# Optimal Exit Policy with Uncertain Demand 

Michele Bisceglia Jorge Padilla Joe Perkins Salvatore Piccolo

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- Does this tell the whole story about exit?


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- If demand is lower than expected, firms may wish to exit, for instance through bankruptcy or merger
- Terms of exit can therefore have an important effect on ex ante investment incentives of market newcomers
- Q: How does exit policy affect investment incentives and consumer welfare when investments are sunk and demand is uncertain?
- Exit has a selection effect with strategic implications


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- Exit has a selection effect with strategic implications
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- Under-investment problem can be solved by a lenient exit policy
- With higher demand uncertainty, consumer welfare maximization requires lower exit barriers
- Application: Mergers


## Literature

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- Dynamic merger policy. Mermelstein et al. (2020), Gilbert-Katz (2021), Mason-Weeds (2013): Symmetric information in takeover game


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$$
t=1
$$

Firm 0:
$I \in\{0,1\}$

$$
t=2
$$

Firm 0:
Observes $\theta$
Exit decision

$$
t=3
$$

Monopoly or
Bayes-Cournot game

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- $\theta^{\star}(1, K)<\theta^{\star}(0, K)$ for all $K$
- $\theta^{\star}(I, K)$ increasing in $K$ for all $I$


## Equilibrium: Investment Stage

- Firm 0's expected profit

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\pi_{0}^{\star}(I, K) \triangleq \underbrace{\int_{-\sigma}^{\theta^{\star}(I, K)} K \frac{d \theta}{2 \sigma}}_{\text {Exit value }}+\underbrace{\int_{\theta^{\star}(I, K)}^{\sigma} x_{0}^{\star}(\theta, I, K)^{2} \frac{d \theta}{2 \sigma}}_{\text {Market value }}
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- Value of investment $\Delta \pi_{0}(K)=\pi_{0}^{\star}(1, K)-\pi_{0}^{\star}(0, K)$ :

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- $\Delta \pi_{0}(\cdot)>0$ for all $K \in[0, \bar{K}] \Longrightarrow I^{\star}=1$ iff $\psi \leq \Delta \pi_{0}(K)$


## Investment and Exit Value

- Differentiating $\Delta \pi_{0}(\cdot)$ w.r.t. $K$ gives
$\underbrace{-\int_{\theta^{\star}(1, K)}^{\theta^{\star}(0, K)} \frac{d \theta}{2 \sigma}}_{\text {Exit effect }(-)}+\underbrace{\int_{\theta^{\star}(0, K)}^{\sigma} \underbrace{\frac{\partial x_{0}^{\star}(\cdot)}{\partial \theta^{\star}(\cdot)} \frac{\partial \theta^{\star}(\cdot)}{\partial K}}_{+} \underbrace{\left[x_{0}^{\star}(\theta, 1, K)-x_{0}^{\star}(\theta, 0, K)\right]}_{+} \frac{d \theta}{\sigma}}_{\text {Selection effect }(+)}$


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- $\Delta \pi_{0}(K)$ is single peaked in $K$ and features a maximum at

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K^{\star} \triangleq\left(\frac{b^{2}(2 \sigma+\mu(1-b))}{8\left(4-b^{2}\right)}\right)^{2} \in(0, \bar{K})
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- $K^{\star}$ is increasing in $\sigma$


## Consumer Surplus

- Expected consumer surplus $C S(I, K)$

$$
\int_{-\sigma}^{\theta^{\star}(I, K)} \underbrace{\frac{\mu^{2}}{8}}_{C^{M}} \frac{d \theta}{2 \sigma}+\int_{\theta^{\star}(I, K)}^{\sigma} \underbrace{\left[\frac{1}{2} \sum_{i=0,1} x_{i}^{\star}(\cdot)^{2}+b x_{0}^{\star}(\cdot) x_{1}^{\star}(\cdot)\right]}_{C S^{D}(\theta, I, K)} \frac{d \theta}{2 \sigma}
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$$

- Social value of investment: $\triangle C S(K) \triangleq C S(1, K)-C S(0, K)$ :

$$
\begin{aligned}
& \Delta C S(K)=\underbrace{\int_{\theta^{\star}(1, K)}^{\theta^{\star}(0, K)}\left(\operatorname{CS}^{D}(\theta, 1, K)-C S^{M}\right) \frac{d \theta}{2 \sigma}}_{\text {Switch to duopoly }(+)}+ \\
& +\underbrace{\int_{\theta^{\star}(0, K)}^{\sigma}\left(\operatorname{CS}^{D}(\theta, 1, K)-C^{D}(\theta, 0, K)\right) \frac{d \theta}{2 \sigma}}_{\text {Investment effect in duopoly }(+)}
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- $\Delta C S(K)>0 \Longrightarrow$ Under-investment problem for $\psi>\Delta \pi_{0}(K)$


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- Results:
- $K^{\star \star}(1)=0$
- $K^{\star \star}(0) \in\left(0, K^{\star}\right)$ iff $b>b_{0}^{\star}$ and $\sigma<\sigma_{0}^{\star}$; otherwise $K^{\star \star}(0)=0$


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- Trivial cases


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- If regulator wants to induce $I=1$, solves

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\max _{K \in[0, \bar{K}]} C S(1, K) \\
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Solution (for all $\psi \in \Psi$ ): $K=\widehat{K} \triangleq \Delta \pi_{0}^{-1}(\psi) \in\left[0, K^{\star}\right]$, increasing in $\psi$

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\text { s.t. } \psi \leq \Delta \pi_{0}(K)
\end{array}\right.
$$

Solution (for all $\psi \in \Psi$ ): $K=\widehat{K} \triangleq \Delta \pi_{0}^{-1}(\psi) \in\left[0, K^{\star}\right]$, increasing in $\psi$

- Otherwise just sets $K=K^{\star \star}(0)$


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The region of parameters $\psi$ expands as $\sigma$ grow large

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$$
t=1 \quad t=2 \quad t=3
$$

Firm 0:
$I \in\{0,1\}$

Firm 1: Takeover offer $K$
Firm 0: Observes $\theta$, accepts or refuses $K$

Monopoly or
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- $\psi>\bar{\psi}$ : Incumbent not willing to offer $K^{P}$ $\Longrightarrow I=0, K^{e}=0$ : merger never takes place


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- Trade-off between encouraging more firms to stay in the market and stimulating ex-ante investment
- Industries in which investments are costly require relatively lenient merger/liquidation policies to secure investments


## Thank you!

## Comments are Welcome.

Michele Bisceglia (michele.bisceglia@tse-fr.eu) Jorge Padilla (JPadilla@compasslexecon.com) Joe Perkins (JPerkins@compasslexecon.com) Salvatore Piccolo (salvatore.piccolo@unibg.it)

