

# A Theory of Crowdfunding Dynamics

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# What is Crowdfunding?

## Crowdfunding:

Open call to many small contributors (usually online).

## Reward-based crowdfunding:

- Funders buy a product that the entrepreneur will produce *after* the campaign.
- Crowdfunding is a form of pre-selling to cover production costs.
- Funders bid the price of the crowdfunding product.  
(we call them bidders)

## Canonical format

- *Aggregate Fund Threshold*: funding goal
- *AoN*: succeeds if funds reach goal by deadline, else fails
  - $\mathcal{S}$  (success)  $\rightarrow$  Bids paid, production occurs, rewards delivered;
  - $\mathcal{F}$  (failure)  $\rightarrow$  Bids reimbursed, no production.
- Reward-based AoN crowdfunding is a popular choice because:
  - It is easy to initiate in practice;
  - Gives to entrepreneurs a market-test that protects from demand uncertainty.

# Popular reward-based crowdfunding platforms

- **Kickstarter** (US)  
235 ML financed projects, 7 BN USD raised from 2009 as of 2023.
- **Indiegogo** (US)  
800 K financed projects, 2 BN USD raised since 2009 as of 2023.
- **Kisskissbankbank** (FR)  
33 K financed project, 150 ML EUR raised from 2009 as of 2023.
- **Verkami** (SP)  
12 K financed projects, 50 ML EUR raised from 2010 as of 2023.
- **Produzioni Dal Basso** (IT)  
8 K financed projects, 23 ML EUR raised from 2005 as of 2023.

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(Recently announced future integration with the blockchain Celo)
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There is also crowdfunding taking place outside big platforms.

(Radiohead's album "In Rainbows" was financed with crowdfunding in 2007 directly on the band's website)

# Anatomy of a crowdfunding campaign

KICKSTARTER

Name and slogan

→ KINDALU®: a new cable case, that solves all cable problems

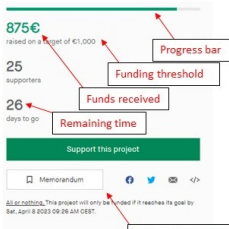
All your cable frustrations – solved with a twist of your finger! 3D PRINTED - UNTANGLE THE CHAOS



Promotional video



Blog



Remind me button

Funding gap = 1.000€ – 875€ = 125€

Contribution without reward

10 €

Support him because you believe in this project.

Support the project without any reward: do so if it really inspires you.

Contribution of €59 or more

KICKSTARTER ALL 3 PACK | 1.5M + 2M + 3M

10% OFF

Get a super discounted KINDALU ALL THREE PACK: 1.5M + 2M + 3M

KINDALU 1.5M - holds cables up to 1.5 meters (5ft) long.  
KINDALU 2M - holds cables up to 2 meters (6.5ft) long.  
KINDALU 3M - holds cables up to 3 meters (10ft) long.

Shipping costs will be determined once the campaign is over in order to secure the best shipping options

ESTIMATED DELIVERY DATES TO: Jun 2023 Worldwide

4 supporters [Complements](#)

Contribution of €15 or more

SUPER EARLY BIRD | KINDALU 1.5 M

30% OFF

Get your KINDALU at a SUPER DISCOUNT PRICE. KINDALU 1.5M - Holds cables up to 1.5 meters (5ft) long.

Shipping costs will be determined once the campaign is over in order to secure the best shipping options.

ESTIMATED DELIVERY DATES TO: Jun 2023 Worldwide

4 supporters [Complements](#)  
Limited quantity (71 of 75 left)

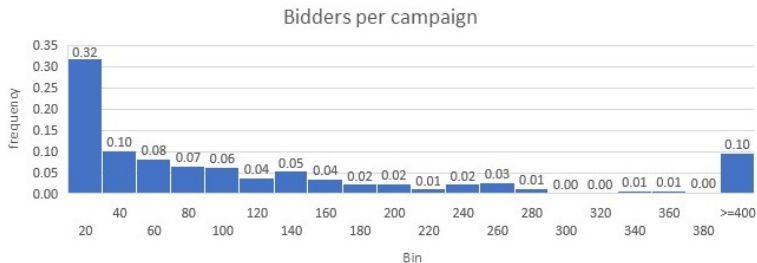
Price tiers

# Statistics from Kickstarter

- **Bids:**

Heavily right-skewed funding distribution:

60 bidders in median, most bidding once per campaign.

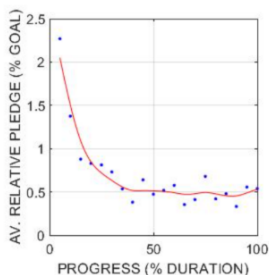
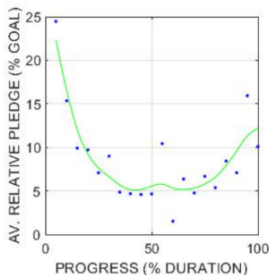


- **Duration:** often 30 or 60 days.
- **Goal:** 5 K USD in median (median pledge: 25 USD), but heterogeneous across categories: (bigger for technology, games, design; smaller for music, food, crafts).
- **Success rate:** 30-40%.



# Empirical puzzle

- Average time profile of bids is a “U-shape” for successful campaigns and an “L-shape” for failed campaigns.



Bidding (as threshold percentage) over time. Bids averaged over all 03/01/2014-02/05/2014, Kickstarter campaigns, conditioning on success (in green), failure (in red).

- What incentives drive these patterns?
- Can we use them to assess the welfare implications of current crowdfunding practices?
- Can we use them to optimize platform and campaign design?

# Determinants of bidding dynamics

- Bid dynamics originate when production uncertainty faced by bidders combines with sunk bidding costs:
- *Aggregate Fund Threshold*: funding goal  $\implies$  strategic complementarity
- *AON*: succeeds if funds reach goal by deadline, else fails
  - $\mathcal{S}$  (success)  $\rightarrow$  Bids paid, production occurs, rewards delivered;
  - $\mathcal{F}$  (failure)  $\rightarrow$  Bids reimbursed, no production
  - $\implies$  no sunk costs in prior works
- But *inspection* involves sunk costs.
- So real-time disclosure of bidding aggregates creates dynamic interactions:
- Bidders sunk the bidding cost only if their estimate of the campaign's success probability is sufficiently high.

# Contribution of this paper

- Characterize co-evolution of bidding and project success rates.
  - Pivotality often substantial given sequential moves  
(30% of campaigns attract  $< 20$  bids)
- Welfare implications of funding disclosure (transparency).
- Optimal price and threshold.
- Price dynamics via price menus with limited quantities.

## Closest Papers

- Alaei et al (2019)
- Deb et al (2021)
- Ellman & Hurkens (2019)

## Campaign

- Price  $p$
- Bidder gap  $g_0 \in \mathbb{N}_+$ .  
(everyone pays the same price: funding gap  $\rightarrow$  bidder gap)
- deadline  $\tau \in \mathbb{R}_+$  (outcome determined at  $\tau_+$ ).
- Time  $t \rightarrow$  time left  $\tau - t$

## Bidders

- Poisson arrival rate  $\lambda$  of bidders over  $[0, \tau]$
- Valuations  $v_t = \begin{cases} v & q \\ 0 & 1 - q \end{cases}$
- Inspection costs  $c_t$  drawn from CDF  $F(\cdot)$  on  $[0, q]$

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# Strategies and equilibrium

- Bidder  $t$  observes the funding state  $(t, g)$  on arrival
  - He also knows  $(c_t, g_0, \tau, p, \lambda, q)$
- Success probability — (funding) state  $(t, g)$ :

$$S_{(t,g)} \triangleq \mathbb{P}(\mathcal{S}|(t, g)) \equiv \mathbb{E}_{(t,g)} \left( \mathbb{1}_{g\tau_+ \leq 0} \right)$$

- Strategies  $a : (t, g, c) \rightarrow \{\mathbf{A}, \mathbf{B}, \mathbf{C}\}$  and their expected payoffs
  - **A** — no inspection, no bid  $\rightarrow U_{(t,g)}^{\mathbf{A}} = 0$
  - **B** — no inspection, bid
  - **C** — valuation-contingent bid  $\rightarrow$

$$U_{(t,g)}^{\mathbf{C}} = qS_{(t,g)}^{\text{bid}}d - c_t \quad d = v - p \quad S_{(t,g)}^{\text{bid}} = S_{(t,g-1)}$$

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$$U_{(t,g)}^{\mathbf{C}} = qS_{(t,g)}^{\text{bid}} - c_t \quad \text{normalization: } d = 1 \quad S_{(t,g)}^{\text{bid}} = S_{(t,g-1)}$$

Unique PBE; threshold strategies:

**C** if  $c_t \leq qS_{(t,g)}^{\text{bid}} \triangleq qS_{(t,g-1)}$ , else **A**.

Bidding rate:  $\beta_{(t,g)} = \lambda q F\left(qS_{(t,g)}^{\text{bid}}\right)$ .

Success rate

Using terminal conditions,  $S_{(\tau,g)} = 0$  for  $g > 0$ ,  $S_{(\tau,g)} = 1$  for  $g \leq 0$ ,

$$S_{(t,g)} = \int_t^\tau \left[ \exp\left(-\int_t^x \beta_{(u,g)} du\right) \beta_{(x,g)} \right] S_{(x,g-1)} dx \quad (\text{REC-}S)$$

- (REC- $S$ ) is an opaque expression, so we use stochastic calculus and a martingale insight to disentangle it.

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- (REC- $S$ ) is an opaque expression, so we use stochastic calculus and a martingale insight to disentangle it.

- Two effects describe the evolution of bidding rates from an initial date  $t$ , at a known gap  $g$ , to a future date  $x$  with a stochastic future gap  $g_x$ :

$$\mathbb{E}_{(t,g)} \left( \beta_{(x,g_x)} \right) - \beta_{(t,g)} = \lambda q \left[ \mathcal{E}_x^{(t,g)} + \mathcal{N}_x^{(t,g)} \right]$$

## Decreasing pivotality (DP)

- By LIE,  $S_{(t,g_t)}$  is a martingale w.r.t. to the natural filtration of  $g_t$ . That is,

$$\mathbb{E}_{(t,g)} \left( S_{(x,g_x)} \right) = S_{(t,g)}$$

- On the other hand, *Pivotality*,

$$\Delta S_{(t,g_t)} \triangleq S_{(t,g_{t-1})} - S_{(t,g_t)}$$

is a supermartingale (decreases in expectation).

- Strategic complementarity falls (on average) since a later bidder expects to have fewer bidders arriving after him.
- Combining the two insights, the bid-conditional success rate

$$S_{(t,g_t)}^{\text{bid}} = S_{(t,g_t)} + \Delta S_{(t,g_t)}$$

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# Pivotality effect (PE)

- The first is the **pivotality effect (PE)**:  $\mathcal{E}_x^{(t,g)}$ .
- PE is the effect of the *expected* decreasing pivotality trend.
- It is *always* negative or null (in trivial cases).

$$\mathcal{E}_x^{(t,g)} \triangleq F \left( \mathbb{E}_{(t,g)} \left( qS_{(x,g_x)}^{\text{bid}} \right) \right) - F \left( qS_{(t,g)}^{\text{bid}} \right)$$

# News effect (NE)

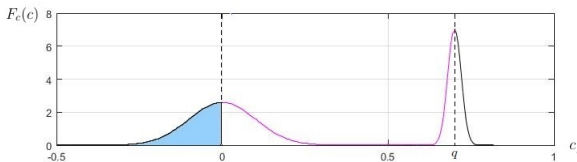
- The second effect is the **News effect (NE)**:  $\mathcal{N}_x^{(t,g)}$ .
- NE is the effect of the **variance** in the funding gap:  
Bidding is stochastic simply because of preference shocks and random arrivals.  
Bidders learn good or bad news depending on the gap they observe upon arrival.
- NE is determined by the sensitivity to news of the bidder population:
  - Null NE with linear cumulative inspection cost distribution  $F$
  - Negative NE with a concave  $F$  ( $\downarrow$  returns to good news)
  - Positive NE with a convex  $F$  ( $\uparrow$  returns to good news)
- Technically, the sign of the NE results from Jensen's inequality:

$$\mathcal{N}_x^{(t,g)} \triangleq \mathbb{E}_{(t,g)} \left( F \left( qS_{(x,g_x)}^{\text{bid}} \right) \right) - F \left( \mathbb{E}_{(t,g)} \left( qS_{(x,g_x)}^{\text{bid}} \right) \right)$$

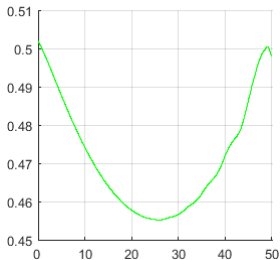


- Combining the two effects:
  - ⇒ Bid rate falls with concave or linear  $F$
  - ⇒ Bid rate rises with convex  $F$  if  $|\mathcal{N}| > |\mathcal{E}|$

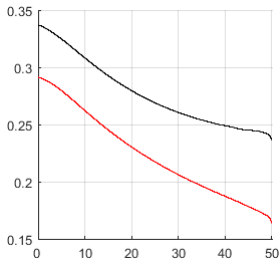
# Empirically salient funding patterns



Density



—  $A_t^S$



—  $A_t$  —  $A_t^F$

$$\text{Welfare: } W = V + RS_0$$

- We assume E's utility from success =  $R$  & neglect revenues.
- Realized arrival sequence  $\{t_n\}$ ,  $n = 1, 2, \dots, N$ .
- Bidder surplus:

$$V = \mathbb{E} \left( \sum_{n=1}^N u^{a(t_n, g_n, c_n)} \right) \underbrace{=}_{\text{Poisson arrivals}} \lambda \tau \mathbb{E} \left( U^{a(t, g_t, c_t)} \right)$$

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- We assume E's utility from success =  $R$  & neglect revenues.
- Realized arrival sequence  $\{t_n\}$ ,  $n = 1, 2, \dots, N$ .
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# Equilibrium of SIM

- In the baseline model the gap is disclosed in real time.
- Is transparency good for welfare?
- To answer this question, we compare our baseline (SEQ) to a no-information benchmark (SIM).
  
- In SIM, bidders arrive sequentially but do not observe  $g_t$ .
- Equilibrium strategies use a constant threshold type  $\hat{c}_{(t,g)} = \hat{c}$

# Welfare comparison of SIM and SEQ

- While in SIM surplus contributions are constant over time, in SEQ they decrease.
- DP and NE manifest themselves also in the welfare analysis:
  - 1 (infra-marginals): Surplus of types  $c_t \leq \hat{c}$  decreases due to DP.
  - 2 (semi-marginals): good-news effects from a bid activates types  $c_t \in (\hat{c}_{(t,g)}, \hat{c}_{(t,g-1)}]$ .
- SEQ yields higher welfare than SIM for polarized inspection costs.
- SIM yields higher welfare than SEQ when inspection costs are sufficiently concentrated (homogenous case).
- Intermediate information structures can improve on both SIM and SEQ.



## Main takeaways

- Characterization of bidding profiles with 2 new forces: pivotality and news effects
  - These effects combined with heterogeneous costs explain observed bidding profiles.
- Cost diversity and adverse conditions can explain real-time disclosure.
  - Partial disclosure can raise welfare
- Framework reveals price-threshold tradeoff, identifies optimal price dynamics, and allows for study of welfare effect of gap-dependent pricing.

## Next:

- Endogenous timing via option to delay (E and F 2021).
- Common value.

Thank you for your attention!

For the paper and the blog post, scan the QR codes below:



Paper



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