

# UNCERTAINTY, OPENNESS TO NOVELTY AND ECONOMIC GROWTH

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# Motivation

*"First, technology has to be invented or adopted. Human societies vary in lots of independent factors affecting their openness to innovation."*

JARED DIAMOND, 2003

# Motivation

- Technological progress through successful innovations = key driver of long-run economic growth
- Innovations → UNCERTAINTY (i.e. a lack of information)
- Growth literature has abstracted from uncertainty so far
- Decisions under uncertainty come with:
  - subjective beliefs coloured by personality traits, past experience, narratives
  - ↔ hypes, misallocation, disappointment, possibly paralysis

# Motivation

- ▶ These are not just innocuous by-products but sometimes have significant feedback effects!

→ Bubbles & crashes!



Image Sources: Seeking Alpha, Bloomberg, Focus Economics

# Motivation

## Openness to Novelty:

Entrepreneurs' intrinsic attitudes towards innovation

⇒ How does openness to novelty matter? Unclear!

- ▶ More openness:
  - Potential innovations are more likely to be tested, quicker adoption of technology
  - Lack of scepticism → ignorance of negative signs, exuberance, misallocation, possibly crisis-induced paralysis

# Motivation

- 1 Which economy grows faster? One with more or less **average** openness?
- 2 What about **heterogeneity** of openness within one economy? Is it detrimental or beneficial?

# Contribution

## A first glance at the data:

- Surprising but robust negative correlation between growth rate of GDP p.c. & a new measure of openness to novelty

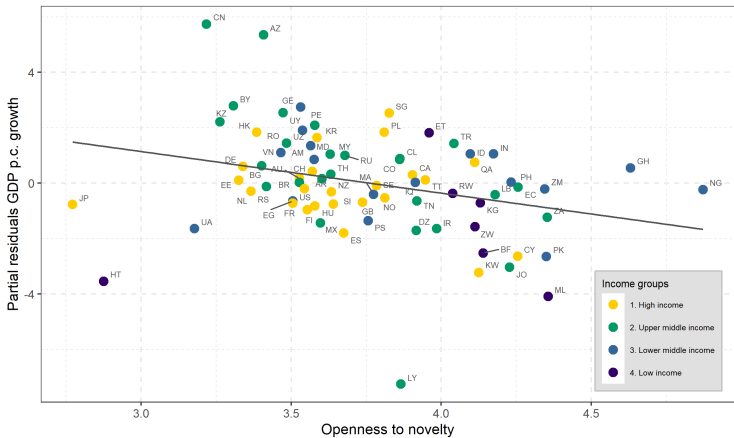
## A formal model with simulations:

Describes + analyses positive & negative mechanisms that link openness to novelty to long-run growth

- 1 General openness: mechanisms' relative strength changes  
→ hump-shaped relationship
- 2 Heterogeneity: clear positive impact on growth

▶ Literature

# Openness to Novelty and Economic Growth

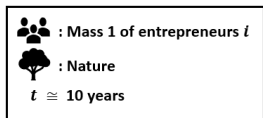


▸ Details

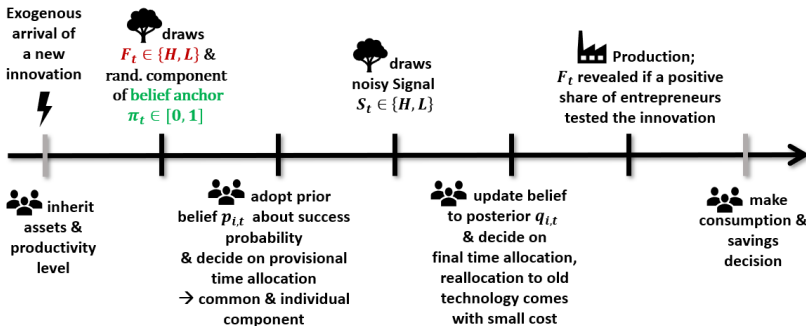
▸ Robustness



# Timeline of One Period/ Model Overview



**UNCERTAINTY**  
 $F_t$ : fundamental state,  
 i.e. whether innovation  
 is successful; success  
 probability is unknown



# Static Equilibrium

Time allocation via "backward approach"

⇒ categorisation of prior beliefs:

- **Pessimistic**: allocates entire time endowment to old method (no opportunity to reconsider)
- **Impartial**: provisionally allocates full time endowment to new method and then listens to the signal
- **Exuberant**: allocates full time endowment to new method and sticks to that decision even if  $S_t = L$

⇒ thresholds change each period

▶ Graph

# Common Belief Anchor $\pi_t$ Components

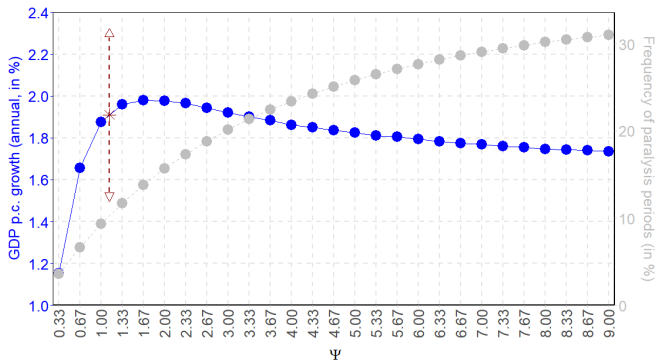
$$\pi_t = (\tilde{\pi}_t)^{1/\Psi} Q_t$$

<b>RANDOM FORCES</b>	$\tilde{\pi}_t \sim iid U[0, 1]$	E.g. (non-)appearance of a contagious narrative	<i>Shiller (2017,2019)</i>
<b>GENERAL OPENNESS</b>	$\Psi \in (0, \infty)$	Cultural component affecting economic decision making	<i>Guiso et al. (2006)</i>
<b>SPILOVERS of PAST EXUBERANCE</b>	$Q_t=0$ if in $t-1$ positive share of exuberant entrepreneurs misallocates time	Negative experiences enhance downsides of experimenting with uncertain innovations & lead to temporarily more conservative priors	<i>Bordalo et al. (2012) &amp; Dittmar and Duchin (2016); Malmendier (2021)</i>

# Simulations

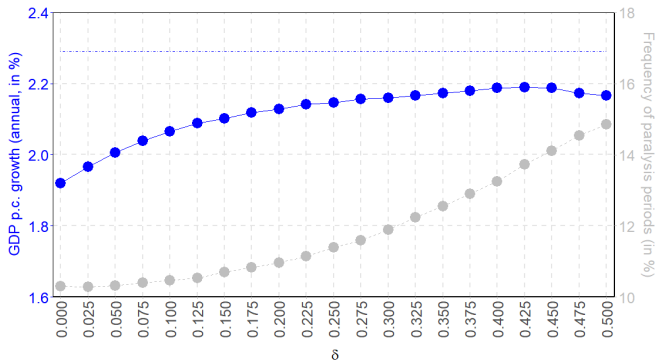
- 1 **General** openness to novelty and growth ( $\delta = 0$ )
- 2 **Heterogeneity** in openness to novelty and growth
  - ▶ 100,000 simulations of a 20-period economy ( $\hat{=} 200$  years)
  - ▶ Focus on Western European Economies

# General Openness to Novelty & Growth



⇒ Annual GDP p.c. growth falls by  $\sim 0.25$  pp from the peak of  $\Psi$  to the upper bound

# Heterogeneity in Openness to Novelty & Growth



⇒ Annual GDP p.c. growth increases by  $\sim 0.36$  pp from lower end of  $\delta$  to max

*Note:* The horizontal dashed line indicates GDP p.c. growth in a simulated economy that is populated by entrepreneurs who stick to the principle of indifference.

## Take-Aways

- **Uncertainty** about innovations offers room for **subjective beliefs** and **narratives** which can create booms, busts & potential paralysis on the macro level of an economy
- **General openness to novelty** has an ambiguous (hump-shaped) effect: at a low level, an increase is extremely beneficial (curiosity/experimentation) but relatively quickly the relationship becomes negative (exuberant beliefs) with a sizeable impact on long-term growth
- **Heterogeneity in openness to novelty** appears to have a non-negligible positive effect on long-term growth

Thank You!



# Literature

- **Effect of culture on long-run economic development:**  
 Doepke and Zilibotti (2008), Galor and Özak (2016),  
 Gorodnichenko and Roland (2017), Sunde et al. (2022),...
- **Cultural influences on prior beliefs:**  
 Guiso et al. (2006, 2008), Mokyr (2017)
- **Impact of experience effects on priors:**  
 Malmendier and Tate (2011), Dittmar and Duchin (2016),  
 Guiso et al. (2018), Malmendier (2021)
- **Relaxing the common prior assumption (heterogeneity):**  
 e.g. Gilboa et al. (2014) - welfare analysis
- **Diversity along various dimensions connected to long-run growth:** e.g. Ashraf and Galor (2013) - genetic diversity

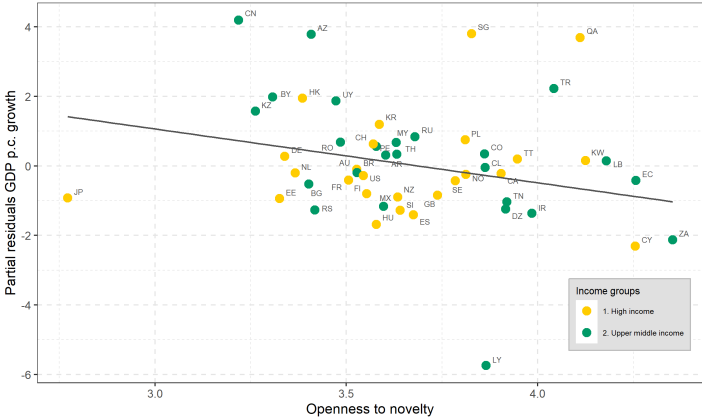


# Robustness

- Removing outliers (5% in each dimension)
- Subgroups: without low income countries, without low and lower middle income countries
- Additional Controls: quality of institutions, human capital
- Each item separately

◀ Empirical Motivation

# Robustness



◀ Simulations

Table: Baseline and Subsets

	<i>Dependent variable: Average annual GDP p.c. growth</i>			
	(1) Baseline	(2) W/o outliers	(3) W/o low income	(4) W/o low & lower middle income
Openness to Novelty	-1.669*** (0.601)	-2.185*** (0.570)	-2.110*** (0.595)	-2.759*** (0.806)
log(GDP2005)	-1.379*** (0.214)	-1.274*** (0.168)	-1.802*** (0.242)	-1.994*** (0.367)
Constant	21.815*** (3.487)	22.829*** (3.150)	27.721*** (3.674)	32.133*** (4.787)
Observations	75	67	68	51
R <sup>2</sup>	0.370	0.477	0.470	0.457
Adjusted R <sup>2</sup>	0.352	0.460	0.454	0.435
Residual Std. Error	1.869	1.324	1.713	1.790
F Statistic	21.118***	29.131***	28.832***	20.236***

Note:

\* p&lt;0.1; \*\* p&lt;0.05; \*\*\* p&lt;0.01





# Final Good Sector

→ single final good  $Y$  produced from capital  $K$  and intermediate good  $X$  with CES aggregate PF:

$$Y_t = Y(K_t, X_t) = (K_t)^\alpha (X_t)^{1-\alpha}, \tag{1}$$

where  $\alpha \in (0, 1)$

→ rental rate  $r$  of capital & technology good price  $m$ :

$$r_t = \alpha(K_t/X_t)^{\alpha-1} - \kappa \quad \text{and} \quad m_t = (1 - \alpha)(K_t/X_t)^\alpha \tag{2}$$



# Timeline of One Period / Model Overview



: mass 1 of entrepreneurs  $i$



: nature

$F_t$ : fundamental state,  
i.e. whether innovation  
is successful

$o$ : old  
 $n$ : new

Arrival of  
innovation



$A_t^n$



draws  
 $F_t \in \{H, L\}$  &  
belief anchor  
 $\pi_t \in [0, 1]$



draws  
noisy Signal  
 $S_t \in \{H, L\}$



Production,  
 $F_t$  revealed if  
 $I_{i,t}^n > 0$



inherit  
assets  $k_{i,t}$  &  
productivity  $A_t^o$   
( $A_{t-1}^o$  or  $A_{t-1}^n$ )



adopt prior  
belief  $p_{i,t}$   
& decide on  
provisional time  
allocation  $\bar{l}_{i,t}^o, \bar{l}_{i,t}^n$





update belief  
to posterior  $q_{i,t}$   
& decide on  
final time allocation  
 $l_{i,t}^o, l_{i,t}^n$



make  
consumption &  
savings decision  
 $c_{i,t}$  &  $k_{i,t+1}$

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# Technologies

## Final Good Sector:

- Single final good PF:  $Y_t = (K_t)^\alpha (X_t)^{1-\alpha}$
- Factor prices,  $r_t$  and  $m_t$ , = marg. productivities (less depreciation for capital)

## Intermediate Good Sector:

- $X_t$  produced by continuum (mass 1) of independent entrepreneurs  $i$  who also own & supply  $K_t$
- Each period access to two production methods:  $A_t^o$  &  $A_t^n$   
 PFs:  $x_{it}^o = A_t^o \ell_{it}^o$  and  $x_{it}^n = A_t^n \ell_{it}^n$ ,  
 →  $\ell_{it}$ : time of entrepreneur  $i \in [0, 1]$ ,  $\ell_{it}^o + \ell_{it}^n = 1$

# Technologies

- Productivity of new method depends on fundamental  $F_t$ :

$$A_t^n = \begin{cases} \theta^H A_t^o & \text{if } F_t = H \\ \theta^L A_t^o & \text{if } F_t = L \end{cases}, \quad (3)$$

where  $\theta^H > 1 > \theta^L$  (for simplicity  $\theta^L = 1/\theta^H$ )

- "Default technology" ( $F_t$  not always revealed)

$$A_{t+1}^o = \begin{cases} A_t^n & \text{if } F_t \text{ revealed } \vee F_t = H \\ A_t^o & \text{otherwise} \end{cases} \quad (4)$$

# Technologies

## Entrepreneurs' **time allocation decision:**

1. Provisional choice  $\tilde{\ell}_{it}^k$  without information on  $Pr(F_t = H)$  based on subjective prior  $p_{it}$
2. Potential to terminate use of new technology after updating belief according to Bayes' Rule based on receiving a **signal**  $S_t \in \{H, L\}$  about  $F_t$  with signal quality  $\sigma = Pr(S_t = F_t) > 1/2$   
 → Withdrawing from new technology comes with a **small loss of time**  $(1 - \lambda)$

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make  
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# Prior Beliefs $p_{i,t}$

## Uncertainty and Beliefs

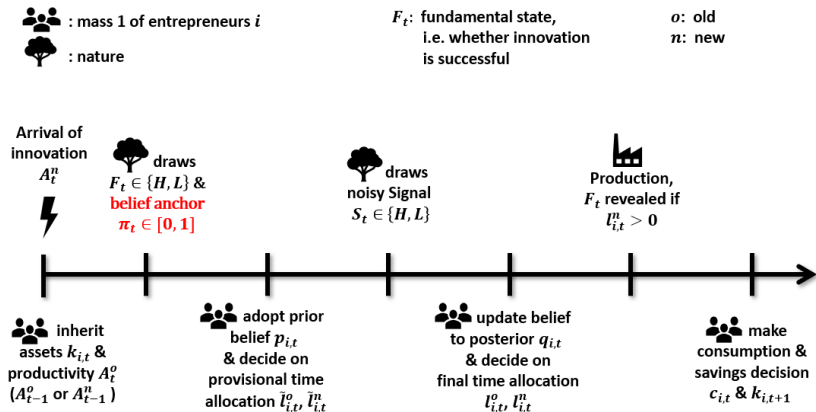
→ Entrepreneurs adopt a subjective prior belief about  $Pr(F_t = H)$ :

$$p_{it} = \pi_t^{(1/\psi_i)-1} \quad (5)$$

- $\pi_t \in (0, 1)$ : **belief anchor**
- $\psi_i$ : entrepreneur-specific characteristic, i.e. individual openness to novelty  
 →  $\psi_i \sim U[\frac{1}{2} - \delta, \frac{1}{2} + \delta]$ ,  $\delta \in (0, \frac{1}{2})$ : degree of belief heterogeneity

▶ Graph

# Timeline of One Period/ Model Overview





# Entrepreneurs: Prior Beliefs $p_{it}(\pi_t; \psi_i) = \pi_t^{(1/\psi_i)-1}$

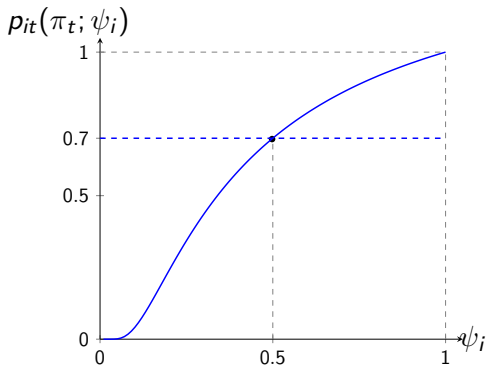


Figure: Distribution of  $p_{it}$  with max. heterogeneity &  $\pi_t = 0.7$

# Distribution of Openness to Novelty $\psi_i$

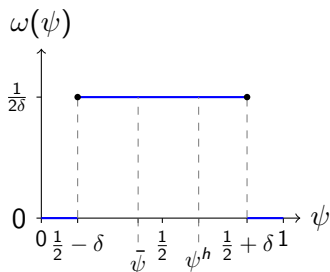


Figure: Distribution of  $\psi$

→ density function  $\omega$ :

$$\omega(\psi) = \begin{cases} 1/(2\delta) & \text{if } \psi \in [1/2 - \delta, 1/2 + \delta] \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

# Belief Anchor $\pi_t$

In practice, **belief anchor** affected by

- Random forces, e.g. (non-)appearance of a contagious narrative (*Shiller, 2017,2019*)
- General openness: cultural component affecting economic decision making (*Guiso et al., 2006*)
- Spillovers of past exuberance: leads to lower anchor  
→ captures that negative experiences enhance downsides of experimenting with uncertain innovations (*Bordalo et al., 2012*) & lead to temporarily more conservative priors (*Dittmar and Duchin, 2016; Malmendier, 2021*)

## Belief Anchor $\pi_t$

→ Components of the **belief anchor**:

$$\pi_t = (\tilde{\pi}_t)^{1/\Psi} Q_t$$

- $\tilde{\pi}_t \sim iid U[0, 1]$ : random forces (e.g. narratives)
- $\Psi \in (0, \infty)$ : general level of openness (cultural component)  
→ the larger  $\Psi$ , the larger the mean of  $(\tilde{\pi}_t)^{1/\Psi}$
- $Q_t$ : spillovers of past exuberance  
→ chance of  $Q_t = 0$  if in previous period a positive share of exuberant entrepreneurs (who ignored  $S_t = L$ ) allocated time to a failed innovation

# Entrepreneurs: Preferences & Aggregation

## Consumption and Saving Decision

- Preferences over  $c_{it}$  &  $k_{it+1}$ :  $U_{it} = \mathbb{E}_{it} \{ (c_{it})^{1-\beta} (k_{it+1})^\beta \}$   
 ( $\beta \in (0, 1)$ ) s.t.  $i$ 's flow budget constraint

$$k_{it+1} = (1 + r_t)k_{it} + m_t x_{it} - c_{it}$$

- Decision after resolution of uncertainty  $\Rightarrow$  time allocation maximises

$$U_{it} = (1 - \beta)^{1-\beta} \beta^\beta \mathbb{E}_{it} \{ (1 + r_t)k_{it} + m_t(x_{it}^o + x_{it}^n) \}$$

Aggregation over mass 1 of entrepreneurs

# Timing

Within each period  $t$ , there is a maximum of seven stages. The sequence of events is as follows:

1. From the previous period, all entrepreneurs  $i \in [0, 1]$  inherit their individual asset holdings,  $k_{it}$ , and the productivity level  $A_t^o$  (either  $A_{t-1}^o$  or  $A_{t-1}^n$ ).
2. Nature draws the initially unobservable fundamental of the new production method,  $F_t \in \{H, L\}$ , as well as the belief anchor,  $\pi_t \in [0, 1]$ .
3. Observing  $\pi_t$ , all entrepreneurs adopt a subjective prior belief about  $\Pr[F_t = H]$ ,  $p_{it}$ , and then decide on the provisional time allocation,  $(\tilde{\ell}_{it}^o, \tilde{\ell}_{it}^n)$ .

# Timing

If non of the entrepreneurs provisionally allocates time to the new production method, stages 4 and 5 are skipped. Otherwise, the sequence continues with stage 4:

4. Nature draws the informative but noisy signal about the fundamental,  $S_t \in \{H, L\}$ .
5. Observing  $S_t$ , all entrepreneurs with  $\tilde{\ell}_{it}^n > 0$  form their posterior belief,  $q_{it}$ , and then decide on the final time allocation,  $(\ell_{it}^o, \ell_{it}^n)$ .
6. Production takes place, incomes are incurred (and the  $z_{it}$ s observed), and - provided that  $\ell_{it}^n > 0$  for some entrepreneurs -  $F_t$  is inferred.
7. All entrepreneurs divide  $z_{it}$  between current consumption,  $c_{it}$ , and future assets,  $k_{it+1}$ .

# Time

## Period Length:

- One period starts with arrival of new innovation and ends with (possible) resolution of uncertainty
- ▶ *Goldfarb and Kirsch (2019)*, tracing major innovations over past 180 years, suggest window of  $\sim 15$  years for major innovations
- ▶ *Dedehayir and Steinert (2016)*, dealing with hype cycles surrounding innovations:  $\sim 2$ -20 years, "normal technologies"  
 $\sim 5$ -8 years

⇒ Based on this we choose **10 years** for calibration



# Static Equilibrium: Time Allocation Decision - Backwards Approach

## (1) **Termination Decision:**

Entrepreneur  $i$  receives signal  $S_t \in (L, H)$  with quality  $\sigma = Pr(S = F) > \frac{1}{2}$  and updates prior  $p_{it} = Pr_i(F_t = H)$  to posterior  $q_{it} = Pr_i(F_t = H)$

$\Rightarrow$  decision whether to terminate if they had previously invested some time in new method ( $\tilde{\ell}_{it}^n > 0$ )

## (2) **Time Allocation decision:**

Based on subjective prior  $p_{it} = Pr_i(F_t = H)$

$\Rightarrow$  time allocation decision old and/or new method

## Static Equilibrium: Time Allocation Decision

- Update prior  $p_{it}$  to posterior  $q_{it}$  with Bayes' rule:

$$q_{it}(S_t, p_{it}, \sigma) = \begin{cases} \left[ 1 + \frac{1-p_{it}}{p_{it}} \frac{1-\sigma}{\sigma} \right]^{-1} & : S_t = H \\ \left[ 1 + \frac{1-p_{it}}{p_{it}} \frac{\sigma}{1-\sigma} \right]^{-1} & : S_t = L \end{cases} . \quad (7)$$

- Condition to continue (assuming investment in new method):

$$q_{it}\theta^H A_t^o \tilde{\ell}_{it}^n + (1 - q_{it})\theta^L A_t^o \tilde{\ell}_{it}^n \geq \lambda A_t^o \tilde{\ell}_{it}^n \quad (8)$$

- Resulting threshold:

$$\bar{q} = \frac{\lambda - \theta^L}{\theta^H - \theta^L} \in (0, 1). \quad (9)$$

# Static Equilibrium: Termination Decision

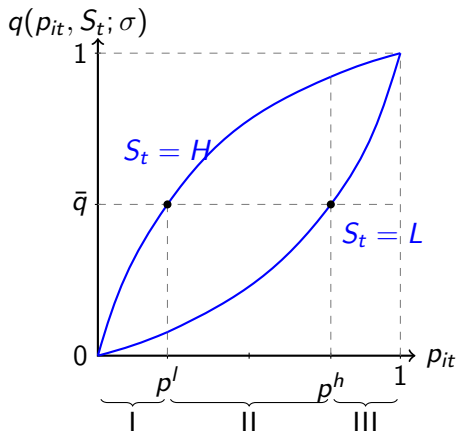


Figure: Posterior belief  $q_{it}$  as a function of  $p_{it}$  and  $S_t$

## Static Equilibrium: Termination Decision

- $q_{it}(H, p^l) = \bar{q}$ :

$$p^l = \frac{(1 - \sigma)(\lambda - \theta^L)}{\lambda - \theta^L + \sigma(\theta^H + \theta^L - 2\lambda)}. \quad (10)$$

- $q_{it}(L, p^h) = \bar{q}$ :

$$p^h = \frac{\sigma(\lambda - \theta^L)}{\theta^H - \lambda + \sigma(2\lambda - \theta^L - \theta^H)}. \quad (11)$$

# Static Equilibrium: Provisional Time Allocation

I)

$$\mathbb{E}_{p_{it} \in I} [x_{it}(0, 1)] = \lambda A_t^o. \quad (12)$$

II) Signal is decisive

		$S_t =$	
		H	L
$F_t =$	H	$p_{it}\sigma$	$p_{it}(1-\sigma)$
	L	$(1-p_{it})(1-\sigma)$	$(1-p_{it})\sigma$

$$\mathbb{E}_{p_{it} \in II} [x_{it}(0, 1)] = \left\{ p_{it}\sigma\theta^H + (1-p_{it})(1-\sigma)\theta^L + [p_{it}(1-\sigma) + (1-p_{it})\sigma] \lambda \right\} A_t^o. \quad (13)$$

III)

$$\mathbb{E}_{p_{it} \in III} [x_{it}(0, 1)] = [p_{it}\theta^H + (1-p_{it})\theta^L] A_t^o. \quad (14)$$

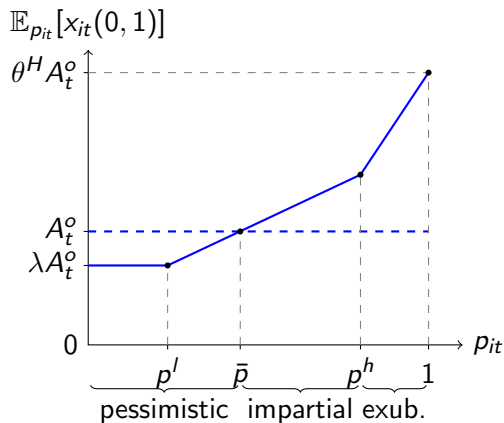
## Static Equilibrium: Provisional Time Allocation

$$\mathbb{E}_{\bar{p}}[x_{it}(0, 1)] = A_t^o \quad (15)$$

⇒ Invest time in new method for all  $p_{it} > \bar{p}$ :

$$\bar{p} = \frac{1 - \theta^L + \sigma(\theta^L - \lambda)}{\lambda - \theta^L + \sigma(\theta^H + \theta^L - 2\lambda)}. \quad (16)$$

# Static Equilibrium: Provisional Time Allocation



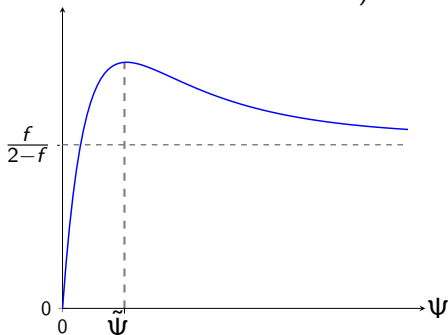
**Figure:** A priori exp output with full time endowment allocated to new method

← Static EQ

# Static Equilibrium: Analysis

Figure: Openness to novelty and the pace of innovation—theory

Pr(new method revealed to be a success)





# Parameter Values

Panel A			
Parameter	Description	Determination	Value
$\alpha$	Reproducible capital's share	Literature	0.20
$\kappa$	Depreciation rate	Literature	0.79
$\theta^H$	Innovation size	Literature	1.75
$\lambda$	Reallocation share	Literature	0.95
$\Psi$	Openness to Novelty	World Value Survey	1.13
$\beta$	Weight of future assets	Calibration	0.217
$\sigma$	Signal quality	Calibration	0.896
$f$	Obj. $\Pr(F_t=H)$ (unknown)	Calibration	0.450
Panel B			
	Avg. GDPp.c. Growth	SD GDPp.c. Growth	Avg. Int. Rate
Data	0.019	0.008	0.029
Model	0.019	0.007	0.029

Table: Parametes and Moments [▶ Determination Details](#)

## Parameter Values

- $\alpha$  &  $\kappa$ : Caselli and Freyer (2007) for Western European countries,  $\kappa$  translated to 10 year frequency
- $\theta^H$ : Akcigit and Kerr (2018)
- $\Psi$ : data from our empirical motivation (World Value Survey)
- $\beta, \sigma$  &  $f$ : calibrated to match mean & std.dev. of 20 Western European GDP p.c. growth rate 1820-2018 (Maddison Project Database: Bolt and Van Zanden, 2020) as well as mean annual real interest rate 1820-2018 of 5 Western European countries (Schmelzing, 2020)

◀ Parameters

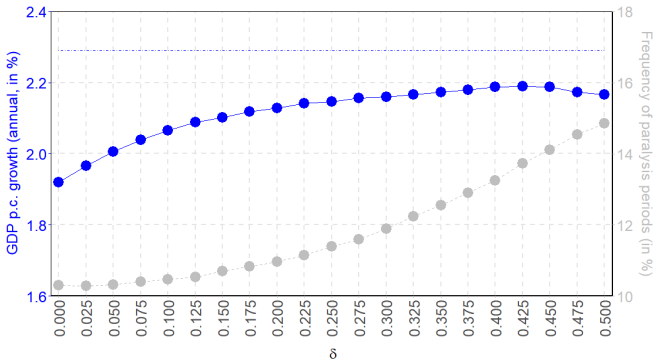


## General Openness to Novelty & Growth

- Annual GDP p.c. growth rises by 0.84 pp (from 1.15% to 1.99%) from lower bound of  $\Psi$  to peak (1.67)
  - It falls by  $\sim 0.25$  pp to 1.73% as  $\Psi$  approaches upper bound
  - If two countries start with same GDP p.c.,  $\frac{1}{4}$  of a pp growth differential means: after 100 years, GDP p.c. in one country is just 78% of that in the other
- ▶ Consistency with empirical observation?!

▶ Empirical Motivation

# Heterogeneity in Openness to Novelty & Growth



*Notes.* Each dot results from 100,000 simulations of a 20-period (200 years) economy. The horizontal dashed line indicates GDP p.c. growth in a simulated economy that is populated by entrepreneurs who stick to the principle of indifference.

## Heterogeneity in Openness to Novelty & Growth

- For most part of the range, growth rate monotonically increases in  $\delta$  (from 1.91% p.a. to max of 2.27% p.a.)
- Difference of 0.36 pp in terms of annual growth = sizeable effect
- ▶ Mean-preserving increase in heterogeneity makes some entrepreneurs more open for experimentation & learning without giving a boost to the risk that a large number of entrepreneurs adopt an exuberant prior at the same time

## Technology Good Sector: Aggregation

⇒ aggregate supply of  $X_t$ :

$$X_t = \int_0^1 (x_{it}^o + x_{it}^n) di = \int_0^1 (A_t^o \ell_{it}^o + A_t^n \ell_{it}^n) di. \quad (17)$$

# Aggregation

⇒ aggregate level of capital:

$$K_{t+1} = \int_0^1 (k_{it}) di = \int_0^1 (\beta[(1+r_t)k_{it} + m_t x_{it}]) di = \beta[(1+r_t)K_t + m_t X_t] \quad (18)$$

⇒ aggregate level of consumption:

$$C_t = \int_0^1 (c_{it}) di = \int_0^1 ((1-\beta)[(1+r_t)k_{it} + m_t x_{it}]) di = (1-\beta)[(1+r_t)K_t + m_t X_t] \quad (19)$$



# Aggregation: Technology Good

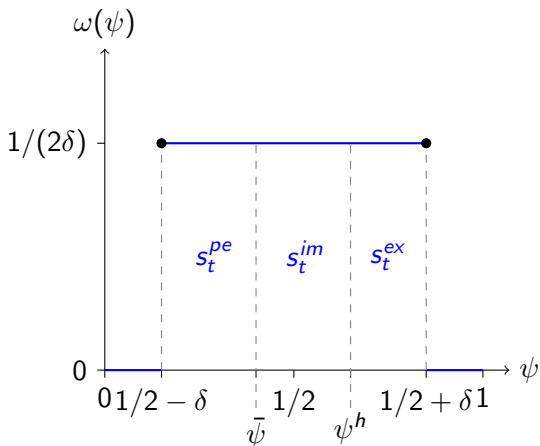


Figure: Distribution of  $\psi$  and categorisation

## Aggregation: Technology Good

→ with:

$$\bar{\psi}(\pi_t) = [1 + \ln(\bar{p}) / \ln(\pi_t)]^{-1} \quad \text{and} \quad \psi^h(\pi_t) = [1 + \ln(p^h) / \ln(\pi_t)]^{-1}$$

→ which yields the shares:

$$s_t^{pe} = \int_0^{\bar{\psi}(\pi_t)} \omega(\psi) d\psi$$

$$s_t^{im} = \int_{\bar{\psi}(\pi_t)}^{\psi^h(\pi_t)} \omega(\psi) d\psi$$

$$s_t^{ex} = \int_{\psi^h(\pi_t)}^1 \omega(\psi) d\psi$$

## Aggregation: Technology Good

⇒ Aggregation:

$$X_t = s_t^{pe} A_t^o + s_t^{im} [\mathbf{1}_{S_t=H} \cdot A_t^n + \mathbf{1}_{S_t=L} \cdot A_t^o \lambda] + s_t^{ex} A_t^n$$

→ with:

$$A_{t+1}^o = \begin{cases} A_t^n & \text{if } F_t = H \wedge (s_t^{im} \cdot \mathbf{1}_{S_t=H} > 0 \vee s_t^{ex} > 0) \\ A_t^o & \text{otherwise} \end{cases} \quad (6')$$

# General Openness to Novelty and Growth - Analytical Results

## PROPOSITION 2

*Suppose that  $\bar{p} < p^h$  and  $\psi_i = 1/2$  for all  $i$  (no heterogeneity in openness to novelty). Then, for any arbitrary period  $t$ ,*

$$\Pr[Q_t = 1] = \left\{ 1 + (1 - f) \left[ 1 - (p^h)^\Psi \right] \right\}^{-1},$$

*where  $f$  is the time-invariant probability of  $F_t = H$  (which is not known to the entrepreneurs).*

# General Openness to Novelty and Growth - Analytical Results

## PROPOSITION 3

*Suppose that  $\bar{p} < p^h$  and  $\psi_i = 1/2$  for all  $i$  (no heterogeneity in openness to novelty). Then, for any arbitrary period  $t$*

$$\Pr[\text{new method in } t \text{ revealed to be a success}] = f \frac{1 - (1 - \sigma)(p^h)^\Psi - \sigma(\bar{p})^\Psi}{1 + (1 - f) [1 - (p^h)^\Psi]},$$

*where  $f$  is the time-invariant probability of  $F_t = H$  (which is not known to the entrepreneurs).*

# General Openness to Novelty and Growth - Analytical Results

## PROPOSITION 4

Suppose that the signal's quality,  $\sigma \in (1/2, 1]$ , is sufficiently large such that

$$f < \frac{2\sigma - 1}{\sigma},$$

where  $f$  is the time-invariant probability of  $F_t = H$  (which is not known to the entrepreneurs). Then,  $\Pr[\text{new method in } t \text{ revealed to be a success}]$  is a quasi-concave function of  $\Psi \in [0, \infty)$ . As  $\Psi$  rises from zero towards infinity, it monotonically increases from zero to some maximum level that is strictly greater than  $f/(2 - f)$  and then monotonically decreases towards  $f/(2 - f)$ .

# General Openness to Novelty and Growth - Analytical Results

## PROPOSITION 5

Suppose that  $\bar{p} < p^h$  and  $\psi_i = 1/2$  for all  $i$  (no heterogeneity in openness to novelty). Then, for any two periods  $t$  and  $t + 1$ , the expected growth rate of the “technology frontier” is given by

$$\mathbb{E}_f \left\{ \frac{A_{t+1}^o - A_t^o}{A_t^o} \right\} = (\theta^H - 1)f \frac{1 - (1 - \sigma)(p^h)^\Psi - \sigma(\bar{p})^\Psi}{1 + (1 - f)[1 - (p^h)^\Psi]},$$

where the notation  $\mathbb{E}_f \{ \cdot \}$  indicates that the expectation is based on the true chance of  $F_t = H$ .



## Future Research

- More extensive empirical analyses
- Investigating the origins of differences (both general & heterogeneity): through what mechanisms can such differences emerge/persist?
- Possible policy implications? Incentives to experiment/invest in uncertain innovations country-dependent?