

Optimal Regulation of Credit Lines

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- Despite their importance, the literature on CLs is relatively scarce

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 - Funds are drawn down even though they are still not needed

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 - Ivashina and Scharfstein (2010), Ippolito et al. (2016), Fernandez-Lafuerza and Gutierrez (2022)
- Bank regulation
 - Perotti and Suarez (2011), Stein (2012), Gersbach and Rochet (2012), Segura and Suarez (2017), Kara and Ozsoy (2010)

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 2. **Banks** channel funds from investors to firms by means of CLs
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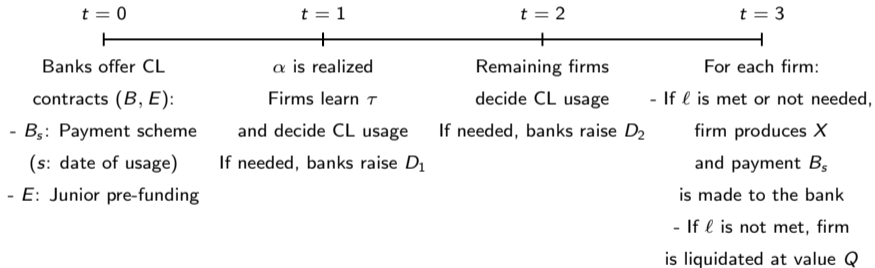
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- At $t = 1$, the fraction α of firms in need of funds is publicly revealed
 - Firms privately learn at $t = 1$ whether and when cash will be needed

Sequence of events



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- Firms' demand for liquidity will be equal to $\alpha \equiv \alpha_1 + \alpha_2 \leq 1$
- **Simplification:** $\alpha_1 = 0$ and $\alpha = \alpha_2 \sim f(\cdot)$ is publicly revealed at $t = 1$

Firms (II)

- At $t = 3$, the firm produces a cash flow

$$\tilde{x} = \begin{cases} X, & \text{if not liquidated,} \\ Q(z), & \text{if liquidated,} \end{cases}$$

where z is the aggregate size of liquidations and $Q' < 0$

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- At most $Y < X$ can be pledged to outsiders
- Access to an alternative investment that yields a private return $\rho < 1$

Assumptions

A1. Continuation return $>$ Liquidation return

$$X - R_1 > Q(0)$$

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A3. Firms in need of funds prefer investing funds in the project over investing them at ρ

$$\rho < X - Y$$

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- The bank commits to raise pre-arranged funding per committed funds equal to E and invest it in cash at $t = 0$
- Pre-arranged funding E is junior to funding raised at $t = 1, 2$ (e.g., LT debt or equity)

The Allocation Problem

- In high liquidity need states, α may not be met: $D_1 + D_2 < \alpha - E$
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- Junior pre-funding E helps to sustain lending over a wider range of α 's
 - Claims associated to E can be diluted to raise additional funds at $t = 1, 2$
 - Yet, pre-funding E demands a higher return

Solving for the unregulated CL contract

The representative bank's problem:

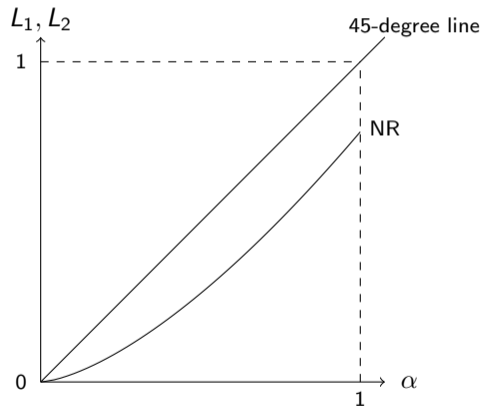
- **Given aggregate liquidations $z(\alpha)$** , the expected payoff of the representative firm is maximized subject to
 1. Some incentive compatibility constraints that prevent opportunism
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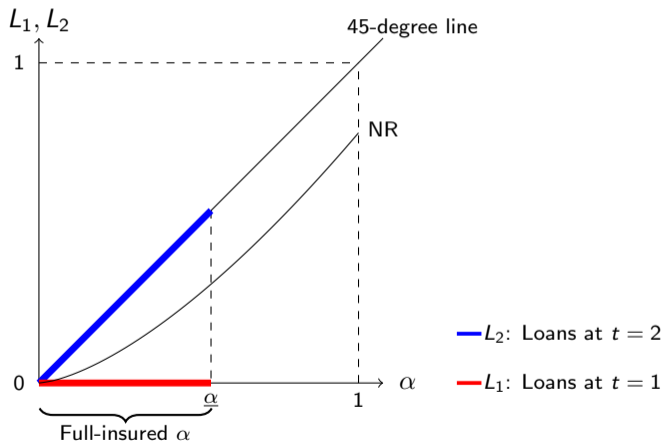
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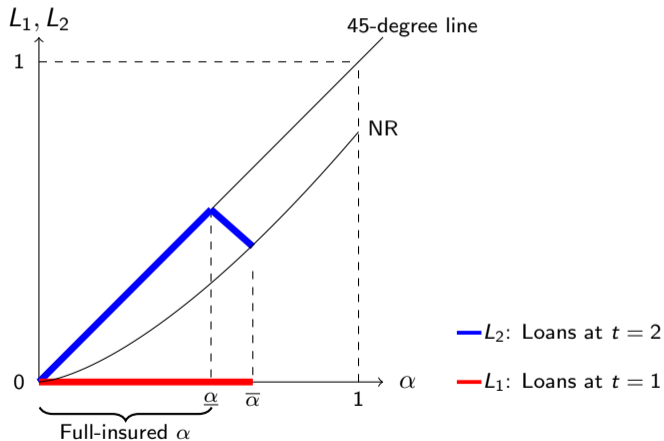
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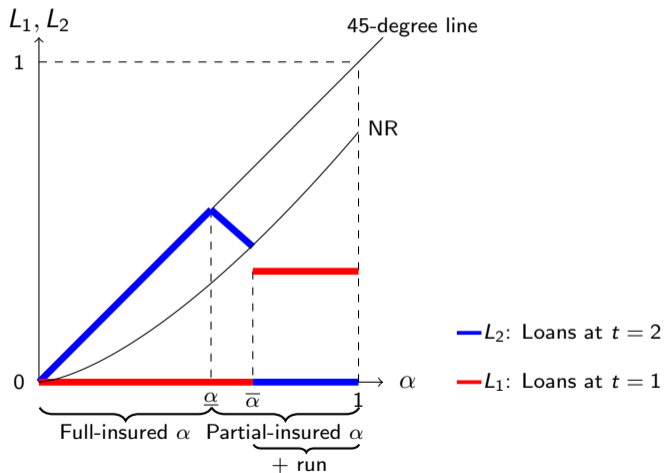
- **Given aggregate liquidations $z(\alpha)$** , the expected payoff of the representative firm is maximized subject to
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- (+) Symmetric eq. can fully characterize the unregulated CL (B^U, E^U)

CL performance given (B, E) for every α



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- If high realizations of α are rare, E is optimally chosen s.t. the unregulated CL contract features liquidations & runs
- Banks do not internalize the effect of liquidations on eq. liquidation values
 - Scope for regulation

Solving for the constrained efficient CL contract

The social planner's problem:

- The expected payoff of the representative firm is maximized subject to
 1. Some incentive compatibility constraints that prevent opportunism
 2. The participation constraint of investors who provide E
 3. **Aggregate liquidations**

Constrained efficient CL contract

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- Socially desirable to increase $E > E^U$

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 - A reduction in the occurrences of CL runs

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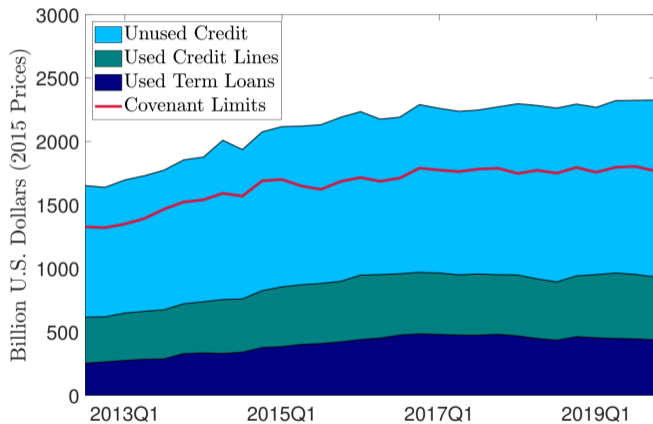
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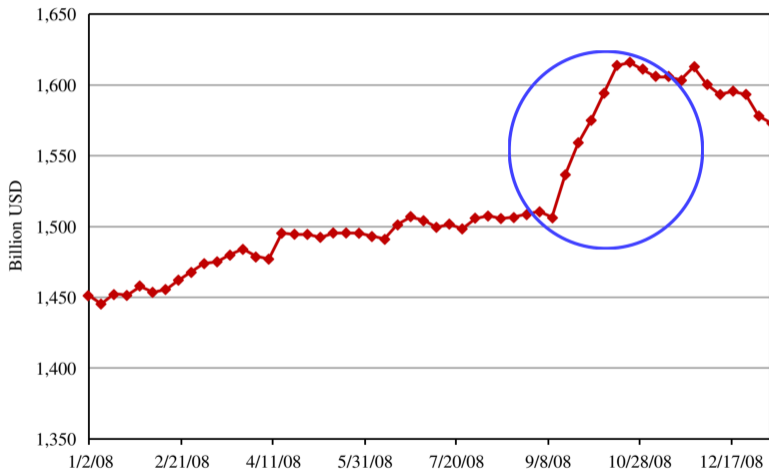
Appendices

Aggregate Term Loans and Credit Lines in the U.S.



Source: Greenwald, Krainer, and Paul (2020) [◀ go back](#)

Commercial and Industrial Bank Credit in the U.S.



Source: Ivashina and Scharfstein (2010) [◀ go back](#)