Joint Search over the Life Cycle

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Motivation

- Individual earnings/unemployment risk is large & varies by age
- Insurance margin for couples: Spousal labor supply
- Added Worker Effect (AWE):

Labor force entry of spouse upon job loss of primary earner

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This Paper:

- Document heterogeneity in the AWE by age from U.S. micro data
 - AWE larger for young than for old
- Construct a life-cycle model of couples
 - frictional labor market, human capital formation, asset accumulation
- Counterfactuals: No need for AWE among old or no opportunity?

- Main earner job loss raises prob. of spouse joining labor force by 6pp
- Effect very heterogeneous by age
 - Age 25-35: 7.5pp
 - Age 56-65: 1.4pp

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 - across education groups
 - across genders
 - across family types (children, excluding retired)
 - over the business cycle
 - across datasets (CPS, SIPP)

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 - across family types (children, excluding retired)
 - over the business cycle
 - across datasets (CPS, SIPP)
- Reason for age differential? Different needs or opportunities?

- Life cycle search model with couple households who differ in
 - their labor market status: employed, searching, not searching
 - labor market experience: human capital accumulation
 - asset holdings: consumption-savings choice

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- Firms post vacancies in markets characterized by household states
 - Age differential in arrival rates
- Model reproduces age differential in added worker effect
- Model counterfactuals
 - $-\,$ significant role for differential asset holdings across age groups
 - smaller roles for differential arrival rates and human capital

Literature

Evidence

- US data from Current Population Survey (CPS) IPUMS CPS (Flood, King, Rodgers, Ruggles, and Warren 2020)
 - Monthly rotating panel
 - $-\,$ Waves from 1994 to 2020

- US data from Current Population Survey (CPS) IPUMS CPS (Flood, King, Rodgers, Ruggles, and Warren 2020)
 - Monthly rotating panel
 - Waves from 1994 to 2020
- Restrict sample to couples (primary earner + spouse)
 - Both members between 25 and 65 years old
 - Focus on one employed and one out of labor force

The Added Worker Effect

	Primary ear	Primary earner transition	
	EE	EU	
Cond. prob. of spousal NE transition	6.03%	8.01%	
Cond. prob. of spousal NU transition	1.63%	5.55%	
Cond. prob. of spousal NN transition	92.34%	86.44%	

▶ With EN

The Added Worker Effect

	Primary earner transition	
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Cond. prob. of spousal NE transition	6.03%	8.01%
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▶ With EN

- Conditional on primary earner transitioning to unemployment
 - Higher probability of spouse entering labor force as employed
 - Higher probability of spouse entering labor force as unemployed
- Increase of roughly 6pp

Regression of spousal labor market transition on head's transition to U:

$$\Delta LFS_{it}^{sp} = \alpha_j + \beta_j \Delta ES_{it+j}^h + \gamma_j X_{it} + \epsilon_{jit}$$

- \blacksquare Repeat analysis for $j=\{-2,-1,0,1,2\}$
- ΔLFS_{it}^{sp} : Change in labor force status of spouse from $t-1 \rightarrow t$
- ΔES_{it}^h : Change in employment status of head from $t 1 \rightarrow t$

 $i=\text{couple};\,t=\text{month};\,h=\text{head};\,\text{sp}=\text{spouse};\,X=\text{add. controls}~(\text{Unemployment Rate, month FE, year FE, state FE, sex, race, education, children})$

The Added Worker Effect



Reasons for unemployment

Added Worker Effect: Heterogeneity by Age

	Primary earner transition		
	EE	EU	
Young (25-35):			
Cond. prob. of spousal NE transition	6.66%	9.30%	
Cond. prob. of spousal NU transition	2.00%	6.89%	
Cond. prob. of spousal NN transition	91.34%	83.81%	
Old (56-65):			
Cond. prob. of spousal NE transition	4.29%	3.73%	
Cond. prob. of spousal NU transition	0.90%	2.75%	
Cond. prob. of spousal NN transition	94.81%	93.52%	

■ Added worker effect larger for young: 7.53% vs. 1.29%



Added Worker Effect: Heterogeneity by Age



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Added Worker Effect: Heterogeneity by Age



Overall: Strong AWE for young, weaker for old

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Model

Two-member households with **five states**:

Two-member households with five states: (t,

1. Age:

- T periods: work for $T_W < T$, retired for $T - T_W$

Two-member households with five states: (t, jk,

1. Age:

- T periods: work for $T_W < T$, retired for $T T_W$
- 2. Joint Labor Market Status:
 - employed (E), unemployed with benefits (U), unemployed without benefits (S) or non-participating (N)
 - joint labor status $jk \in \mathcal{J} = \{E, U, S, N\} \times \{E, U, S, N\}$

Two-member households with five states: (t, jk, z,

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- 3. Match Quality $(z = (z_1, z_2))$:
 - only for employed members Exogenous Process

Two-member households with five states: (t, jk, z, h,

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Transitions

- joint labor status $jk \in \mathcal{J} = \{E, U, S, N\} \times \{E, U, S, N\}$
- 3. Match Quality $(z = (z_1, z_2))$:
 - only for employed members Exogenous Processes
- 4. Human Capital $(h = (h_1, h_2))$:
 - accumulate while E, de-cumulate while U, S, N

Exogenous Processes

Two-member households with five states: (t, jk, z, h, a)

1. Age:

- T periods: work for $T_W < T$, retired for $T T_W$
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Transitions

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Exogenous Processes

5. **Assets:**

- risk free bond at interest rate \boldsymbol{r}

Consumption-Savings Choice

$$V_t^{jk}(z, h, a) = \max_{a'} u(c^{jk}(z, h, a, a')) + \psi_t^{jk} + \beta \Theta_{t+1}^{jk}(z, h, a')$$

• Value consumption u(c) (pooled within HH)



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■ Additional instantaneous utility ψ_t^{jk} ⇒ Utility of staying at home and dis-utility of search

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• Value consumption u(c) (pooled within HH)



- Additional instantaneous utility ψ_t^{jk}
 ⇒ Utility of staying at home and dis-utility of search
- Continuation value $\Theta^{jk}_t(z,h,a')$ · Continuation Value · Choice Sets

Vacancy Posting and Arrival Rates

- Output of a match and wages
 - $\ \operatorname{Output}\, y\left(z,h\right) = zh$
 - $\ \, {\rm Wage} \ \, w\left(z,h\right) = \chi y\left(z,h\right)$

Vacancy Posting and Arrival Rates

- Output of a match and wages
 - $\text{ Output } y\left(z,h\right) = zh$
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 - Vacancy posting problem of single worker firm
 - Free entry with vacancy posting cost κ
 - Markets conditional on household state variables

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 - Markets conditional on household state variables
- Scaled by search intensity
 - Equal intensities $\lambda_U = \lambda_S$ for unemployed
 - Lower intensity λ_N for out of the labor force

Firm Problem

Calibration: Joint Labor Market States

- Model period is a month: 40 years of working life \rightarrow 480 periods
- Target joint labor market states, income/asset profiles, flows,

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- Model period is a month: 40 years of working life \rightarrow 480 periods
- Target joint labor market states, income/asset profiles, flows, ...



The Added Worker Effect in the Model

Joint Labor Market Transitions	by	Age	(Model vs.	Data
--------------------------------	----	-----	------------	------

	Primary earner transition	
	EE	EU/ES
Young (25-35):		
Cond. prob. of spousal NE transition	2.26%	3.12%
	6.66%	9.30%
Cond. prob. of spousal NS transition	0.40%	5.28%
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Cond. prob. of spousal NN transition	97.34%	91.60%
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Old (55-65):		
Cond. prob. of spousal NE transition	1.95%	2.24%
	4.29%	3.73%
Cond. prob. of spousal NS transition	0.11%	1.16%
	0.90%	2.75%
Cond. prob. of spousal NN transition	97.95%	96.60%
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The Added Worker Effect in the Model

Joint Labor Market Tra	ansitions by Age	(Model vs.	Data
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AWE for young: 5.74% 7.53%

The Added Worker Effect in the Model

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	94.81%	93.52%

AWE for old: 1.35% 1.29%

Which factors explain the change in the AWE over the life cycle?

- Three candidates: arrival rates, human capital, assets
- Compute average values of old and young along each dimension
- Adjust every young household's state such that
 - On average, young have characteristics of old
 - Preserves within young position in distribution

The AWE over the Life Cycle: Counterfactuals

	Primary ear	Primary earner transition	
	EE	EU/ES	
Young (25-35):			
Cond. prob. of spousal NE transition	2.26%	3.12%	
Cond. prob. of spousal NS transition	0.40%	5.28%	
Cond. prob. of spousal NN transition	97.34%	91.60%	
Counterfactual assets			
Cond. prob. of spousal NE transition	1.04%	1.73%	
Cond. prob. of spousal NS transition	0.30%	3.31%	
Cond. prob. of spousal NN transition	98.66%	94.96%	

Higher asset holdings

■ AWE: 3.70% vs. 5.74%

The AWE over the Life Cycle: Counterfactuals

	Primary ear	Primary earner transition	
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Young (25-35):			
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Cond. prob. of spousal NS transition	0.40%	5.28%	
Cond. prob. of spousal NN transition	97.34%	91.60%	
Counterfactual human capital			
Cond. prob. of spousal NE transition	1.70%	3.02%	
Cond. prob. of spousal NS transition	0.24%	3.09%	
Cond. prob. of spousal NN transition	98.06%	93.89%	

- Approximately same human capital for out of labor force spouse
- Higher human capital for primary earner
- AWE: 4.17% vs. 5.74%

The AWE over the Life Cycle: Counterfactuals

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Young (25-35):		
Cond. prob. of spousal NE transition	2.26%	3.12%
Cond. prob. of spousal NS transition	0.40%	5.28%
Cond. prob. of spousal NN transition	97.34%	91.60%
Counterfactual meeting probabilities		
Cond. prob. of spousal NE transition	2.14%	2.93%
Cond. prob. of spousal NS transition	0.41%	5.36%
Cond. prob. of spousal NN transition	97.46%	91.71%

- Reduced meeting probabilities for young, but small effect
- New version: Larger role for arrival rates
 - Vacancy posting after exogenous separations

Conclusion

Summary

- Evidence: AWE stronger for young than for old
- Model: Life-cycle search model of two-member households
- $-\,$ Similar contributions of "no need" and "no opportunity" channels
- Next steps
 - Model estimation of new version
 - Age-dependent unemployment insurance

comments and questions very welcome: lukas.nord@eui.eu

Appendix

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Related Literature

Empirical work on the added worker effect

Lundberg (1985), Maloney (1987, 1991), Stephens (2002), Toohey (2012), Mankart and Oikonomou (2016), Guner, Kulikova,

and Valladares-Esteban (2021)

 \Rightarrow AWE over the entire life cycle

Search models with two-member households

Guler, Guvenen, and Violante (2012), Mankart and Oikonomou (2016), Fang and Shephard (2019), Wang (2019), Choi and Valladares-Esteban (2020), Birinci (2021), Morazzoni and Smirnov (2021), Bardóczy (2022), Ellieroth (2022), Fernández-Blanco (2022)

\Rightarrow Life cycle, endogenous arrival rates

■ Life-cycle search models

Chéron, Hairault, and Langot (2011, 2013), Michelacci and Ruffo (2015), Menzio, Telyukova, and Visschers (2016), Jung and Kuhn (2019), Griffy (2021)

Life-cycle family labor supply

Ortigueira and Siassi (2013), Blundell, Pistaferri, and Saporta-Eksten (2016), Haan and Prowse (2020), Wu and Krueger (2021)

 \Rightarrow Joint labor supply decisions with search frictions over life cycle

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	EE	EU (by reasons for U)			
		Layoff	Job Loser	Temp. Job ended	Job Leaver
NE	6.03%	6.13%	8.81%	7.56%	10.47%
NU	1.63%	3.51%	6.66%	6.59%	7.68%
NN	92.34%	90.35%	84.53%	85.85%	81.86%

◀ Back

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■ Layoff, potentially temporary => small AWE



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■ Layoff, potentially temporary => small AWE

■ Job loss, more permanent => larger AWE



	EE	EU (by reasons for U)				
		Layoff	Job Loser	Temp. Job ended	Job Leaver	
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■ Layoff, potentially temporary => small AWE

- Job loss, more permanent => larger AWE
- Temp. job ended, more permanent => larger AWE



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		Layoff	Job Loser	Temp. Job ended	Job Leaver	
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■ Layoff, potentially temporary => small AWE

- Job loss, more permanent => larger AWE
- Temp. job ended, more permanent => larger AWE
- Quits => joint optimization

	Primary earner transition		
	EE EU EN		
Cond. prob. of spousal NE transition	6.03%	8.01%	16.79%
Cond. prob. of spousal NU transition	1.63%	5.55%	1.33%
Cond. prob. of spousal NN transition	92.34%	86.44%	81.88%

	Primary earner transition		
	EE	EU	EN
Young (25-35):			
Cond. prob. of spousal NE transition	6.66%	9.30%	26.93%
Cond. prob. of spousal NU transition	2.00%	6.89%	2.02%
Cond. prob. of spousal NN transition	91.34%	83.81%	71.05%
Old (56-65):			
Cond. prob. of spousal NE transition	4.29%	3.73%	8.69%
Cond. prob. of spousal NU transition	0.90%	2.75%	0.56%
Cond. prob. of spousal NN transition	94.81%	93.52%	90.76%

Heterogeneity by Age: Other Age Groups

	Primary earner transition		
	EE	EU	EN
Age Spouse 36-45:			
Cond. prob. of spousal NE transition	6.73%	9.32%	26.69%
Cond. prob. of spousal NU transition	1.86%	6.37%	2.00%
Cond. prob. of spousal NN transition	91.41%	84.31%	71.30%
Age Spouse 46-55:			
Cond. prob. of spousal NE transition	6.13%	7.96%	16.62%
Cond. prob. of spousal NU transition	1.62%	4.79%	1.72%
Cond. prob. of spousal NN transition	92.25%	87.25%	81.66%

CPS vs. SIPP – Full Sample



 Δ Pr(Spouse enters LF) this month





 Δ Pr(Spouse enters LF) this month



CPS vs. SIPP - Age 56 to 65



 Δ Pr(Spouse enters LF) this month



Added Worker Effect by Net Liquid Wealth



Regression add. controls for age; Net Liquid Wealth = total wealth - home equity - vehicle equity - unsec. debt; Data Source: SIPP

Added Worker Effect by Net Liquid Wealth



Δ Pr(Spouse enters LF) this month



Stronger AWE for low wealth households

Regression add, controls for age: Net Liquid Wealth = total wealth - home equity - vehicle equity - unsec, debt; Data Source; SIPP

Heterogeneity by Age and Education

College				
	Prim	ary earner tra	insition	
	EE	EU	EN	
Spouse Young:				
Cond. prob. of spousal NE transition	7.31%	13.25%	33.25%	
Cond. prob. of spousal NU transition	1.70%	7.22%	1.29%	
Cond. prob. of spousal NN transition	90.99%	79.53%	65.46%	
Spouse Old:				
Cond. prob. of spousal NE transition	6.04%	7.72%	11.81%	
Cond. prob. of spousal NU transition	1.35%	4.87%	0.86%	
Cond. prob. of spousal NN transition	92.61%	87.41%	87.33%	

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Heterogeneity by Age and Education

-

No College

	Primary earner transition		
	EE	EU	EN
Spouse Young:			
Cond. prob. of spousal NE transition	6.30%	8.34%	21.76%
Cond. prob. of spousal NU transition	2.01%	6.28%	2.21%
Cond. prob. of spousal NN transition	91.69%	85.37%	76.03%
Spouse Old:			
Cond. prob. of spousal NE transition	4.19%	4.20%	9.41%
Cond. prob. of spousal NU transition	0.99%	2.83%	0.80%
Cond. prob. of spousal NN transition	94.82%	92.97%	89.79%

◀ Back

	Primary earner transition		
	EE	EU	EN
Spouse is a Man (Young) :			
Cond. prob. of spousal NE transition	13.54%	14.07%	44.10%
Cond. prob. of spousal NU transition	6.19%	11.69%	2.59%
Cond. prob. of spousal NN transition	80.27%	74.24%	53.31%
Spouse is a Man (Old):			
Cond. prob. of spousal NE transition	4.50%	4.59%	10.36%
Cond. prob. of spousal NU transition	1.13%	3.23%	0.63%
Cond. prob. of spousal NN transition	94.37%	92.18 %	89.01%

	Primary earner transitior EE EU EN		
Spouse born between 1960-70 (Young):			
Cond. prob. of spousal NE transition	6.98%	8.62%	21.67%
Cond. prob. of spousal NU transition	1.89%	6.70%	2.42%
Cond. prob. of spousal NN transition	91.13%	84.68%	75.92%
Spouse born between 1960-70 (Old)			
Cond. prob. of spousal NE transition	4.28%	2.94%	12.86%
Cond. prob. of spousal NU transition	1.11%	3.68%	1.04%
Cond. prob. of spousal NN transition	94.61%	93.38%	86.10%

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Children (Parents below 40)

	Primary earner transition		
	EE	EU	EN
Have Children:			
Cond. prob. of spousal NE transition	6.26%	8.71%	28.30%
Cond. prob. of spousal NU transition	1.75%	6.65%	2.31%
Cond. prob. of spousal NN transition	91.98%	84.64%	69.40%
No Children:			
Cond. prob. of spousal NE transition	9.68%	12.68%	23.69%
Cond. prob. of spousal NU transition	3.40%	8.54%	1.59%
Cond. prob. of spousal NN transition	86.91%	78.78%	74.72%

Young Children (Parents below 40)

	Primary earner transition		
	EE	EU	EN
Have Children below 5:			
Cond. prob. of spousal NE transition	5.63%	8.55%	30.09%
Cond. prob. of spousal NU transition	1.47%	6.14%	1.96%
Cond. prob. of spousal NN transition	92.90%	85.31%	67.95%
No Children below 5:			
Cond. prob. of spousal NE transition	8.08%	9.95%	24.82%
Cond. prob. of spousal NU transition	2.60%	7.80%	2.35%
Cond. prob. of spousal NN transition	89.32%	82.24%	72.82%

Reasons for Non-Participation

	Primary earner transition		
	EE	EU	EN
Excluding Retirement (Young):			
Cond. prob. of spousal NE transition	6.66%	9.32%	27.13%
Cond. prob. of spousal NU transition	2.00%	6.91%	2.06%
Cond. prob. of spousal NN transition	91.33%	83.77%	70.81%
Excluding Retirement (Old):			
Cond. prob. of spousal NE transition	4.95%	4.15%	11.45%
Cond. prob. of spousal NU transition	1.18%	3.33%	1.00%
Cond. prob. of spousal NN transition	93.87%	92.52%	87.54%

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Reasons for Non-Participation

	Primary earner transition		
	EE	EU	EN
Excluding Disabled/III (Young):			
Cond. prob. of spousal NE transition	6.55%	9.34%	27.02%
Cond. prob. of spousal NU transition	1.96%	6.94%	2.01%
Cond. prob. of spousal NN transition	91.49%	83.72%	70.97 %
Excluding Disabled/III (Old):			
Cond. prob. of spousal NE transition	4.17%	3.42%	8.53%
Cond. prob. of spousal NU transition	0.88%	2.77%	0.50%
Cond. prob. of spousal NN transition	94.95%	93.81%	90.97%

Reasons for Non-Participation

	Primary earner transitio		
		LU	LIN
Excluding Retired and Disabled/III (Young)):		
Cond. prob. of spousal NE transition	6.55%	9.36%	27.23%
Cond. prob. of spousal NU transition	1.97%	6.96%	2.05%
Cond. prob. of spousal NN transition	91.48%	83.68%	70.72%
Excluding Retired and Disabled/III (Old):			
Cond. prob. of spousal NE transition	4.74%	3.62%	11.20%
Cond. prob. of spousal NU transition	1.16%	3.40%	0.89%
Cond. prob. of spousal NN transition	94.11%	92.99%	87.91%

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By State of the Business Cycle

	Primary earner transition		
	EE	EU	EN
NBER Recession, Young			
Cond. prob. of spousal NE transition	6.48%	7.74%	22.38%
Cond. prob. of spousal NU transition	1.98%	8.73%	0.99%
Cond. prob. of spousal NN transition	91.55%	83.53%	76.63%
NBER Recession, Old			
Cond. prob. of spousal NE transition	4.14%	5.43%	7.71%
Cond. prob. of spousal NU transition	0.83%	2.76%	0.68%
Cond. prob. of spousal NN transition	95.03%	91.81%	91.61%
By State of the Business Cycle

	Primary earner transition		
	EE	EU	EN
No NBER Recession, Young			
Cond. prob. of spousal NE transition	6.68%	9.53%	27.45%
Cond. prob. of spousal NU transition	2.00%	6.63%	2.14%
Cond. prob. of spousal NN transition	91.31%	83.85%	70.41%
No NBER Recession, Old			
Cond. prob. of spousal NE transition	4.30%	3.46%	8.80%
Cond. prob. of spousal NU transition	0.91%	2.75%	0.54%
Cond. prob. of spousal NN transition	94.79%	93.79%	90.66%

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By Reasons for Unemployment





By Reasons for Unemployment





Other Age Groups





Exogenous Processes

Human Capital:

- E: increases one unit with $Pr(h'_i = h^{j+1} | h_i = h^j) = \phi^{up}(h_i)$
- U, S, N: decreases a unit with $Pr(h'_i = h^{j-1}|h_i = h^j) = \phi^{down}(h_i)$



Match quality:

- Together with job offer receive initial draw from distribution $\pi_0(z)$
- Employed *z* evolves as Markov process.

Labor Market Transitions



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Timing

Receive labor income (UI benefits) and asset income \downarrow Consumption-savings choice \downarrow Separation shocks and job offers realize \downarrow Match quality shocks and human capital transitions realize \downarrow Choose joint future labor market state from feasible subset of \mathcal{J}

Continuation value if EE today can be defined in two steps:

1. Expectation over separations and resulting choice sets:

$$\begin{aligned} \Theta_{t+1}^{EE}(z_1, z_2, h_1, h_2, a') &= \\ (1 - \delta(h_1))(1 - \delta(h_2)) \ \widetilde{V}_{t+1}(z_1, z_2, h_1, h_2, a', \mathcal{J}_{XX}^{EE}) \\ + \delta(h_1)(1 - \delta(h_2)) \ \widetilde{V}_{t+1}(z_1, z_2, h_1, h_2, a', \mathcal{J}_{UX}^{XE}) \\ + (1 - \delta(h_1))\delta(h_2) \ \widetilde{V}_{t+1}(z_1, z_2, h_1, h_2, a', \mathcal{J}_{XU}^{EX}) \\ + \delta(h_1)\delta(h_2) \ \widetilde{V}_{t+1}(z_1, z_2, h_1, h_2, a', \mathcal{J}_{UU}^{XX}) \end{aligned}$$

Continuation Value

Continuation value if *EE* today can be defined in two steps:

2. Exogenous processes and labor supply decision:

$$\begin{split} \widetilde{V}_{t+1}(z_1, z_2, h_1, h_2, a, \mathcal{J}_{QR}^{OP}) &= \\ \phi^{up}(h_1)\phi^{up}(h_2) \ \mathbb{E}_{z_1'|z_1} \mathbb{E}_{z_2'|z_2} \ \mathbb{E}_{\epsilon} \max_{\widehat{jk} \in \mathcal{J}_{QR}^{OP}} \left\{ V_{t+1}^{\widehat{jk}}(z_1, z_2, h_1, h_2, a) + \sigma \epsilon^{\widehat{jk}} \right\} \\ &+ \phi^{up}(h_1)(1 - \phi^{up}(h_2)) \ \mathbb{E}_{z_1'|z_1} \mathbb{E}_{z_2'|z_2} \ \mathbb{E}_{\epsilon} \max_{\widehat{jk} \in \mathcal{J}_{QR}^{OP}} \left\{ V_{t+1}^{\widehat{jk}}(z_1, z_2, h_1, h_2, a) + \sigma \epsilon^{\widehat{jk}} \right\} \\ &+ (1 - \phi^{up}(h_1))\phi^{up}(h_2) \ \mathbb{E}_{z_1'|z_1} \mathbb{E}_{z_2'|z_2} \ \mathbb{E}_{\epsilon} \max_{\widehat{jk} \in \mathcal{J}_{QR}^{OP}} \left\{ V_{t+1}^{\widehat{jk}}(z_1, z_2, h_1, h_2, a) + \sigma \epsilon^{\widehat{jk}} \right\} \\ &+ (1 - \phi^{up}(h_1))(1 - \phi^{up}(h_2)) \ \mathbb{E}_{z_1'|z_1} \mathbb{E}_{z_2'|z_2} \ \mathbb{E}_{\epsilon} \max_{\widehat{jk} \in \mathcal{J}_{QR}^{OP}} \left\{ V_{t+1}^{\widehat{jk}}(z_1, z_2, h_1, h_2, a) + \sigma \epsilon^{\widehat{jk}} \right\} \\ &+ (1 - \phi^{up}(h_1))(1 - \phi^{up}(h_2)) \ \mathbb{E}_{z_1'|z_1} \mathbb{E}_{z_2'|z_2} \ \mathbb{E}_{\epsilon} \max_{\widehat{jk} \in \mathcal{J}_{QR}^{OP}} \left\{ V_{t+1}^{\widehat{jk}}(z_1, z_2, h_1, h_2, a) + \sigma \epsilon^{\widehat{jk}} \right\} \\ &+ (1 - \phi^{up}(h_1))(1 - \phi^{up}(h_2)) \ \mathbb{E}_{z_1'|z_1} \mathbb{E}_{z_2'|z_2} \ \mathbb{E}_{\epsilon} \max_{\widehat{jk} \in \mathcal{J}_{QR}^{OP}} \left\{ V_{t+1}^{\widehat{jk}}(z_1, z_2, h_1, h_2, a) + \sigma \epsilon^{\widehat{jk}} \right\} \end{split}$$

where $\epsilon \in \mathbb{R}^{|\mathcal{J}_{nm}^{j\kappa}|}$ is a vector of i.i.d., mean zero extreme value shocks.

Labor Supply Choice Sets

Benefit	Job (Offer)			
Eligibility	Both	Member 1	Member 2	None
Both	$ \begin{aligned} \mathcal{J}_{UU}^{EE} &= \\ \{E, U, N\} \\ \times \{E, U, N\} \end{aligned} $	$\begin{array}{l} \mathcal{J}_{UU}^{EX} = \\ \{E,U,N\} \\ \times \{U,N\} \end{array}$	$ \begin{aligned} \mathcal{J}_{UU}^{XE} &= \\ \{U, N\} \\ \times \{E, U, N\} \end{aligned} $	$\begin{array}{l} \mathcal{J}_{UU}^{XX} = \\ \{U, N\} \\ \times \{U, N\} \end{array}$
Member 1	$\begin{array}{l} \mathcal{J}_{UX}^{EE} = \\ \{E, U, N\} \\ \times \{E, S, N\} \end{array}$	$ \begin{array}{l} \mathcal{J}_{UX}^{EX} = \\ \{E, U, N\} \\ \times \{S, N\} \end{array} $	$ \begin{aligned} \mathcal{J}_{UX}^{XE} &= \\ \{U, N\} \\ \times \{E, S, N\} \end{aligned} $	$ \begin{aligned} \mathcal{J}_{UX}^{XX} &= \\ \{U, N\} \\ \times \{S, N\} \end{aligned} $
Member 2	$\begin{array}{l} \mathcal{J}^{EE}_{XU} = \\ \{E,S,N\} \\ \times \{E,U,N\} \end{array}$	$\begin{array}{l} \mathcal{J}^{EX}_{XU} = \\ \{E,S,N\} \\ \times \{U,N\} \end{array}$	$ \begin{array}{l} \mathcal{J}_{XU}^{XE} = \\ \{S,N\} \\ \times \{E,U,N\} \end{array} $	$ \begin{aligned} \mathcal{J}_{XU}^{XX} &= \\ \{S, N\} \\ \times \{U, N\} \end{aligned} $
None	$\begin{array}{l} \mathcal{J}^{EE}_{XX} = \\ \{E,S,N\} \\ \times \{E,S,N\} \end{array}$	$\begin{array}{l} \mathcal{J}^{EX}_{XX} = \\ \{E,S,N\} \\ \times \{S,N\} \end{array}$	$ \begin{aligned} \mathcal{J}_{XX}^{XE} &= \\ \{S, N\} \\ \times \{E, S, N\} \end{aligned} $	$\mathcal{J}_{XX}^{XX} = \\ \{S, N\} \\ \times \{S, N\}$

Firm Problem

Firms' value of employing member *i*:

$$J_t^{jk}(z_i, z_{-i}, h_i, h_{-i}, a) = \pi(z_i, h_i) + \frac{1}{1+r} (1 - \delta(h_1)) \mathbb{E}_{P,R} E J_{t+1}^{jk}(z_i, z_{-i}, h_i, h_{-i}, a', \mathcal{J}_{XR}^{EP})$$

with continuation value

$$\begin{split} EJ_{t+1}^{jk}(z_i, z_{-i}, h_i, h_{-i}, a', \mathcal{J}_{QR}^{OP}) \\ &= \mathbb{E}_{h_i'|h_i} \mathbb{E}_{h_{-i}'|h_{-i}} \mathbb{E}_{z_i'|z_i} \mathbb{E}_{z_{-i}'|z_{-i}} \mathbb{E}_{j\hat{k} \in \mathcal{J}_{QR}^{OP}} \mathbb{I}_{\hat{j} = E|x'} J_{t+1}^{\hat{j}\hat{k}}(z_i', z_{-i}', h_i', h_{-i}', a') \end{split}$$

and per-period profit

$$\pi(z_i, h_i) = y(z_i, h_i) - w(z_i, h_i) = (1 - \chi)z_i h_i$$

Free entry condition determines arrival for member *i*:

 $\kappa = q(\theta_t(h_i, h_{-i}, z_{-i}, a, jk)) \mathbb{E}_{P,R} E J_{t+1}^{jk}(z_i, z_{-i}, h_i, h_{-i}, a', \mathcal{J}_{XR}^{EP})$

- incorporates endogenous acceptances and (future) quits
- \blacksquare depends on labor market transition of spouse -i
- $\Rightarrow\,$ have to solve for arrivals simultaneously if both non-employed

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Calibration – Asset Levels

	Model	Data
All	10.4	11.8
Age 25-35	2.8	3.0
Age 35-45	4.9	7.0
Age 45-55	10.6	14.6
Age 55-65	23.3	24.1

Asset Levels

■ Target: Net financial assets (incl. IRA) + vehicle equity

■ 1 unit = \$10,000

Income Levels and Dispersion						
	Level		Standard	deviation		
	Model	Data	Model	Data		
All	0.3596	0.3424	0.1363	0.2374		
Age 25-35	0.3296	0.3020	0.1172	0.2009		
Age 35-45	0.3538	0.3572	0.1341	0.2456		
Age 45-55	0.3752	0.3629	0.1429	0.2486		
Age 55-65	0.3826	0.3400	0.1511	0.2466		

- Target: Labor Income
- 1 unit = \$10,000

Calibration – Individual Labor Market Transitions



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The Added Worker Effect in the Model

