})$$

$$\text{s.t. } \begin{cases} c + q_{st} b'_{st} + q_{lt} (b'_{lt} - b_{lt}) = gF(k, 1) - k + b_{st} + b_{lt} & \text{if } M = 0. \\ c + q_{st} b'_{st} + q_{lt} b'_{lt} = gF(k, 1) - k_t + b_{st} + b_{lt}(1 + q_{lt}^{bb}) \wedge b'_{lt} \geq b_{lt} & \text{if } M = 1. \end{cases}$$

The price of one unit of bond of maturity $j \in \{st, lt\}$

$$q_{lt}(s, b'_{st}, b'_{lt}) = \frac{1}{1+r} \mathbb{E}_{s'|s} \left[(1 - D(\Omega'_P)) \left\{ 1 + (1 - M(\Omega'_P)) q_{lt}(s', b''_{st}, b''_{lt}) + M(\Omega'_P) q_{lt}^{bb} \right\} \right],$$

$$q_{st}(s, b'_{st}, b'_{lt}) = \frac{1}{1+r} \mathbb{E}_{s'|s} \left[(1 - D(\Omega'_P)) \right],$$

- Lender's threat is **sudden stop** on debt: $b'_{st} \geq 0$ and $b'_{lt} \geq b_{lt}$.
- When is the threat **credible**?
 - If $b'_{st} \geq 0$, an *official* buyback is not enforceable for any (b_{st}, b_{lt}) .
 - If $b'_{st} < 0$, an *official* buyback is enforceable when either $-b_{st}$ is sufficiently large or $-b_{lt}$ and χ are not too large.

- Two types of multiplicity:

- 1 Static → current period behavior as in Cole and Kehoe (2000).

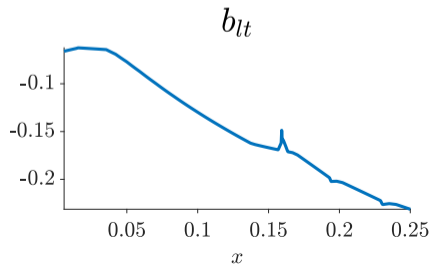
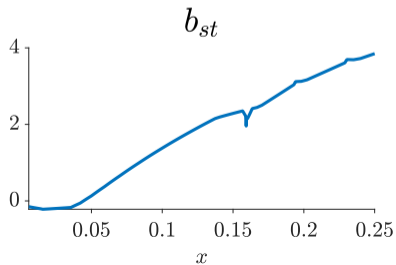
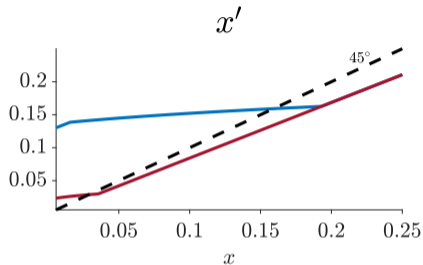
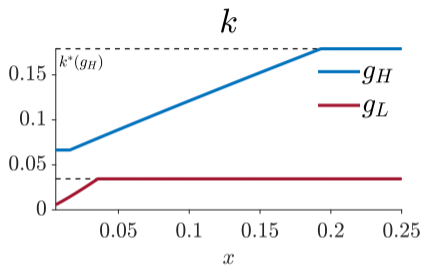
- 2 Dynamic → future behavior as in Aguiar and Amador (2020).

- Sunspot is composed of two parts: $v_t = \underbrace{\varpi_0}_{\text{Dynamic coordination}} (1 + \underbrace{\omega_t}_{\text{Static coordination}})$.

Appendix

Optimal contract main policy functions

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Appendix

Parameters

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Parameter	Value	Description	Targeted Moment
A. Based on Literature			
ϑ	2.00	Relative risk aversion	
r^f	0.01	Risk-free rate	
B. Direct Measure from the Data			
$\pi(g_H g_H)$	0.93	Probability staying high state	
$\pi(g_L g_L)$	0.68	Probability staying low state	Real total factor productivity
g_L	0.44	Productivity in low state	
$1 - \alpha$	0.70	Labor share	Labor income share
χ	4.59	Official buyback premium	Financial over face value of debt
r^e	0.04	Excess return	US excess return on debt
C. Based on Model solution			
β	0.80	Discount factor	Debt-to-GDP ratio
g_H	1.12	Productivity in high state	Correlation consumption and output
ϕ	1.50	CES production	Investment-to-GDP ratio
λ	0.281	Probability re-accessing market	Average spread

CRRRA utility $u(c) = \frac{c^{1-\vartheta}}{1-\vartheta}$, excess return $r = r^e + r^f$, and $v = \mathbb{I}_{g=g_H}$ and CES $F(k, l) = \left[\alpha k^{\frac{\phi-1}{\phi}} + (1-\alpha)l^{\frac{\phi-1}{\phi}} \right]^{\frac{\phi}{\phi-1}}$.

Appendix

Welfare decomposition

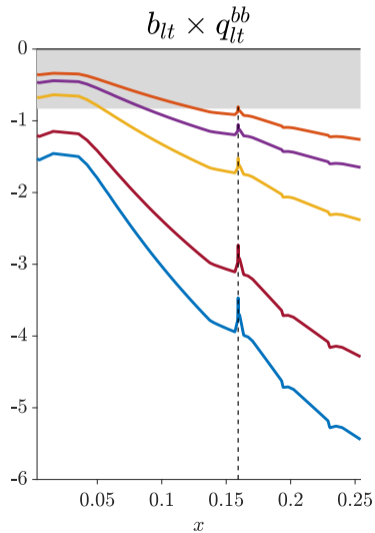
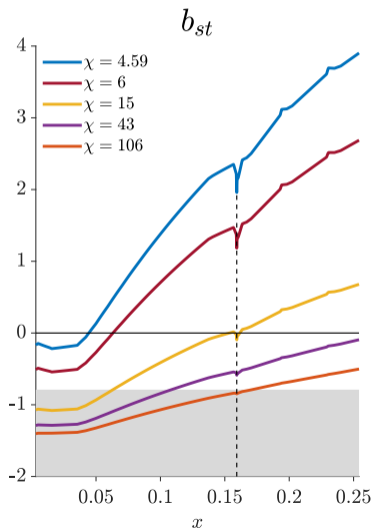
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State	MAND		CEA	
	State contingency (percent)	Cost of default (percent)	State contingency (percent)	Cost of default (percent)
g_H	1.90	98.10	15.67	84.33
g_L	99.13	0.87	98.70	1.30
average	20.38	79.62	31.45	68.55

Appendix

Cost of Buybacks

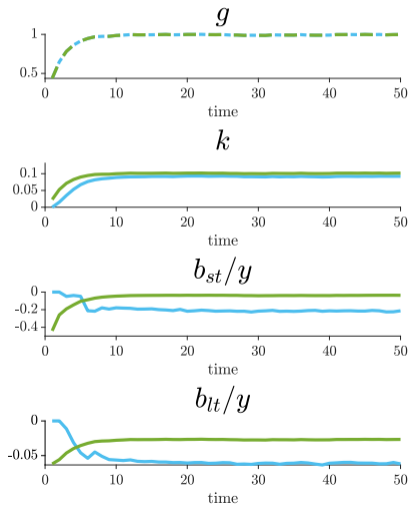
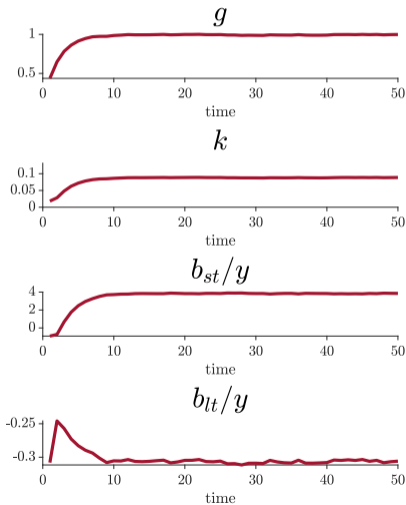
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Appendix

Impulse responses

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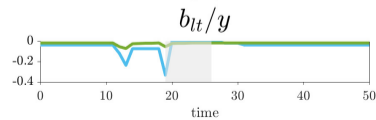
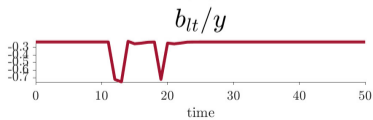
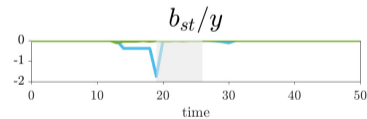
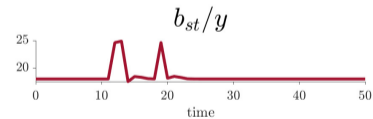
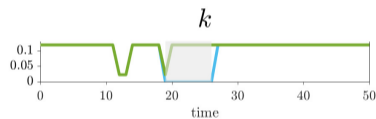
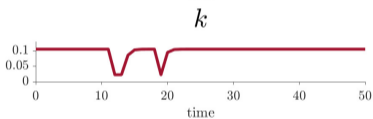
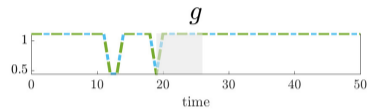
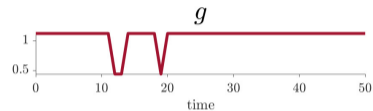


— CEA — MA — MAND

Appendix

Simulation

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— CEA — MA — MAND

- With the implementation, I get a correspondence between x and (b_{st}, b_{lt}) .
- Define $\ddot{V}^l : G \times X \rightarrow \mathbb{R}$ as the lender's value in a Markov equilibria expressed in X .
- The distance to the Pareto frontier is then

$$\mathcal{F}(g) = \frac{\int_{\underline{x}}^{\bar{x}} \ddot{V}^l(g, x) dx}{\int_{\underline{x}}^{\bar{x}} V^l(g, x) dx}.$$