

Bipartite interference:  
Estimating health effects of power plant  
interventions

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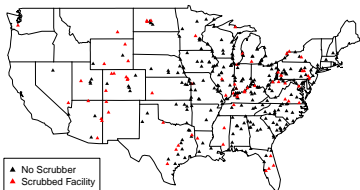
*with Cory Zigler (UT Austin) and Laura Forastiere (Yale)*

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# Major Pollution Source: Power Plants

⇒ Many regulations to reduce emissions

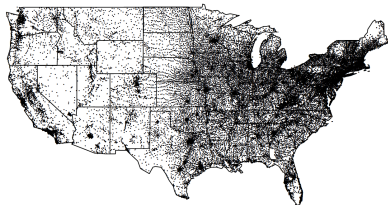
Interventions at Power Plants:  
“Scrubber” Installation  
⇒ Reduce SO<sub>2</sub> emissions



Affect?



Health at Population Locations  
(Zip Codes)



**Question:** Do scrubbers on coal-fired power plants causally affect hospitalizations for Ischemic Heart Disease (IHD) among Medicare beneficiaries?

# Formalization of Bipartite Structure

Two types of observational units:

## 1 Intervention Units

- $\mathcal{P} = \{p_1, p_2, \dots, p_j, \dots, p_J\}$ : a set of  $J$  power plants, where interventions occur (or not)
- $S_j = 1/0$  denotes presence/absence of intervention
- Treatment allocation:  $\mathbf{S} = (S_1, \dots, S_j, \dots, S_J)$
- Space of possible vectors of treatment allocations:  $\mathcal{S}(J)$
- Covariates  $\mathbf{X}^{int} = (\mathbf{X}_1^{int}, \dots, \mathbf{X}_j^{int}, \dots, \mathbf{X}_J^{int})$

## 2 Outcome Units

- $\mathcal{M} = \{m_1, m_2, \dots, m_i, \dots, m_n\}$ : a set of  $n$  locations, where outcomes are measured
- $Y_i$  denotes the outcome of interest
- Covariates:  $\mathbf{X}^{out} = (\mathbf{X}_1^{out}, \dots, \mathbf{X}_i^{out}, \dots, \mathbf{X}_n^{out})$

Potential Outcomes

- $Y_i(\mathbf{s})$  potential outcome that would be observed at outcome unit  $i$  under treatment allocation  $\mathbf{s}$ ,  $\mathbf{s} \in \mathcal{S}(J)$
  - No multiple versions of treatment:  $Y_i(\mathbf{s}) = Y_i(\mathbf{s}') \forall i$  when  $\mathbf{s} = \mathbf{s}'$
- (Zigler and Papadogeorgou, 2021; Papadogeorgou, Mealli, Zigler, 2019)

# Examples and Challenges

## Examples:

### 1 *Economics of housing (Stock, 1989)*

- Intervention units: Hazardous-waste disposal sites where treatments (cleaning up) can be applied
- Outcome units: Locations where outcomes (e.g., housing values) are measured

### 2 *Education economics (Crema, 2022)*

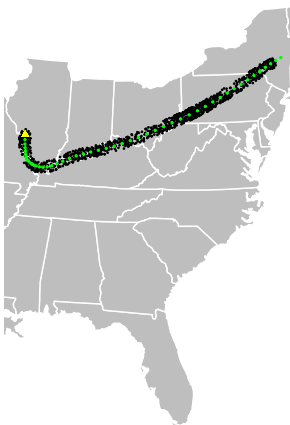
- Intervention units: Neighborhoods which may be exposed to openings of charter schools (treatment)
- Outcome units: Traditional public schools (TPS) where outcome (e.g., racial segregation) are measured

## Non trivial differences in:

- the formulation of the estimands
- the assignment mechanism
- different types and sources of confounding

# Interference Mapping and Causal Quantities

Using Long-range Pollution Transport Models (HyADS)  
Henneman et al (2019)

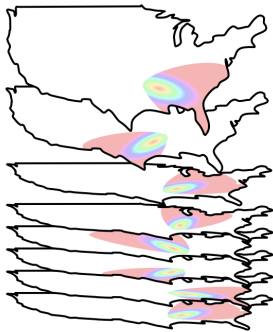


- Emissions originating at a power plant (**yellow triangle**) *move*
  - ↪ Long distances towards conversion to harmful pollution
- Potential outcomes for zip code  $i$ :
  - ↪  $Y_i(\text{power plants that pollute over } i)$
- Estimands that compare the potential outcomes
  - ↪ if the *most influential (or closest)* power plant were treated
  - ↪ if the 10 most influential power plants were treated
  - ↪ any other intervention allocation

# Interference Mapping and Causal Quantities

Using Long-range Pollution Transport Models (HyADS)  
Henneman et al (2019)

Use atmospheric transport  
models to simulate  
emissions events starting  
at individual stack



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# Bivariate Treatment

- ① Outcome unit  $i$ 's “key associated” intervention unit:  $J_{(i)}^*$ , i.e., the power plant that is most influential for ZIP code  $i$ 
  - $J_{(i)}^* \equiv j : t_{ij} = \max_j \{t_{i1}, \dots, t_{ij}, \dots, t_{iJ}\}$
- ② “Individual” Treatment:  $Z_i = S_{J_{(i)}^*}$ , i.e., scrubber status of the key associated power plant  $J_{(i)}^*$ 
  - $Z_i = 0, 1$  according to whether the key power plant has a scrubber or not
- ③ “Upwind” Treatment: Function of the scrubber statuses of all other “linked” power plants
  - “Exposure Mapping:”  $g_i(\cdot; T) : \{0, 1\}^{J-1} \rightarrow \mathcal{G}_i$
  - $g_i(\mathbf{S}, T) = G_i = \sum_{j \neq J_{(i)}^*} t_{ij} S_j$
  - HyADS-weighted upwind treatment rate

(Aronow, Samii, 2017; Forastiere et al., 2021)



# “Upwind Interference” Assumption

(Adaptation of SUTVA)

$$Y_i(\mathbf{S}) = Y_i(Z_i, G_i) = Y_i(Z'_i, G'_i) = Y_i(\mathbf{S}')$$

- Reduces interference to depend only on  $Z_i$  and  $G_i$  (not on the entire  $\mathbf{S}$ )
- Hospitalizations are the same under different  $\mathbf{S}$  if the treatment of the key power plant and the “upwind” treatment rate are the same
- **The key assumption** about interference

Assignment mechanism governing the joint treatment:

$$P(\mathbf{Z}, \mathbf{G} \mid \mathbf{X}^{out}, \mathbf{X}^{int}, \{Y_i(z, g), z \in \{0, 1\}, g \in \mathcal{G}\})$$

## “Direct” Effects in the Bipartite Setting

Average dose-response under key-associated treatment  $z$  and upwind treatment  $g$

$$\mu(z, g) = \mathbb{E}_{X^{int}, X^{out}} [\mathbb{E}_{Y(\cdot)|X^{int}, X^{out}} [Y_i(z, g) \mid X_i^{int}, X_i^{out}]]$$

The “direct” effect of treating the key plant while holding fixed the “upwind” treatments:

$$\tau(g) = \mu(1, g) - \mu(0, g)$$

“Overall” average over the distribution of “upwind” treatments:

$$\tau = \sum_{g \in \mathcal{G}} \tau(g) P(G_i = g)$$

“The effect on IHD hospitalizations that we are expecting to have in a zipcode from installing a scrubber on the *key associated* power plant”

## “Indirect” or “Spillover” Effects in the Bipartite Setting

The “indirect” or “upwind” effect of installing scrubbers on upwind power plants without changing the key plant:

$$\delta(g; z) = \mu(z, g) - \mu(z, g^{min})$$

“Overall” average over the distribution of “upwind” treatments:

$$\Delta(z) = \sum_{g \in \mathcal{G}} \delta(g; z) P(G_i = g)$$

“The effect on IHD hospitalizations that we are expecting to have in a zipcode from installing more scrubbers on upwind plants”

# Confounding Specification

Ignorability of the Joint Treatment:

$$Y_i(z, g) \perp\!\!\!\perp Z_i, G_i \mid \{\mathbf{X}_j^{int}\}_{j:t_{ij}>0}, \mathbf{X}_i^{out}, \quad \forall z \in \{0, 1\}, g \in \mathcal{G}_i, \forall i$$

$\mathbf{X}_i^{out}$  includes: population, urbanicity, race/ethnicity, education, HH income, poverty, occupied housing, migration, smoking, region, temperature, humidity, Medicare age, sex.

$$\{\mathbf{X}_j^{int}\}_{j:t_{ij}>0} = \left\{ \mathbf{X}_{j(i)}^{int*}, \{\mathbf{X}_j^{int}\}_{j \neq j(i): t_{ij}>0} \right\}$$

$\mathbf{X}_{j(i)}^{int*}$  includes: operating time, heat input, %operating capacity, ARP phase II participation, NO<sub>x</sub> controls sulfur content of coal of *power plant j(i)\**

$\{\mathbf{X}_j^{int}\}_{j \neq j(i): t_{ij}>0}$  includes: “upwind” versions of power plant characteristics (e.g., the HyADS-weighted operating time of upwind plants)

# Individual and Neighborhood Propensity Scores

Extension of Forastiere et al. (2021)

View “individual” and “upwind” treatments as bivariate treatment and estimate a **joint propensity score**:

$$\psi_i(z, g; \mathbf{x}^{int}, \mathbf{x}^{out}) = P(Z_i = z, G_i = g \mid \{\mathbf{X}_j^{int}\}_{j:t_{ij}>0} = \mathbf{x}^{int}, \mathbf{X}_i^{out} = \mathbf{x}^{out})$$

Further decompose into:

$$\psi_i(z, g; \mathbf{x}^{int}, \mathbf{x}^{out}) = P(Z_i = z \mid \{\mathbf{X}_j^{int,z}\}_{j:t_{ij}>0} = \mathbf{x}^{int,z}, \mathbf{X}_i^{out,z} = \mathbf{x}^{out,z}) \quad (1)$$

$$\times P(G_i = g \mid Z_i = z, \{\mathbf{X}_j^{int,g}\}_{j:t_{ij}>0} = \mathbf{x}^{int,g}, \mathbf{X}_i^{out,g} = \mathbf{x}^{out,g}) \quad (2)$$

(1)  $\equiv \phi_i(z; \mathbf{x}^{int,z}, \mathbf{x}^{out,z}) \equiv$  “individual propensity score”

(2)  $\equiv \lambda_i(g; z, \mathbf{x}^{int,g}, \mathbf{x}^{out,g}) \equiv$  “upwind propensity score”

# Estimation strategy

Extension of Forastiere et al. (2021)

- 1 Estimate  $\phi_i$  and  $\lambda_i$ :  $\hat{\phi}_i, \hat{\lambda}_i$
- 2 Stratify zip codes into  $K = 5$  strata based on based on  $\hat{\phi}_i$
- 3 Specify and estimate  $Y_i(z, g) | \hat{\lambda}_i \sim f^y(z, g, \hat{\lambda}_i; \theta_k)$ ; derive predicted values  $\hat{Y}_i(z, g)$
- 4 Estimate within-stratum dose-response function  $\mu_k(z, g)$ :

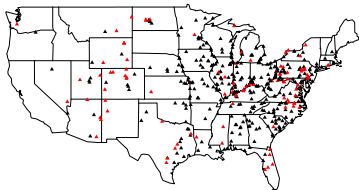
$$\hat{\mu}_k(z, g) = \frac{\sum_{i \in n_k} \hat{Y}_i(z, g)}{n^k}$$

- 5 Obtain an overall estimate:  $\hat{\mu}(z, g) = \sum_{k=1}^K \hat{\mu}_k(z, g) \pi^k$
- 6 Calculate Direct and Upwind effects
- 7 Intervention-Unit Bootstrap - not exactly right, but shown via simulations to be conservative as a measure of model and design variability

# Power Plant and Zip Code Data

Integrated with HyADS atmospheric model

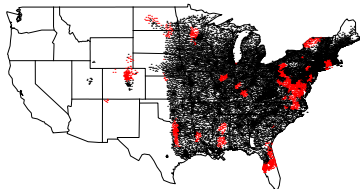
472 Coal-fired power plants  
operating in 2005



Affect



Medicare IHD Hospitalizations in  
2005 at 25,553 zip codes (overlap  
criteria)

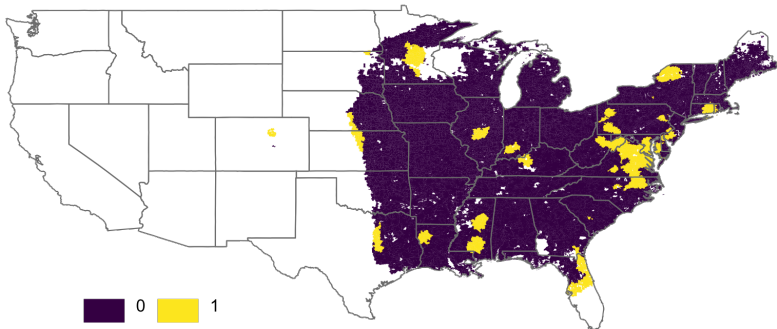


- 106 with scrubbers installed
- Information on emissions, plant size, operating capacity, other controls, etc. (EPA)

- Information on population demographics (Census, Medicare), weather (NOAA), smoking rates (CDC)

# Individual Treatment

Whether the **most influential** plant has a scrubber



$Z_i = 0$  if  $j^*$  has no scrubber

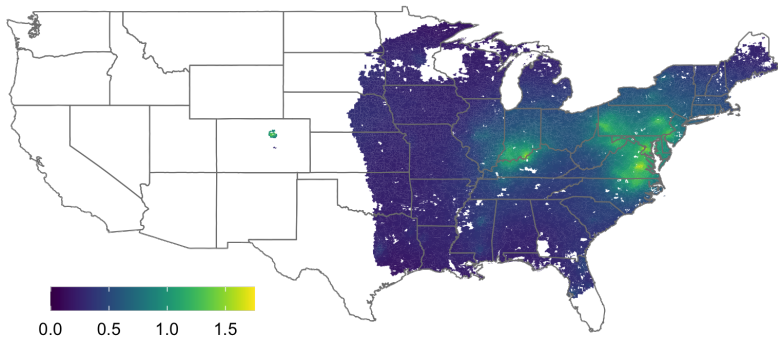
$Z_i = 1$  if  $j^*$  has scrubber (2,753 zip codes)

278 power plants are key-associated and 35 have scrubber

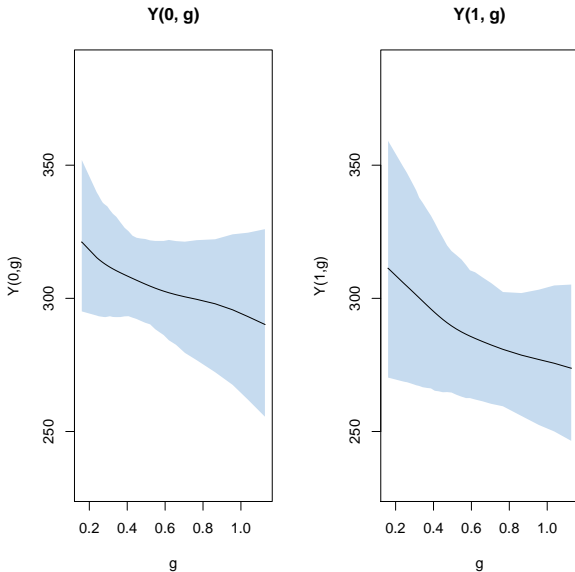


# “Upwind” Treatment

HyADS-weighted treatment rate of upwind plants



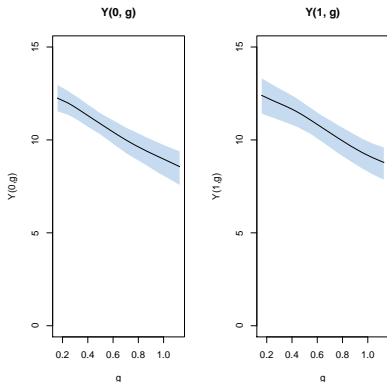
# Average Dose-Response for $Y(z, g)$



# Estimated Effects of Scrubbers on IHD Hospitalization

- Average “direct” effect of installing a scrubber on the key power plant ( $\tau$ )
  - **Most influential plant:** -23 (-38, 14)  
... hospitalizations per 10K person-years
- Average “upwind” effect of installing more scrubbers on “upwind” plants ( $\Delta(z)$ ):
  - **Most influential plant:**
    - If  $z = 1$  : -18 (-39, 2)
    - If  $z = 0$  : -14 (-37, 2)

# Average Dose-Response for $PM_{2.5}(z, g)$



$$\hat{\tau} = -0.37 \text{ } (-0.32, 0.84);$$
$$\Delta(0) = -1.34 \text{ } (-1.75, -0.99); \Delta(1) = -1.16 \text{ } (-1.63, -0.80)$$

# Summary

- Causal inference in bipartite observational settings
  - ▷ Introduce new types of causal questions and estimands
  - ▷ Complex exposure patterns generate different types of interference, going beyond unit-to-unit or spatial interference
  - ▷ New notions of confounding and homophily
  - ▷ New methods for **bipartite causal inference**
- Relevance for many other interventions with a clear distinction between intervention and outcome units

## References

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