# Trends in Worker Bargaining Power 

Paolo Mengano<br>University of Zurich

August 29, 2023

## The Productivity-Pay Gap



Figure: The Productivity-Pay Gap
Economic Policy Institute

## Introduction

> How did worker bargaining power evolve over time?

1. Measure worker bargaining power

- structural method combining macroeconomics and industrial organization

2. Study the implications for the economy
3. Propose policy interventions
4. Shed lights on potential drivers

## Literature

1. Declining worker bargaining power

Stansbury\&Summers, 2020; Drautzburg et al, 2020; Lombardi et al, 2022; Ratner\&Sim, 2022

- microfounded evidence

2. Frictional labor markets with wage bargaining

Jaimovich et al., 2021, Dix-Carneiro et al., 2021, Cacciatore and Ghironi, 2021, ...

- theory-consistent value

3. Rent sharing

Card et al., 2018; Friedrich et al., 2021; Barth et al., 2016; Fakhfakh and FitzRoy, 2004,...

- model-consistent and time-varying

4. Monopsony

Manning, 2020; Berger et al., 2021; Jarosch et al., 2021; Yeh et al., 2022; Traina, 2021,...

- new evidence on how the surplus is split

Model

## Environment

Heterogeneous firms model with random search in the labor market (DMP)

Risk neutral workers and firms

- continuum of workers
- free entry determines \# firms

Workers (

- employed $\rightarrow$ working
- unemployed $\rightarrow$ searching


## Firms

- heterogeneous in productivity
- post vacancies


## Labor market

- random search frictions
- Nash bargaining


## Wage Equation

Nash bargaining:

$$
\operatorname{wage}(w)=\underset{w}{\arg \max }(\text { Firm Surplus })^{1-\tau}(\text { Worker Surplus })^{\tau}
$$

with $\tau$ being worker bargaining power

Solving the Nash product:

$$
w=\tau\binom{\text { marginal }}{\text { productivity }}+(1-\tau)\binom{\text { outside }}{\text { option }}+\tau\binom{\text { labor market }}{\text { conditions }}
$$

# Empirical Framework 

## Estimation With Firm Heterogeneity

$$
\text { Target equation: } w_{i s t}=\tau \mathrm{MPN}_{i s t}+(1-\tau) b_{s t}+\tau \theta_{s t} \kappa_{s t}+\varepsilon_{i s t}
$$

Three main challenges:

1. MPN is unobservable
2. endogeneity bias
3. $\left\{\begin{array}{c}\text { outside, } \\ \text { option }\end{array}, \begin{array}{c}\text { labor market } \\ \text { conditions }\end{array}\right\}$

## Estimation With Firm Heterogeneity

$$
\text { Target equation: } w_{i s t}=\tau \mathrm{MPN}_{i s t}+(1-\tau) b_{s t}+\tau \theta_{s t} \kappa_{s t}+\varepsilon_{i s t}
$$

Three main challenges:

1. MPN is unobservable $\rightarrow$ estimate MPN at the firm-level
2. endogeneity bias
3. $\left\{\begin{array}{c}\text { outside, } \\ \text { option }\end{array}, \begin{array}{c}\text { labor market } \\ \text { conditions }\end{array}\right\}$

## Estimation With Firm Heterogeneity

$$
\text { Target equation: } w_{i s t}=\tau \mathrm{MPN}_{i s t}+(1-\tau) b_{s t}+\tau \theta_{s t} \kappa_{s t}+\varepsilon_{i s t}
$$

Three main challenges:

1. MPN is unobservable $\rightarrow$ estimate MPN at the firm-level
2. endogeneity bias $\rightarrow$ IV strategy: lagged productivity
3. $\left\{\begin{array}{c}\text { outside, } \\ \text { option }\end{array}\right.$ labor market $\left.\begin{array}{c}\text { conditions }\end{array}\right\}$

## Estimation With Firm Heterogeneity

$$
\text { Target equation: } w_{i s t}=\tau \mathrm{MPN}_{i s t}+(1-\tau) b_{s t}+\tau \theta_{s t} \kappa_{s t}+\varepsilon_{i s t}
$$

Three main challenges:

1. MPN is unobservable $\rightarrow$ estimate MPN at the firm-level
2. endogeneity bias $\rightarrow$ IV strategy: lagged productivity
3. $\left\{\begin{array}{c}\text { outside, } \\ \text { option } ;\end{array} \begin{array}{c}\text { labor market } \\ \text { conditions }\end{array}\right\} \rightarrow$ fixed effects

## Estimation With Firm Heterogeneity

$$
\text { Target equation: } w_{i s t}=\tau \mathrm{MPN}_{i s t}+(1-\tau) b_{s t}+\tau \theta_{s t} \kappa_{s t}+\varepsilon_{i s t}
$$

Three main challenges:

1. MPN is unobservable $\rightarrow$ estimate MPN at the firm-level
2. endogeneity bias $\rightarrow$ IV strategy: lagged productivity
3. $\left\{\begin{array}{c}\text { outside, } \\ \text { option } ;\end{array} \begin{array}{c}\text { labor market } \\ \text { conditions }\end{array}\right\} \rightarrow$ fixed effects

Later: incorporate worker dimension

## Estimation With Firm Heterogeneity

$$
\text { Target equation: } w_{i s t}=\tau \mathrm{MPN}_{i s t}+(1-\tau) b_{s t}+\tau \theta_{s t} \kappa_{s t}+\varepsilon_{i s t}
$$

Three main challenges:

1. MPN is unobservable $\rightarrow$ estimate MPN at the firm-level
2. endogeneity bias $\rightarrow$ IV strategy: lagged productivity
3. $\left\{\begin{array}{c}\text { outside, } \\ \text { option } ;\end{array} \begin{array}{c}\text { labor market } \\ \text { conditions }\end{array}\right\} \rightarrow$ fixed effects

Later: incorporate worker dimension $\rightarrow$ no effect on aggregate trend

## Data

US: Compustat
financial information on universe of publicly listed firms

- balance sheet and income statement
- sales, \# employees, wages (lc/n), intermediate inputs, fixed assets, COGS
- period: 1960-2019


## Data

US: Compustat
financial information on universe of publicly listed firms

- balance sheet and income statement
- sales, \# employees, wages (lc/n), intermediate inputs, fixed assets, COGS
- period: 1960-2019
$\Rightarrow$ focus on Manufacturing: $\sim 37 \%$ of workforce


## Data

France: Administrative data

1. FARE/FICUS: financial information on universe of firms, 1994-2019 (2020)

- universe of private firms
- balance sheet and income statement


## Data

## France: Administrative data

1. FARE/FICUS: financial information on universe of firms, 1994-2019 (2020)
2. DADS-Postes: job-level information, 1994-2019 (2020)

- universe of employees
- wages, hours, age, office location, residence, occupation, contract, (collective agreement)
- anonymized data with firm identifier
- 2-year tracking


## Data

France: Administrative data

1. FARE/FICUS: financial information on universe of firms, 1994-2019 (2020)
2. DADS-Postes: job-level information, 1994-2019 (2020)
3. Robustness and extensions:
a) DADS-Panel: worker panel 1976-2019 (20), up to $8 \%$ of workforce $\rightarrow$ education
b) EAP: survey on production, 2008-19 (20) $\rightarrow$ prices
c) TIC Entreprises: survey on ICT, 2008-19 (20) $\rightarrow$ ERP, ICT, robots
d) EAE Industrie: annual business survey, 1994-2007 $\rightarrow$ export, outsourcing

Results

## Constant Bargaining Power


(a) United States

(b) France

## Trends in Bargaining Power


(a) United States

(b) France

## Trends in Bargaining Power


(a) United States

(b) France

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change


Figure: FR Manufacturing

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change
- Technological differences


Figure: FR Manufacturing

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change
- Technological differences
- Product market power


Figure: FR Manufacturing

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change
- Technological differences
- Product market power
- Intra-firm bargaining


Figure: FR Manufacturing

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change
- Technological differences
- Product market power
- Intra-firm bargaining

2. Worker Heterogeneity

- Sorting


Figure: FR Manufacturing

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change
- Technological differences
- Product market power
- Intra-firm bargaining

2. Worker Heterogeneity

- Sorting
- Occupation composition


Figure: FR Manufacturing

## Trends in Bargaining Power - Robustness

1. Firm Heterogeneity

- Technical change
- Technological differences
- Product market power
- Intra-firm bargaining

2. Worker Heterogeneity

- Sorting
- Occupation composition
- Worker information


Figure: FR Manufacturing

## Why Is This Important?

Compare steady states with highest and lowest WBP

Table: United States

| Variable | Model |  |  | Data |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | 80 s | 10 s |  | 80 s | 10 s |
| Unemp | 7.3 | 6.1 |  | 7.3 | 6.3 |
| W/P | 1 | 0.91 |  | 1 | 0.72 |
| Barg. Power | 0.34 | 0.15 |  | 0.34 | 0.15 |

$\rightarrow$ policy interventions!

What Happened to Bargaining Power?

## What Happened to Bargaining Power?

Find the sources of the decline

- distinguish firms and workers according to specific characteristics
- estimate differential BP

$$
\begin{array}{ccc}
w_{i t}^{A}=\tau^{A} \mathrm{MPN}_{i t}+\Omega_{i t}^{A}+\varepsilon_{i t}^{A} & \text { vs } & w_{i t}^{B}=\tau^{B} \mathrm{MPN}_{i t}+\Omega_{i t}^{B}+\varepsilon_{i t}^{B} \\
w_{j i t}^{A}=\tau^{A} \mathrm{MPN}_{j i t}+\Omega_{j i t}^{A}+\varepsilon_{j i t}^{A} & \text { vs } & w_{j i t}^{B}=\tau^{B} \mathrm{MPN}_{j i t}+\Omega_{j i t}^{B}+\varepsilon_{j i t}^{B}
\end{array}
$$

Two purposes

1. show differences across groups
2. study differential trends

## Sources of Decline in Worker Bargaining Power


(a) Technology

(b) Trade

## Sources of Decline in Worker Bargaining Power


(a) Gender

(b) Occupation

## Conclusions

Propose a novel method for estimating worker bargaining power
Measure time-varying bargaining power uncovering an aggregate decline
Help reconcile unemployment and labor share trends and design policy interventions

Such a decline is concentrated in non routine occupations and male workers

- technology, competition, trade, and outsourcing seem to play a smaller role

Ongoing projects: link to labor force participation, the effect of COVID

> Thank you!
> paolo.mengano@uzh.ch

Appendix

## Non Profit Condition

$$
\underbrace{\kappa}_{\text {Vacancy cost }}=\underbrace{\beta \mathbb{E}\left[q\left(\theta_{t}\right) J_{i t+1}\right]}_{\text {Expected profits }}
$$

## Worker Problem

Workers

$$
\begin{aligned}
& E_{t}=w_{t}+\beta \mathbb{E}\left[(1-s) E_{t+1}+s U_{t+1}\right] \\
& U_{t}=b_{t}+\beta \mathbb{E}\left[p\left(\theta_{t}\right) E_{t+1}+\left(1-p\left(\theta_{t}\right)\right) U_{t+1}\right]
\end{aligned}
$$

Surplus from becoming employed:

$$
E_{t}-U_{t}=w_{t}-b_{t}+\beta \mathbb{E}\left[\left(1-s-p\left(\theta_{t}\right)\right)\left(E_{t+1}-U_{t+1}\right)\right]
$$

## Firm Problem

Firm problem

$$
\begin{aligned}
\Pi_{t}= & \max _{v_{t}, k_{t}} \pi_{t}+\beta \mathbb{E}\left[\Pi_{t+1}\right] \\
\text { s.t. } & N_{t+1}=(1-s) N_{t}+V_{t} q\left(\theta_{t}\right) \\
& A_{t+1}=g\left(A_{t}\right)+\nu_{t+1}
\end{aligned}
$$

with $\pi_{t}=F\left(A_{t}, N_{t}\right)-w_{t} N_{t}-\kappa_{t} V_{t}$

## Labor Market

Random search frictions: workers and firms meet at random

Matching function

- CRS, increasing in v and u
- $M(v, u)=A v^{\alpha} u^{1-\alpha}$

Tightness ratio: $\theta=\frac{v}{u}$
Exogenous separation: s
Job filling rate: $q(\theta)=\frac{M}{v}$
Job finding rate: $p(\theta)=\frac{M}{u}=\theta q(\theta)$

## Summary Statistics for France

Table: Summary statistics
(a) Firms

|  | p1 | p25 | p50 | p75 | p99 | Mean | N |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sales | 113 | 510 | 1,041 | 2,406 | 41,756 | 3,231 | $8,987,284$ |
| Value Added | 35 | 186 | 353 | 754 | 9,818 | 877 | $8,856,811$ |
| Materials | 1 | 107 | 334 | 998 | 24,605 | 1,566 | $8,987,284$ |
| Capital | 5 | 106 | 270 | 733 | 19,528 | 1,223 | $8,987,284$ |

(b) Workers

|  | p1 | p25 | p50 | p75 | p99 | Mean | N |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Wages | 5.5 | 10.0 | 12.1 | 15.9 | 43.3 | 14.2 | $227,043,310$ |

Notes: this table shows summary statistics for firms and employees in the sample of analysis. All variables are real. Values for firms are in thousands of Euros, values for employees are in Euros.

## Summary Statistics for the US

Table: Summary Statistics

|  | All | Reporting | Non-Reporting | $\Delta$ |
| :--- | :---: | :---: | :---: | :---: |
| Revenues | 1,185 | 3,849 | 924 | $2,925^{* * *}$ |
| Capital | 345 | 1,259 | 256 | $1,003^{* * *}$ |
| Employees | 6 | 21 | 5 | $16^{* * *}$ |
| Wages | 35 | 35 | . | . |
| Observations | 128,757 | 13,794 | 114,963 |  |

Revenues and Capital are expressed in USD millions;
Number of Employees and Wages in thousands of workers and USD, respectively

## Calibration

| Parameter | US |  |  |  | France |  |
| :--- | :---: | :---: | :--- | :--- | :---: | :---: |
|  | Value | Source |  | Value | Source |  |
| Productivity $(z)$ | 1 | normalization |  | 1 | normalization |  |
| Discount factor $(\beta)$ | 0.99 | $4 \%$ annual interest |  | 0.99 | $4 \%$ annual interest |  |
| Bargaining power $(\tau)$ | 0.34 | own estimation |  | 0.28 | own estimation |  |
| Outside option $(\mathrm{b})$ | 0.4 | Shimer (2005) |  | 0.6 | Cahuc et al. (2010) |  |
| Separation rate $(s)$ | 0.1 | 2001q1-2019q4 |  | 0.02 | Hairault et al. (2015) |  |
| Matching elasticity $(\alpha)$ | 0.22 | Lange et al. (2020) |  | 0.5 | Cahuc et al. (2010) |  |
| Matching scale $(A)$ | 1 | normalization |  | 0.1 | normalization |  |

Calibration $\kappa$ to match unemployment rate

## Why Is This Important?

Compare steady states with highest and lowest WBP

Table: France

| Variable | Model |  |  | Data |  |
| :--- | :---: | :---: | :--- | :--- | :---: |
|  | 95 | 18 |  | 95 | 18 |
| Unemp | 11.8 | $\mathbf{9 . 2}$ |  | 11.8 | $\mathbf{9 . 0}$ |
| W/P | 1 | $\mathbf{0 . 9 4}$ |  | 1 | $\mathbf{0 . 9 9}$ |
| Barg. Power | 0.28 | 0.16 |  | 0.28 | 0.16 |

$\rightarrow$ policy interventions!

## Bargaining Power in the United States



Figure: US Manufacturing


Figure: Work Stoppages

## Bargaining Power in France



Figure: FR Manufacturing


Figure: FR Total Economy

## Bargaining Power by Size



Figure: Constant


Figure: Time-varying

## Trends in Bargaining Power: Regional Differences*



Figure: Bargaining Power


Figure: HHI (employment)

Trends in Bargaining Power: Industry Breakdown


Trends in Bargaining Power: Breakdown in Manufacturing


Figure: Bargaining Power

## Bargaining vs Markdowns




## Measuring Workers' Productivity

$$
\mathrm{MPN}=\frac{\partial F(\cdot)}{\partial N}=\epsilon_{Y, N} \frac{Y}{N}
$$

$\varepsilon_{Y, L}$ is unobservable and recovering it presents many challenges (Ackerberg et al. 2015)

- technology, competition

Olley \& Pakes' intuition (control function approach):

1. firm productivity is unobservable to the econometrician but observable to the firm
$\rightarrow$ use another observable variable to infer unobserved productivity
2. exploit the stochastic (first-order Markov) process of productivity

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?

2 . what is $F(\cdot)$ ?

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $Y_{i t}=A_{i t} K_{i t}^{\epsilon_{K}} N_{i t}^{\epsilon_{L}}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=a_{i t}+\epsilon_{K} k_{i t}+\epsilon_{L} n_{i t}+\varepsilon_{i t}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

$$
\text { 1. } y_{i t}=m_{t}^{-1}\left(m_{i t}, \Omega_{i t}\right)+\epsilon_{K} k_{i t}+\epsilon_{L} n_{i t}+\varepsilon_{i t}
$$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=\phi\left(m_{i t}, k_{i t}, n_{i t}, \Omega_{i t}\right)+\varepsilon_{i t}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=\phi\left(m_{i t}, k_{i t}, n_{i t}, \Omega_{i t}\right)+\varepsilon_{i t} \rightarrow \hat{y}_{i t}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=\phi\left(m_{i t}, k_{i t}, n_{i t}, \Omega_{i t}\right)+\varepsilon_{i t} \rightarrow \hat{y}_{i t}$
2. $a_{i t}=g\left(a_{i t-1}\right)+\nu_{i t}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=\phi\left(m_{i t}, k_{i t}, n_{i t}, \Omega_{i t}\right)+\varepsilon_{i t} \rightarrow \hat{y}_{i t}$
2. $\underbrace{a_{i t}}_{\hat{y}_{i t}-\epsilon \times\{k, n\}_{i t}}=g(\underbrace{a_{i t-1}}_{\hat{y}_{i t-1}-\epsilon \times\{k, n\}_{i t-1}})+\nu_{i t}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=\phi\left(m_{i t}, k_{i t}, n_{i t}, \Omega_{i t}\right)+\varepsilon_{i t} \rightarrow \hat{y}_{i t}$
2. $\underbrace{a_{i t}}_{\hat{y}_{i t}-\epsilon \times\{k, n\}_{i t}}=g(\underbrace{a_{i t-1}}_{\hat{y}_{i t-1}-\epsilon \times\{k, n\}_{i t-1}})+\nu_{i t}$

## Control Function Approach

Aim: recover Hicks-neutral productivity as a residual: $Y=A F(\cdot) \rightarrow A=Y / F(\cdot)$
Two main challenges:

1. what is in the residual?
2. what is $F(\cdot)$ ?

Two steps:

1. $y_{i t}=\phi\left(m_{i t}, k_{i t}, n_{i t}, \Omega_{i t}\right)+\varepsilon_{i t} \rightarrow \hat{y}_{i t}$
2. $\underbrace{a_{i t}}_{\hat{y}_{i t}-\epsilon \times\{k, n\}_{i t}}=g(\underbrace{a_{i t-1}}_{\hat{y}_{i t-1}-\epsilon \times\{k, n\}_{i t-1}})+\nu_{i t}$

Value added vs Gross Output, Cobb-Douglas vs Translog, Single labor vs multiple labor types, Revenues vs Quantities

## Instruments and Fixed Effects

IV: lagged productivity $\rightarrow$ structural identification

- relevance: Markov Process
- exclusion restriction: period-by-period renegotiation

FEs: industry $\times$ year $\rightarrow$ time variation but restrictive on the cross-section

- gradually relax introducing worker dimension

Final equation:

$$
w_{i s t}=\tau \underbrace{\mathrm{MPN}_{i s t}}_{\substack{\mathrm{MPN}_{i s t-1}}}+\Omega_{i s t}+\varepsilon_{i s t}
$$

## Technical Change



Figure: US


Figure: FR Manufacturing

Allowing the production function to vary every year

## Alternative Production Function: Translog



Figure: US


Figure: France
flexible and firm-specific production function:

$$
y_{i t}=a_{i t}+\beta_{K} 1 k_{i t}+\beta_{K} 2 k_{i t}^{2}+\beta_{L} 1 n_{i t}+\beta_{L} 2 n_{i t}^{2}+\beta_{K} L k_{i t} n_{i t}+\varepsilon_{i t}
$$

## Bargaining Power with Heterogeneous Markups

Wage equation with market power in the output market

$$
w=\tau \mathrm{MRPN}+(1-\tau) b+\tau \theta \kappa
$$

Hence, in need of MRPN!
It takes the form: $\operatorname{MRPN}=\frac{\beta_{L}}{\mu} \frac{P Y}{N} \rightarrow$ De Loecker \& Warzynski's approach

## Bargaining Power with Heterogeneous Markups



Figure: US


Figure: FR Manufacturing

## Wages with Multi-Worker Negotiation

Firms internalize effect of new hire on existing workforce:
$w=\tau\left(\operatorname{MPN}-N \frac{\partial w}{\partial N}\right)+(1-\tau) b+\tau \theta \kappa$

## Wages with Multi-Worker Negotiation

Firms internalize effect of new hire on existing workforce:

$$
\begin{aligned}
& w=\tau\left(\mathrm{MPN}-N \frac{\partial w}{\partial N}\right)+(1-\tau) b+\tau \theta \kappa \\
& w N^{\frac{1}{\tau}}=\int \frac{\mathrm{MPN}}{N^{1-\frac{1}{\tau}}} d N+[(1-\tau) b+\tau \theta \kappa] N^{\frac{1}{\tau}}+C_{2}
\end{aligned}
$$

## Wages with Multi-Worker Negotiation

Firms internalize effect of new hire on existing workforce:
$w=\tau\left(\mathrm{MPN}-N \frac{\partial w}{\partial N}\right)+(1-\tau) b+\tau \theta \kappa$

$$
w N^{\frac{1}{\tau}}=\int \frac{\mathrm{MPN}}{N^{1-\frac{1}{\tau}}} d N+[(1-\tau) b+\tau \theta c] N^{\frac{1}{\tau}}+C_{2}
$$

Additional assumptions:

1. Cobb-Douglas: $Y=A N^{\beta_{L}} K^{\beta_{K}} \quad \Rightarrow \quad \mathrm{MPN}=\beta_{L} \frac{Y}{N}$

$$
w=\frac{1}{\left(\beta_{L}+\frac{1}{\tau}-1\right)} \mathrm{MPN}+(1-\tau) b+\tau \theta \kappa+C_{3} N^{-\frac{1}{\tau}}
$$

## Wages with Multi-Worker Negotiation

Firms internalize effect of new hire on existing workforce:
$w=\tau\left(\mathrm{MPN}-N \frac{\partial w}{\partial N}\right)+(1-\tau) b+\tau \theta \kappa$

$$
w N^{\frac{1}{\tau}}=\int \frac{\mathrm{MPN}}{N^{1-\frac{1}{\tau}}} d N+[(1-\tau) b+\tau \theta c] N^{\frac{1}{\tau}}+C_{2}
$$

Additional assumptions:

1. Cobb-Douglas: $Y=A N^{\beta_{L}} K^{\beta_{K}} \quad \Rightarrow \quad \mathrm{MPN}=\beta_{L} \frac{Y}{N}$

$$
w=\frac{1}{\left(\beta_{L}+\frac{1}{\tau}-1\right)} \mathrm{MPN}+(1-\tau) b+\tau \theta \kappa+C_{3} N^{-\frac{1}{\tau}}
$$

2. $\lim _{N \rightarrow 0} \underbrace{N w}_{\text {Labor Cost }}=0 \Rightarrow C_{3}=0$

$$
w=\frac{1}{\left(\beta_{L}+\frac{1}{\tau}-1\right)} \mathrm{MPN}+(1-\tau) b+\tau \theta \kappa
$$

## The Role Of Sorting



Figure: US


Figure: France

Estimation in first differences
$\rightarrow$ Preliminary: don't find evidence for increasing sorting

## Controlling For Occupation Composition

Intuition: include occupation-specific components (FEs) (Wong, 2021; Chen et al., 2020)

Step 1: estimate occupation FEs (on random subsample, 20\%)

$$
\ln w_{j i t}^{o}=\underbrace{\alpha_{t}^{o}}_{\text {occupation FEs }}+\underbrace{\psi_{i(j, t), t}}_{\text {firm } \times \mathrm{t} \text { FEs }}+\underbrace{X_{j t} \Gamma_{t}}_{\text {worker controls }}+\varepsilon_{j i t}
$$

Step 2: construct firm-level "labor bundle" in efficiency units

$$
\tilde{H}_{i t}=\sum_{j} \exp \left(\alpha_{t}^{o}\right) h_{j i t}^{o}
$$

$\ldots$ estimate PFE, $Y_{i t}=F_{t}\left(A_{i t}, \tilde{H}_{i t}, K_{i t}\right)$, and BP

## Comparing Occupation and Worker Ability



Figure: Occupation Ability


Figure: Worker Ability from $8 \%$ of workforce

## Bargaining Power Controlling For Occupation Composition



Figure: FR Total Economy


Figure: FR Manufacturing

## Including Worker Information

$$
w_{j i t}=\tau_{t} M P L_{i t}+X_{j t} \Gamma_{t}+\delta_{s t}+\varepsilon_{j i t}
$$

with $X_{j t}$ including:

- polynomial in age
- gender, region, contract dummies


Figure: FR Manufacturing

